

# Control of Time-Varying Behavior

Proportional-Derivative (PD) controller: react to the immediate sensory inputs

- E.g.: yaw control
- Need a reference (or “desired”) heading

Where does this reference come from?

# Control of Time-Varying Behavior

Where does the reference come from?

- Determined by what our task is (or subtask)
- E.g.: at the current state of a mission, it may be appropriate to orient the craft in a particular direction so that it can fly back “home”

# Control of Time-Varying Behavior

Can often express a “mission” in terms of a sequence of sub-tasks (or a plan)

- But: we also want to handle contingencies when they arrive

Finite state machines are a simple way of expressing such plans and contingencies

# Finite State Machines (FSMs)

Pure FSM form is composed of:

- A set of states
- A set of possible inputs (or events)
- A set of possible outputs (or actions)
- A transition function:
  - Given the current state and an input: defines the output and the next state

# Finite State Machines (FSMs)

## States:

- Represent all possible “situations” that must be distinguished
- At any given time, the system is in exactly one of the states
- There is a finite number of these states

# Finite State Machines (FSMs)

An example: our synchronous counter

- States: ?

# Finite State Machines (FSMs)

An example: our synchronous counter

- States: the different combinations of the digits: 000, 001, 010, ... 111
- Inputs: ?

# Finite State Machines (FSMs)

An example: our synchronous counter

- Inputs:
  - Really only one: the event associated with the clock transitioning from high to low
  - We will call this “C”
- Outputs: ?



# Finite State Machines (FSMs)

An example: our synchronous counter

- Outputs: same as the set of states
- Transition function: ?

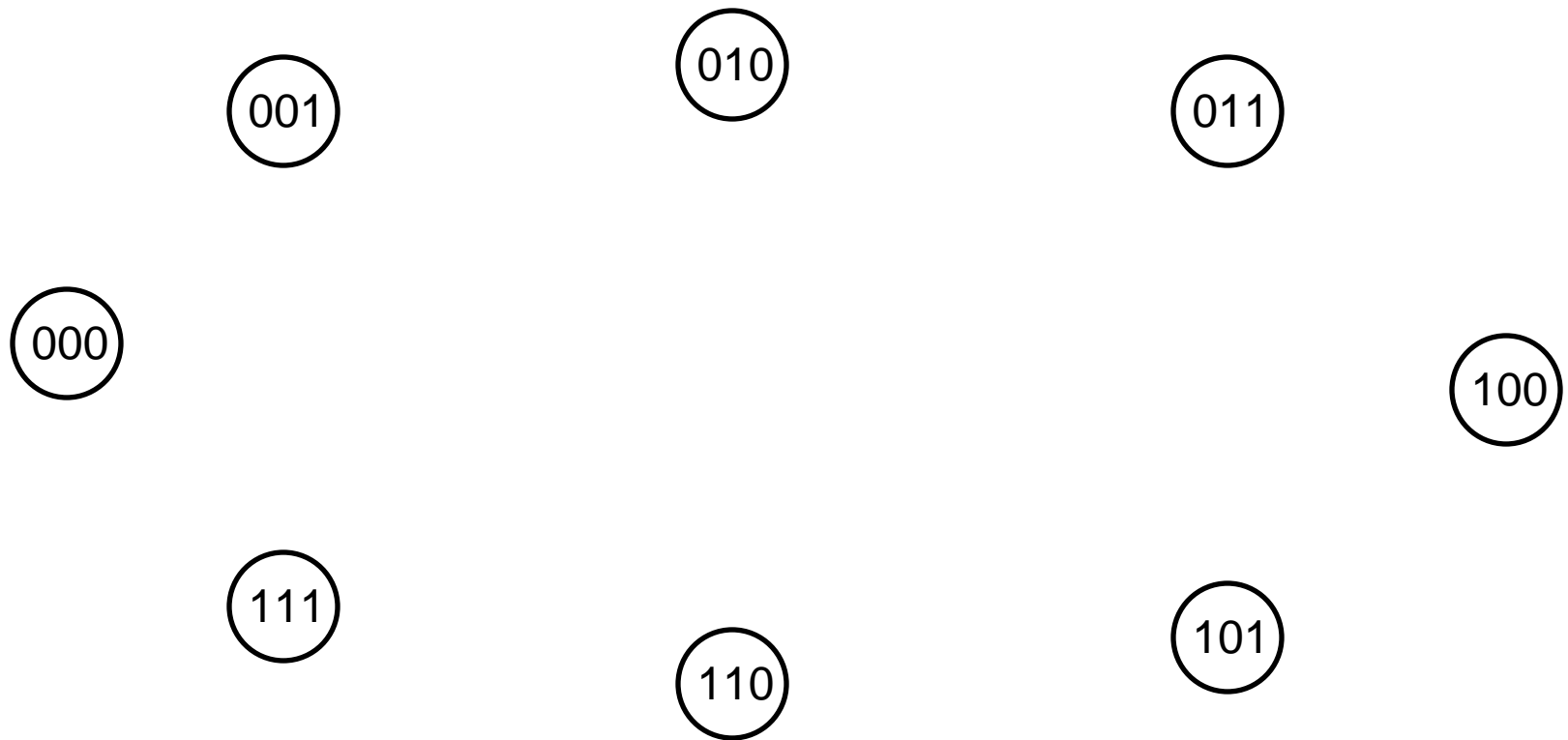
# Finite State Machines (FSMs)

An example: our synchronous counter

- Transition function:
  - On the clock event, transition to the next state in the sequence

# FSM Example: Synchronous Counter

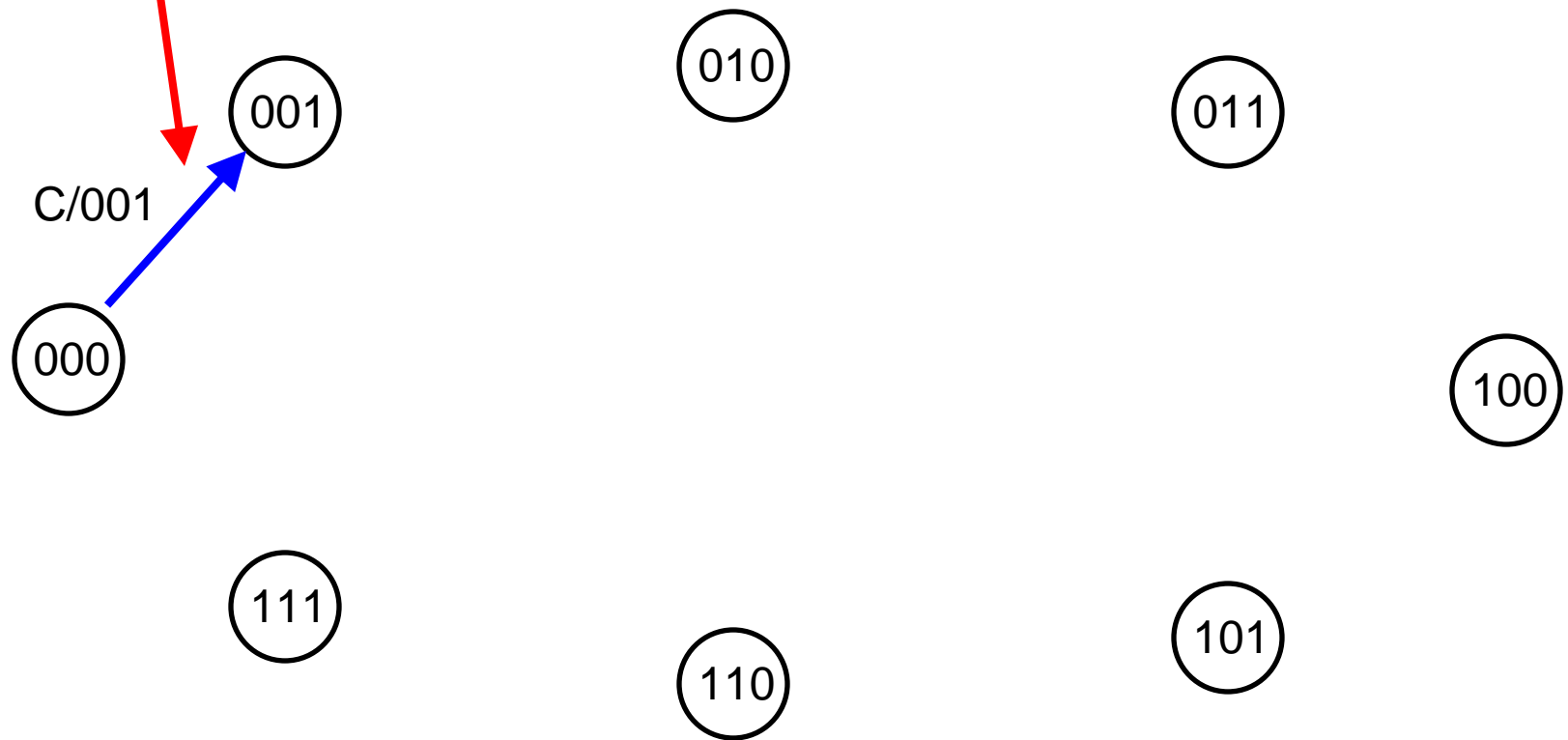
A Graphical Representation:



A set of states

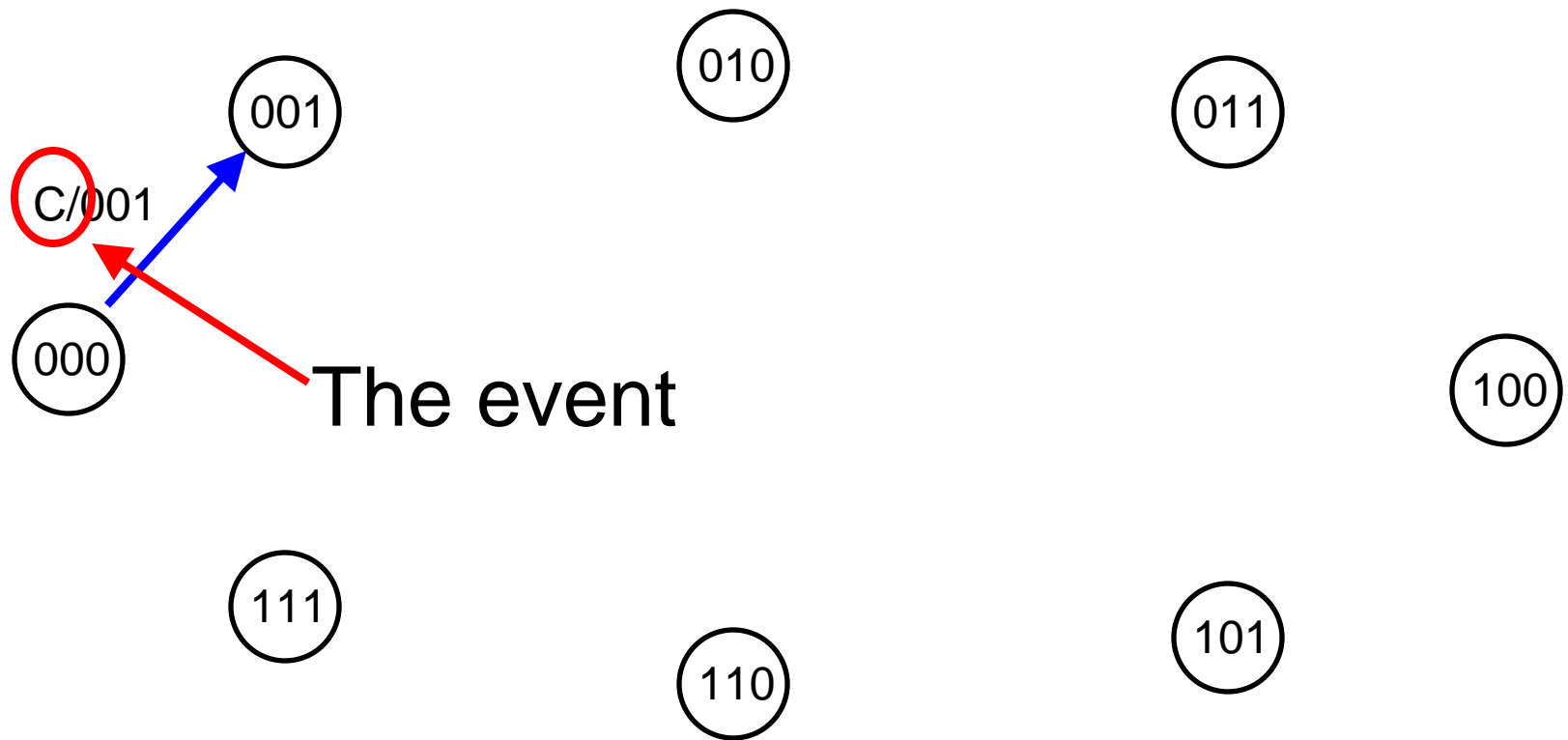
# FSM Example: Synchronous Counter

A transition



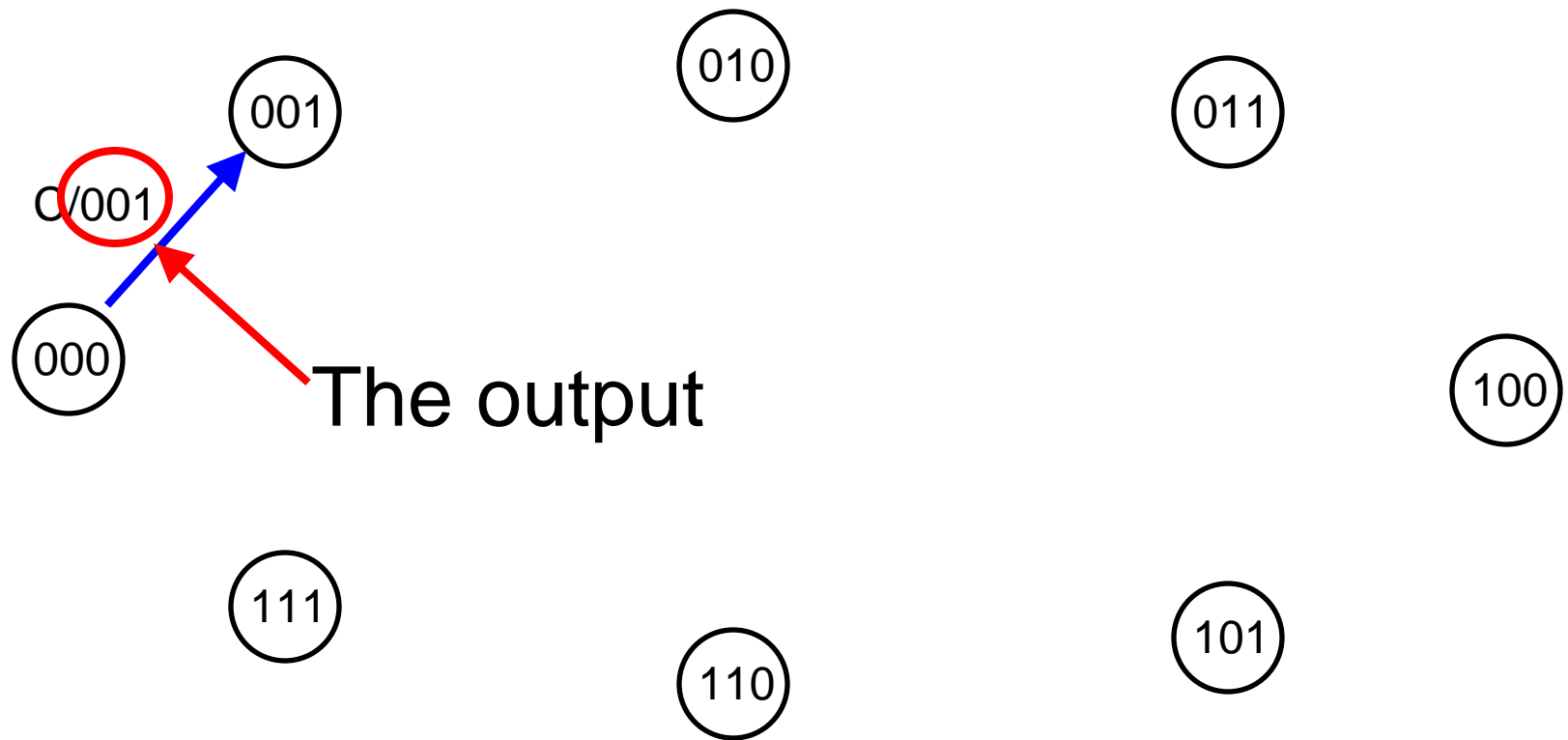
# FSM Example: Synchronous Counter

A transition



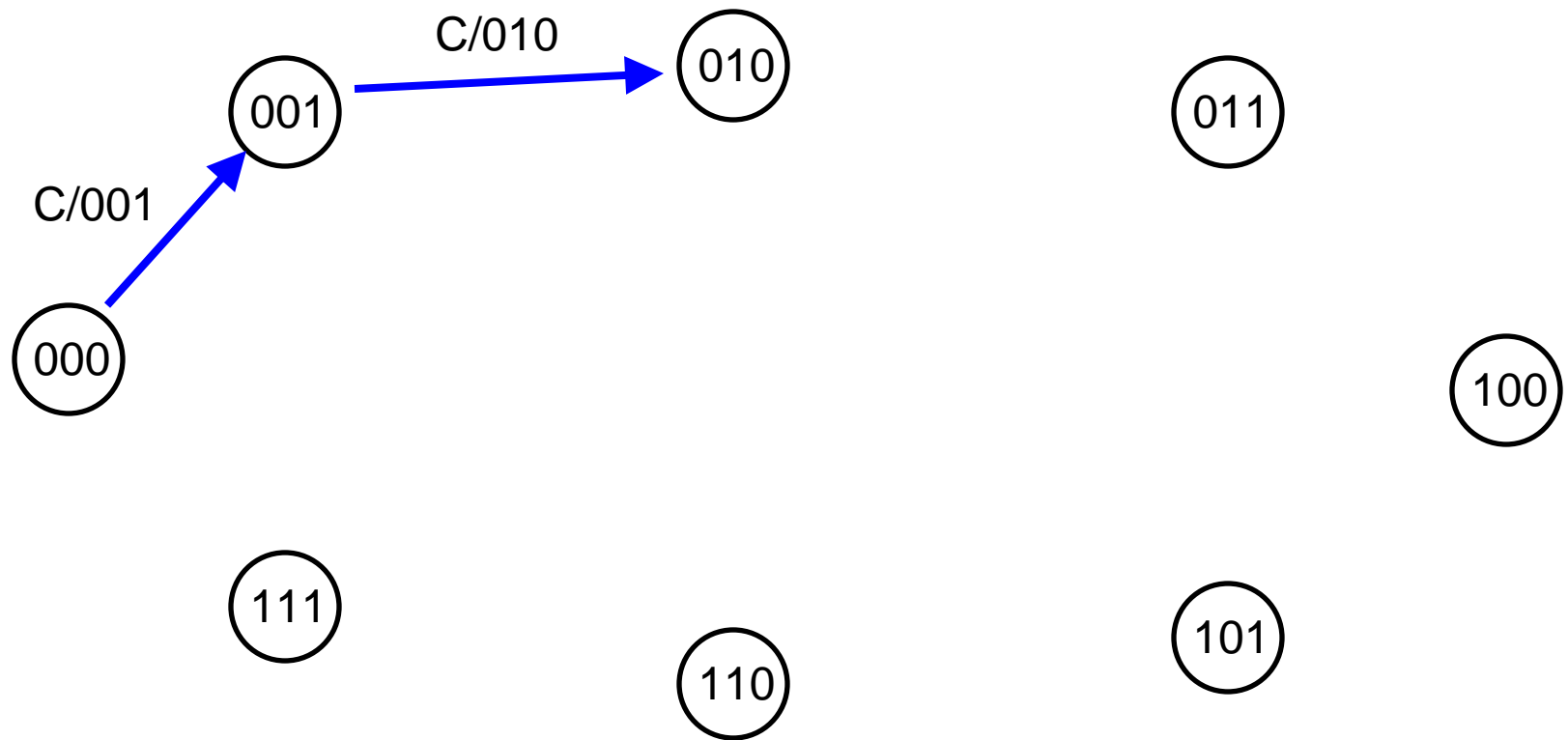
# FSM Example: Synchronous Counter

A transition



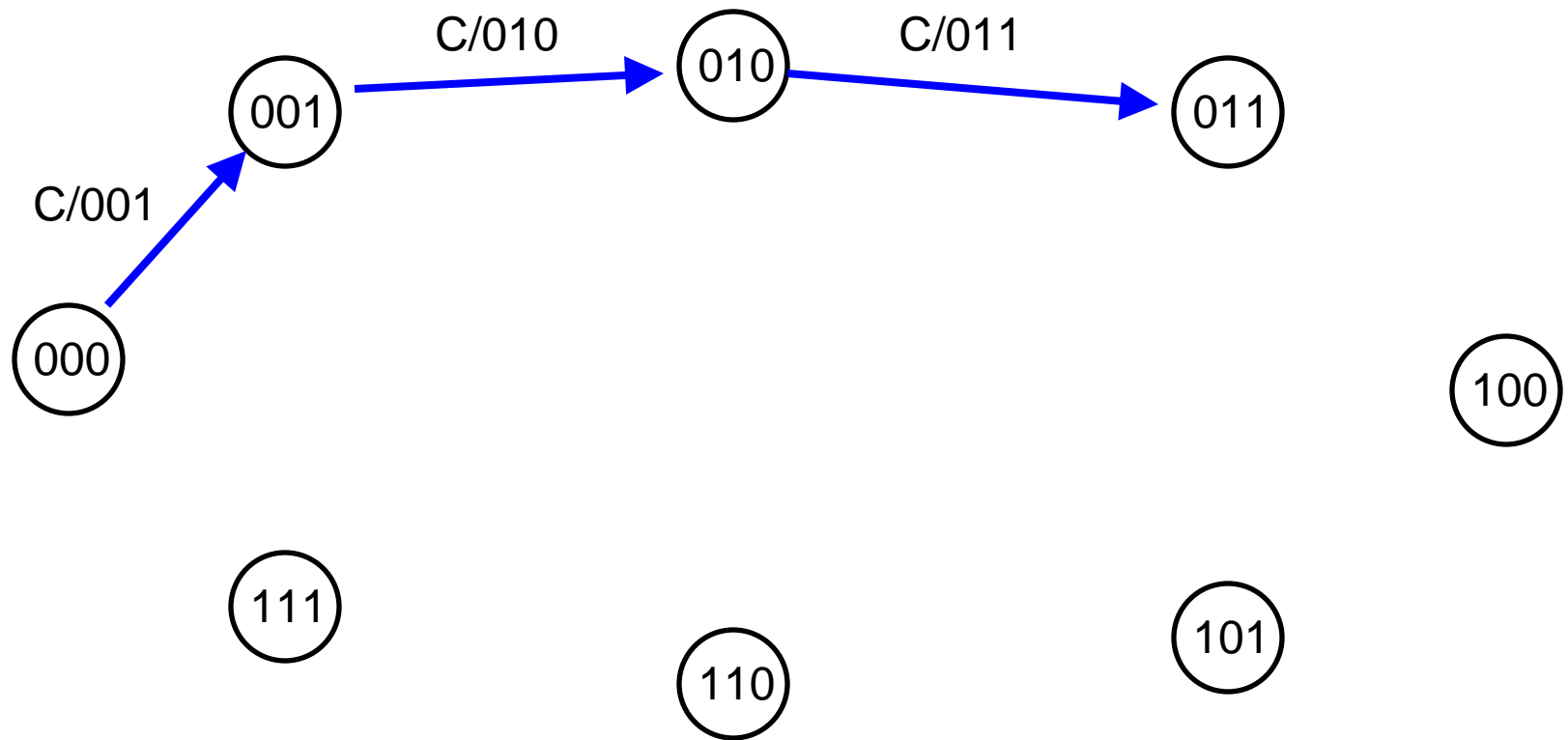
# FSM Example: Synchronous Counter

The next transition



# FSM Example: Synchronous Counter

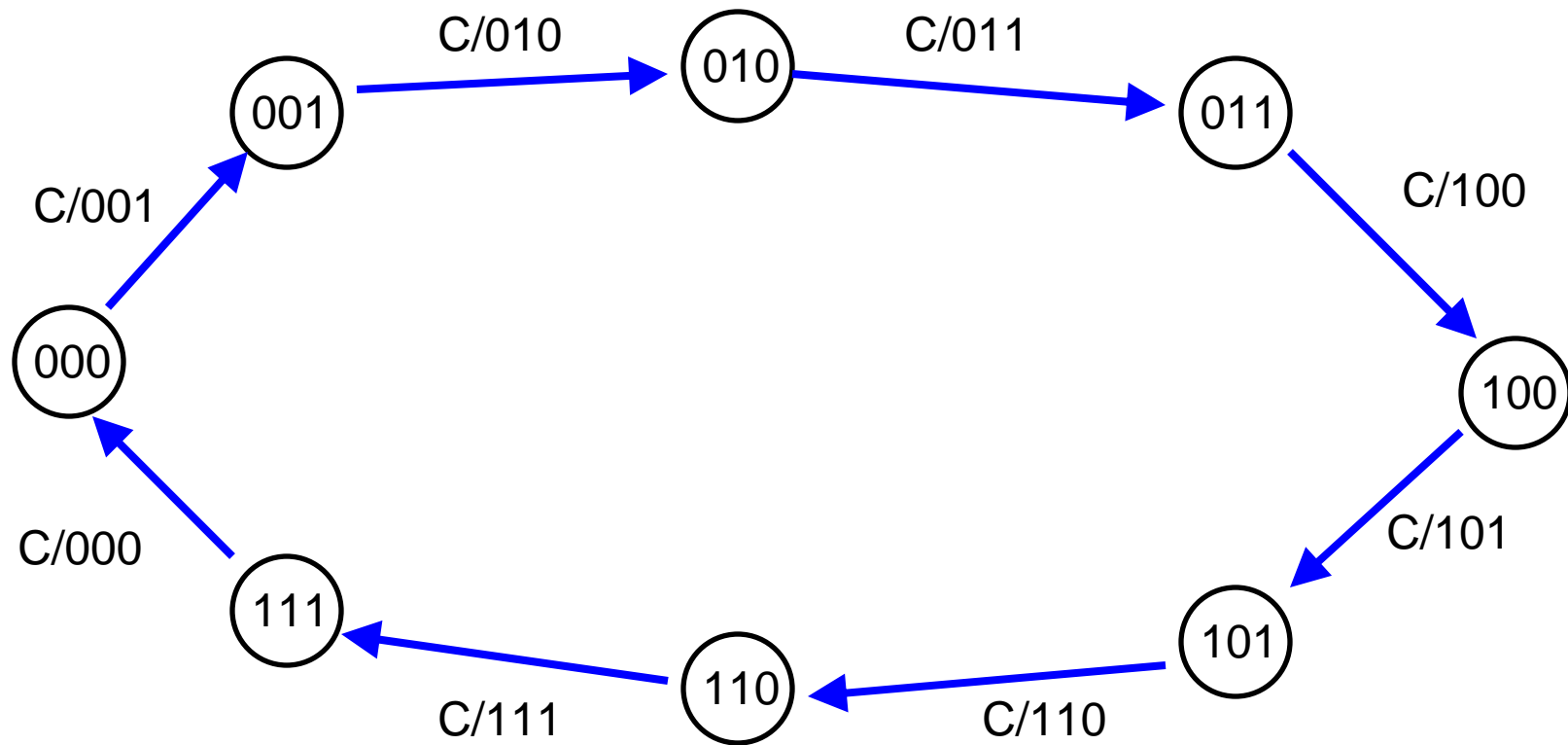
The next transition





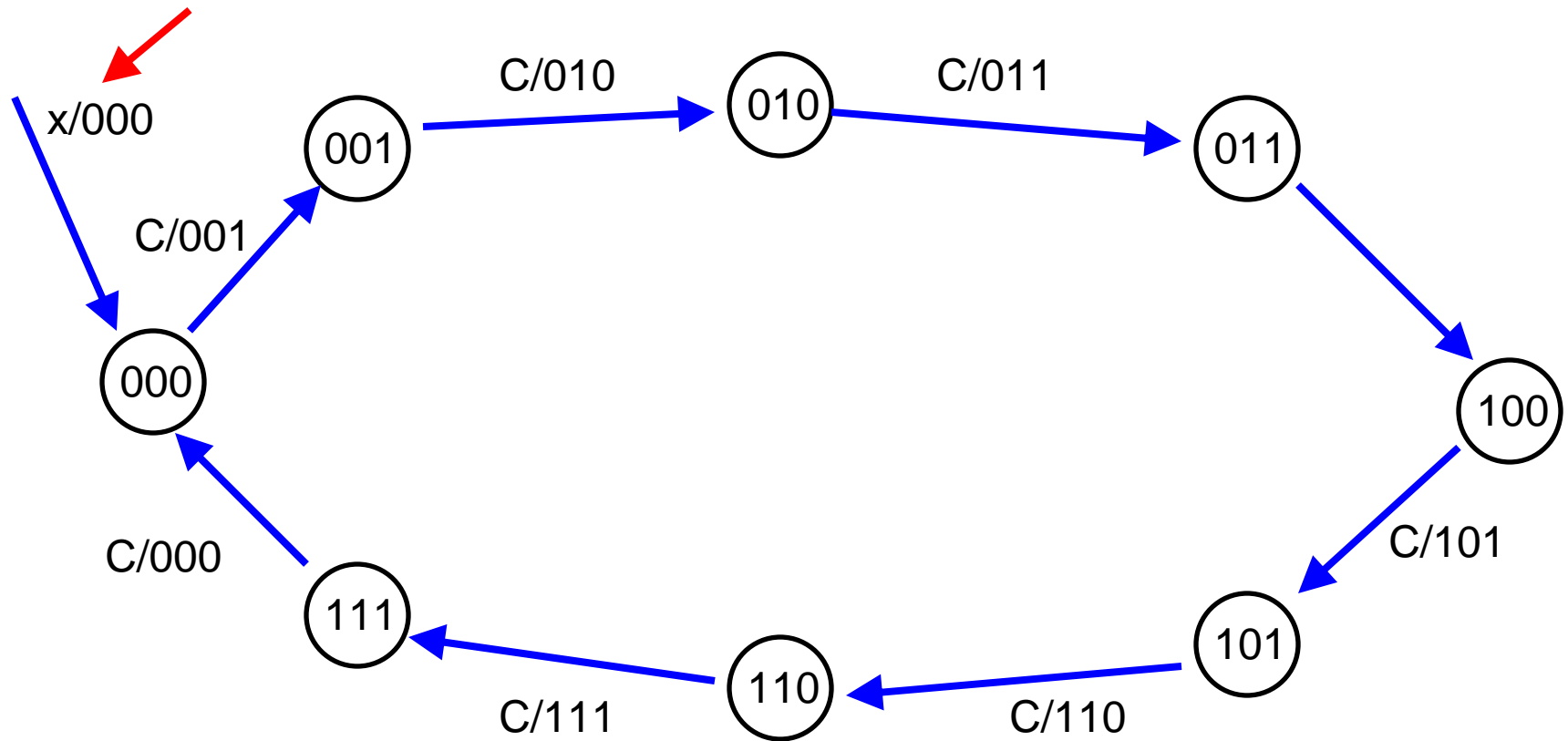
# FSM Example: Synchronous Counter

The full transition set



# FSM Example: Synchronous Counter

Initial condition



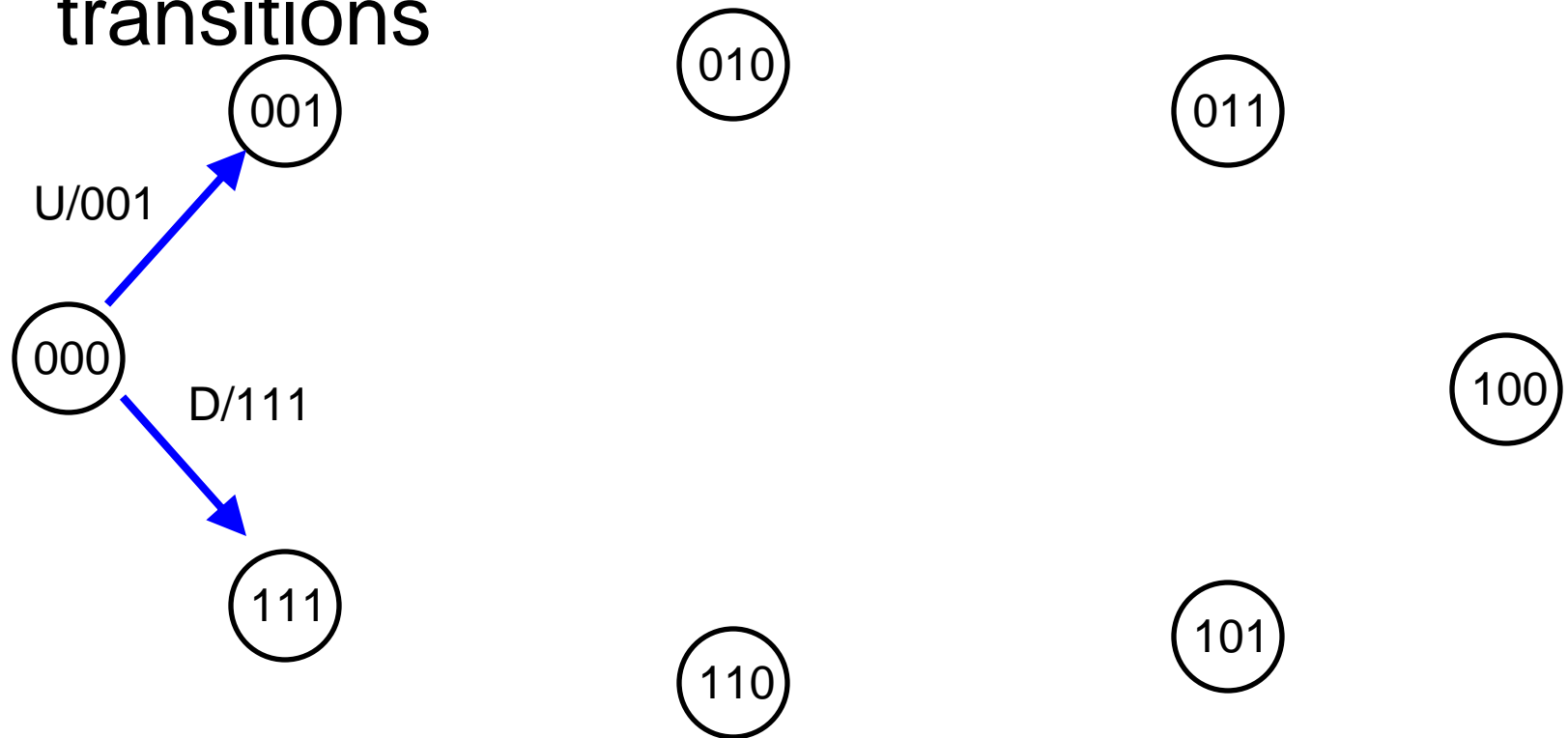
# Example II: An Up/Down Counter

Suppose we have two events (instead of one): Count up and count down

- How does this change our state transition diagram?

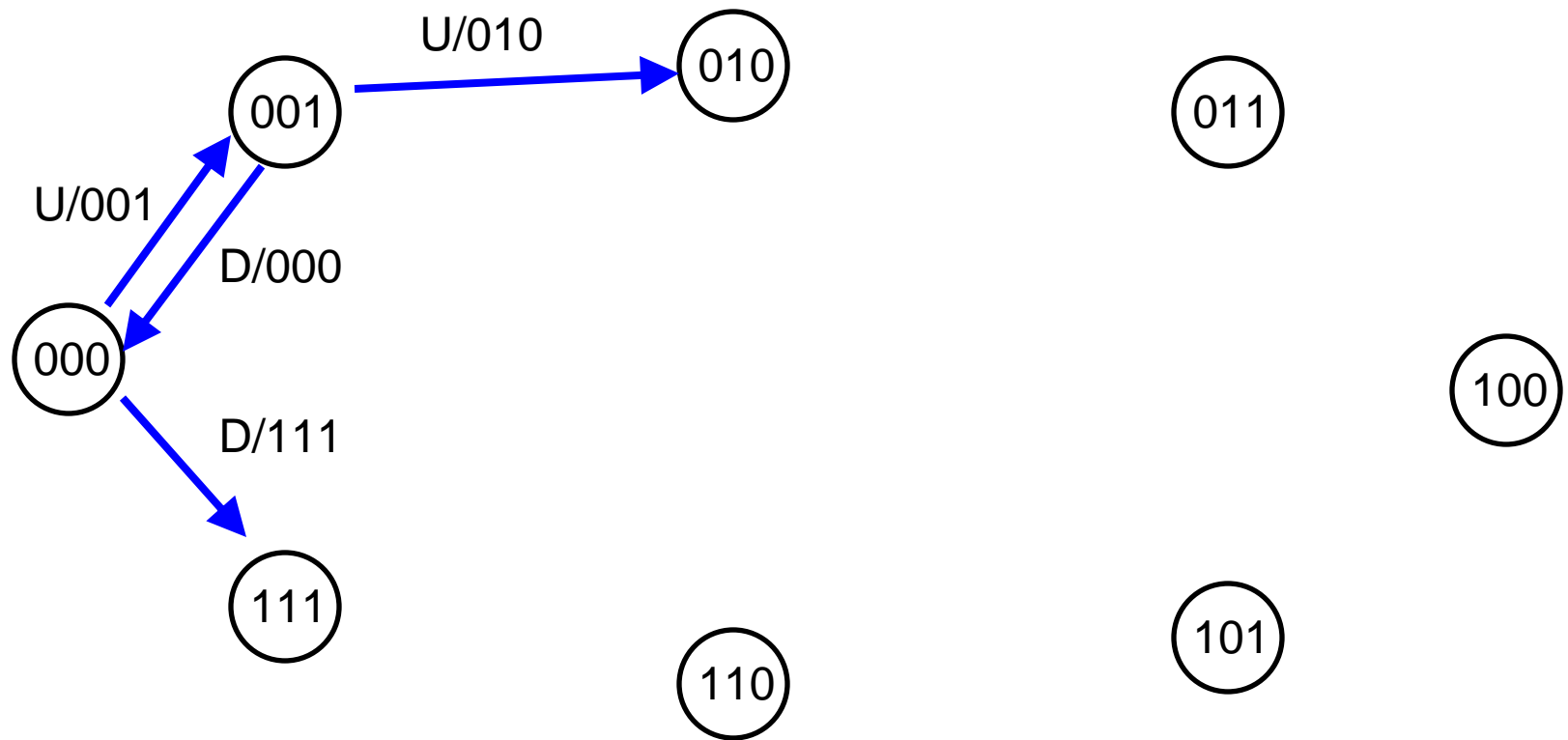
# Example II: An Up/Down Counter

From state 000, there are now two possible transitions



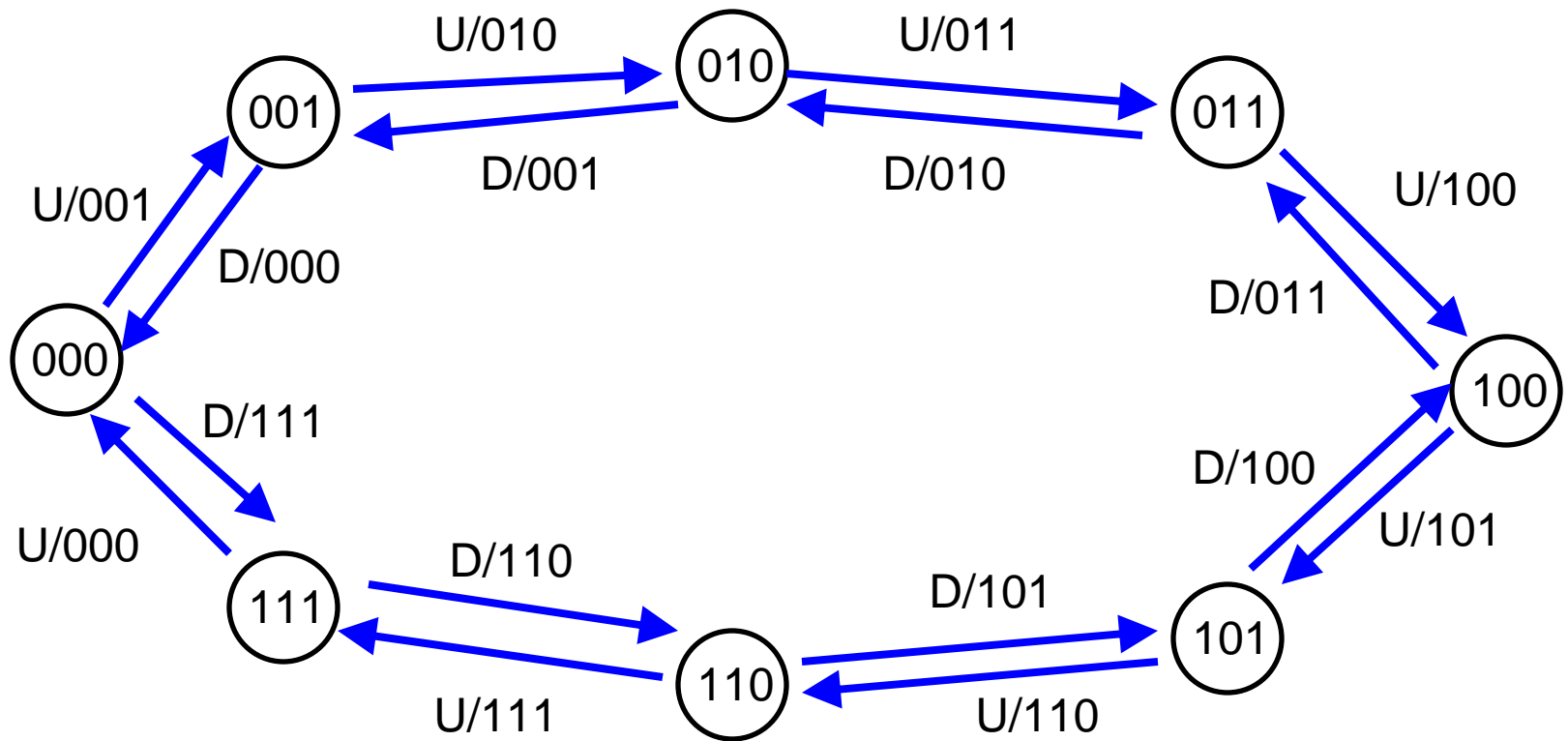
# Example II: An Up/Down Counter

Likewise for state 001...



# Example II: An Up/Down Counter

The full transition set



# FSMs and Control

How do we relate FSMs to Control?

- States are ?

# FSMs and Control

How do we relate FSMs to Control?

- States are our memory of recent inputs
- Inputs are ?



# FSMs and Control

How do we relate FSMs to Control?

- States are our memory of recent inputs
- Inputs are some processed representation of what the sensors are observing
- Outputs are ?

# FSMs and Control

How do we relate FSMs to Control?

- States are our memory of recent inputs
- Inputs are some processed representation of what the sensors are observing
- Outputs are the control actions

# FSMs: A Control Example

Suppose we have a vending machine:



- Accepts dimes and nickels
- Will dispense one of two things once \$.20 has been entered: Jolt or Buzz Water
  - The “user” requests one of these by pressing a button
- Ignores select if  $< \$.20$  has been entered
- Immediately returns any coins above \$.20



# Vending Machine FSM

What are the states?

# Vending Machine FSM

What are the states?

- \$0
- \$.05
- \$.10
- \$.15
- \$.20

# Vending Machine FSM

What are the inputs/events?

# Vending Machine FSM

What are the inputs/events?

- Input nickel (N)
- Input dime (D)
- Select Jolt (J)
- Select Buzz Water (BW)

# Vending Machine FSM

What are the outputs?



# Vending Machine FSM

What are the outputs?

- Return nickel (RN)
- Return dime (RD)
- Dispense Jolt (DJ)
- Dispense Buzz Water (DBW)
- Nothing (Z)



# Vending Machine Design

What is the initial state?

# Vending Machine Design

What is the initial state?

- $S = \$0$

# Vending Machine Design

What can happen from  
 $S = \$0$ ?

Event	Next State	Output

# Vending Machine Design

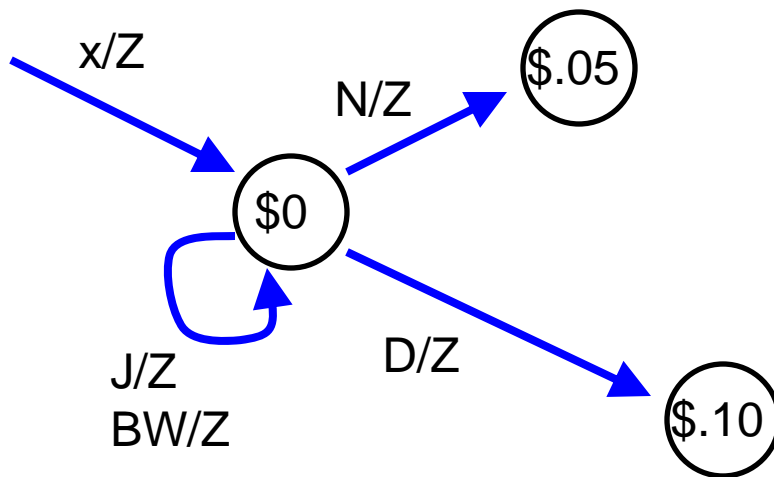
What can happen from  
 $S = \$0$ ?

What does this part of  
the diagram look like?

Event	Next State	Output
N	\$.05	Z
D	\$.10	Z
J	\$0	Z
BW	\$0	Z

# Vending Machine Design

A piece of the state diagram:



# Vending Machine Design

What can happen from  
 $S = \$0.05$ ?

Event	Next State	Output

# Vending Machine Design

What can happen from  
 $S = \$0.05$ ?

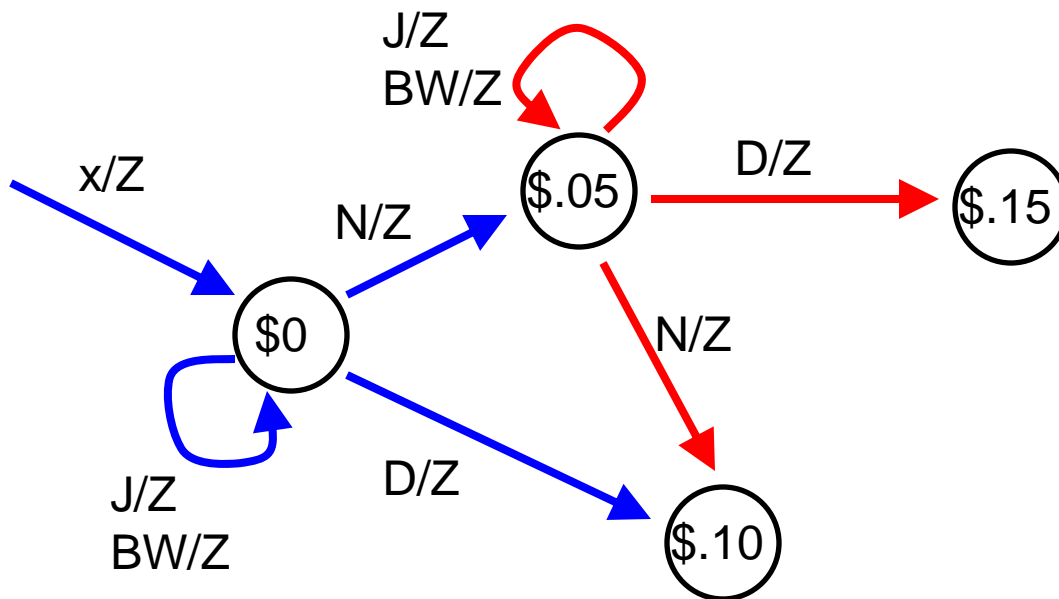
What does the modified  
diagram look like?

Event	Next State	Output
N	\$.10	Z
D	\$.15	Z
J	\$.05	Z
BW	\$.05	Z



# Vending Machine Design

A piece of the state diagram:



# Vending Machine Design

What can happen from  
 $S = \$0.10$ ?

Event	Next State	Output

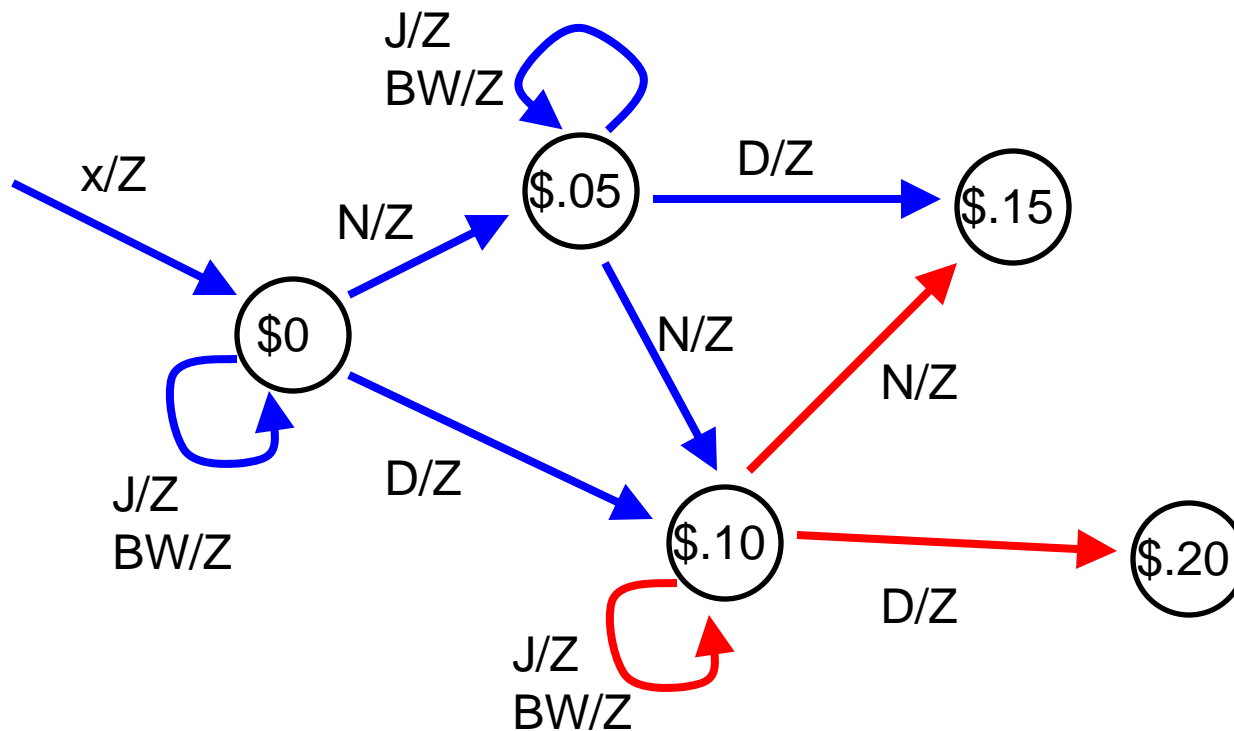
# Vending Machine Design

What can happen from  
 $S = \$0.10$ ?

Event	Next State	Output
N	\$.15	Z
D	\$.20	Z
J	\$.10	Z
BW	\$.10	Z

# Vending Machine Design

A piece of the state diagram:



# Vending Machine Design

What can happen from  
 $S = \$0.15$ ?

Event	Next State	Output

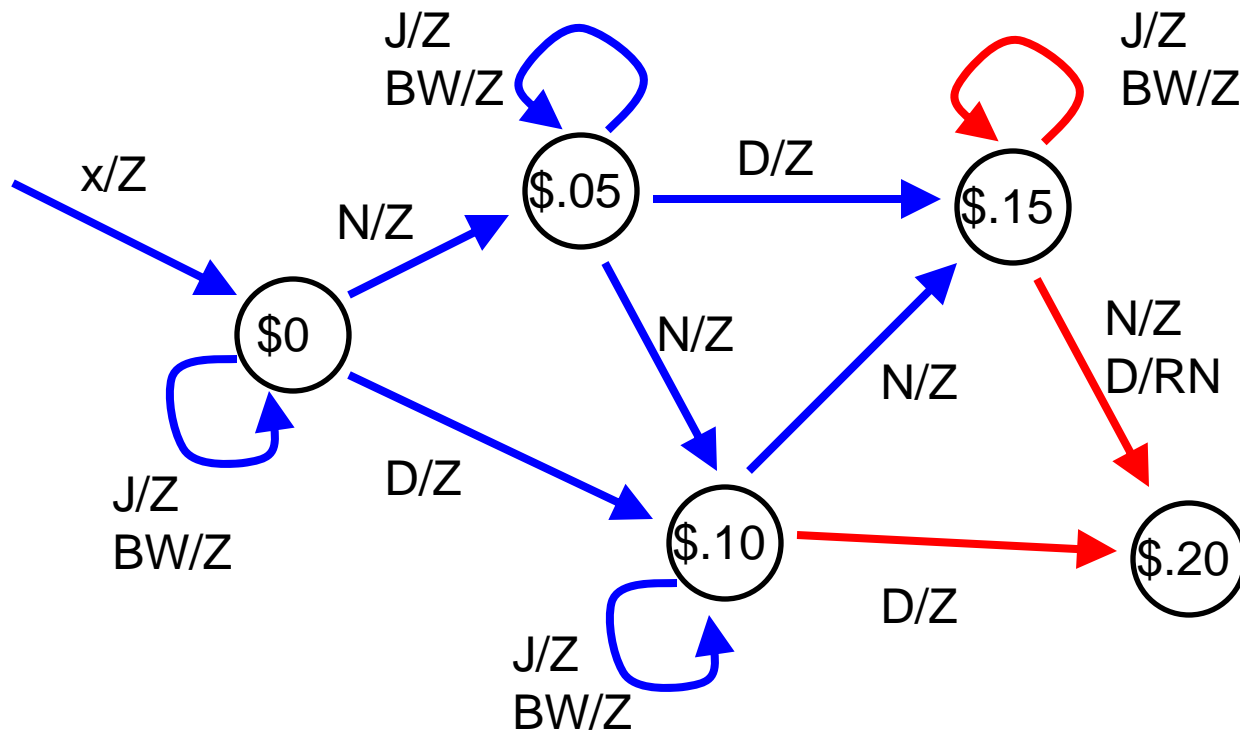
# Vending Machine Design

What can happen from  
 $S = \$0.15$ ?

Event	Next State	Output
N	\$.20	Z
D	\$.20	RN
J	\$.15	Z
BW	\$.15	Z

# Vending Machine Design

A piece of the state diagram:



# Vending Machine Design

Finally: what can happen from  $S = \$0.20$ ?

Event	Next State	Output



# Vending Machine Design

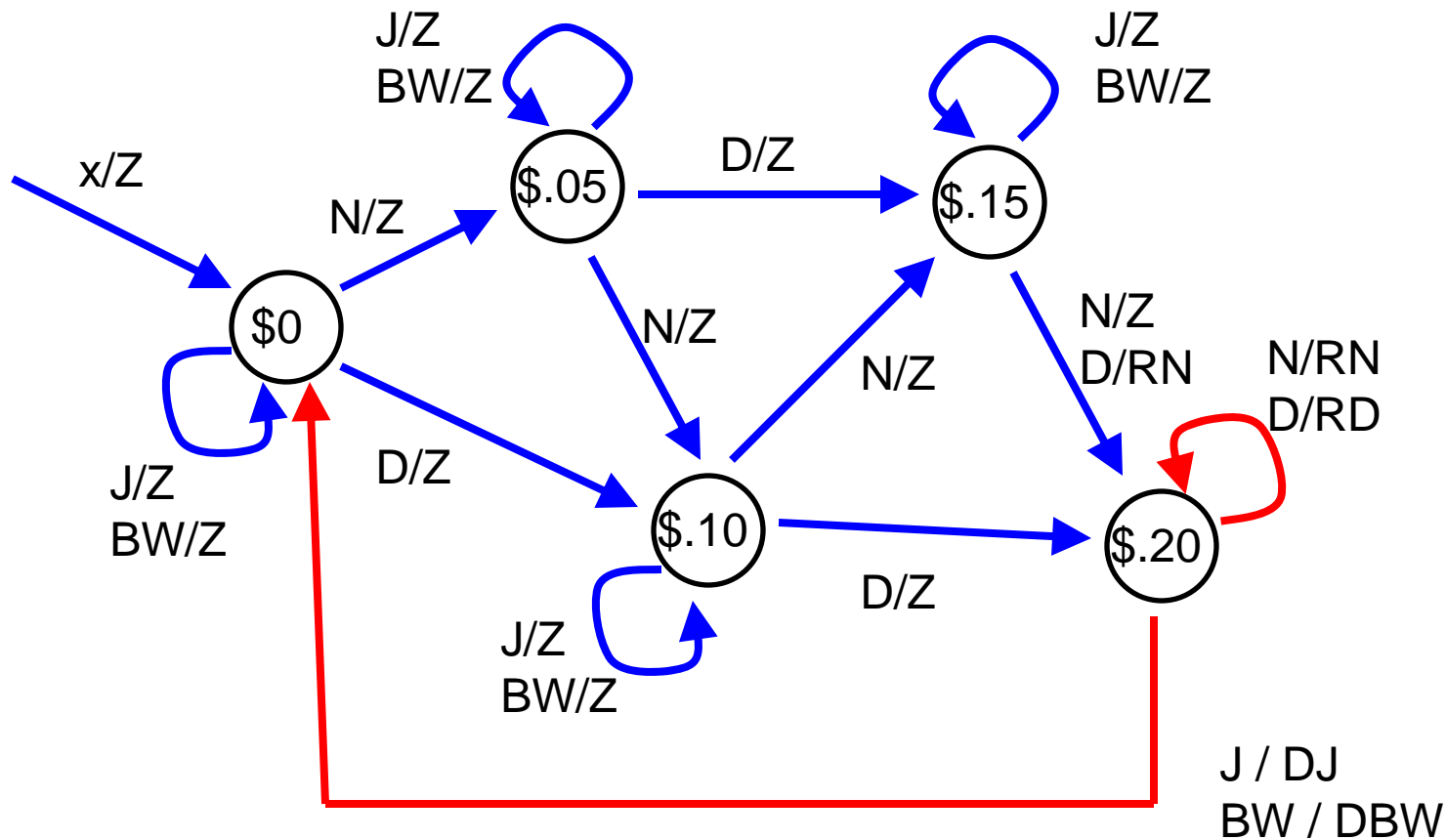
Finally, what can happen from  $S = \$0.20$ ?

Event	Next State	Output
N	\$.20	RN
D	\$.20	RD
J	\$0	DJ
BW	\$0	DBW



# Vending Machine Design

The complete state diagram:



# Project Group Exercise

Design a FSM for control of the sonar

- What are the states?
- What are the events?
- What are the actions?

# Project 4

## Sonar FSM hints:

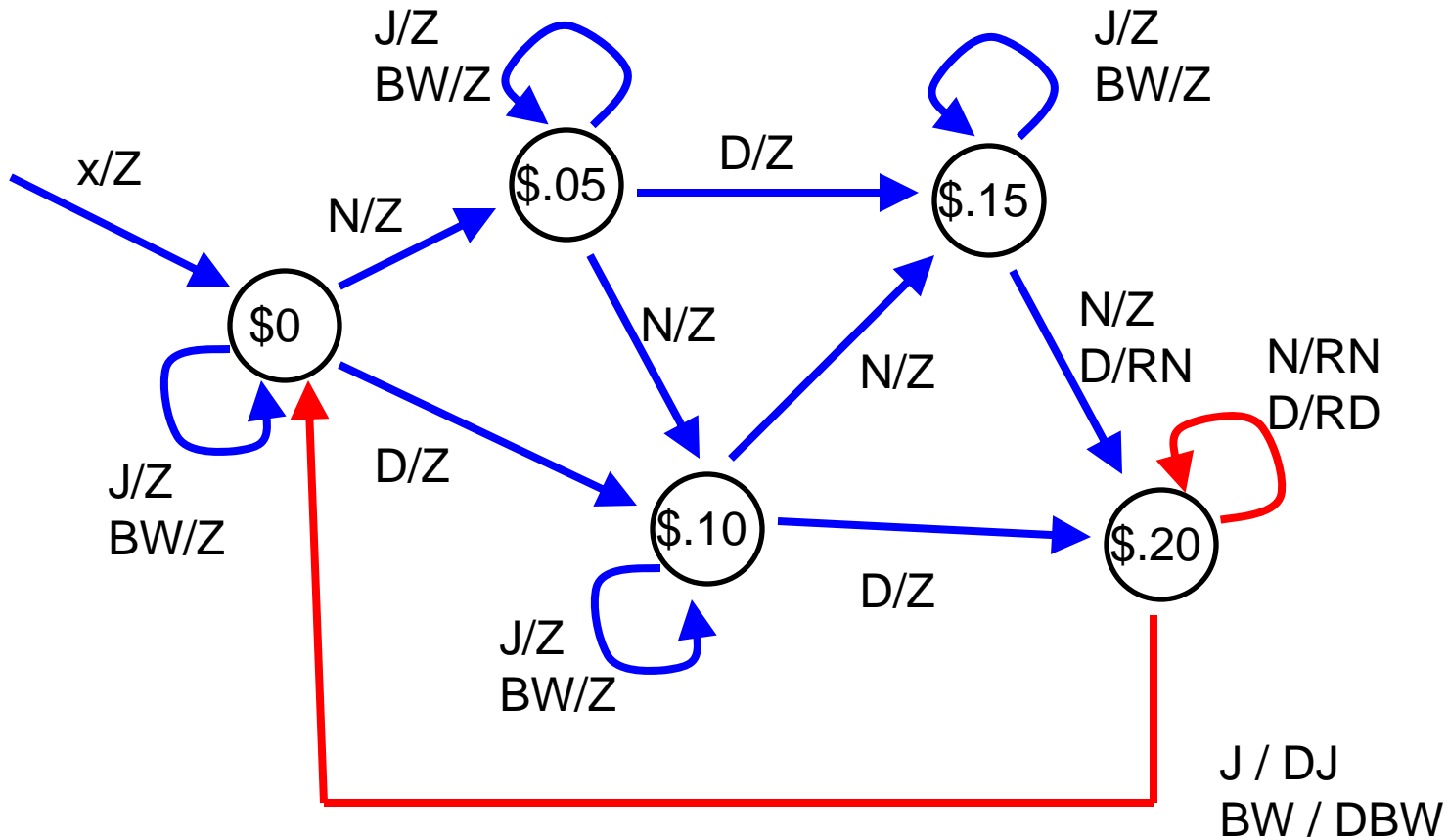
- Remember that the overflow ISR is called at regular intervals
- Each call to your ISR:
  - Depending on the current FSM state, you will:
    - Check the time on a clock
    - Check the input from the sonar
    - Generate an output to the sonar

# ISR Trap: Shared Data Problem





# Last Time



# Today

- Implementation of finite state machines in code

Homework 4 due next Tuesday

Project 4 due a week from Tuesday

Note: I am out of town next week (but accessible via email)



# FSMs and Control

How do we relate FSMs to Control?

- States are ?

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How do we relate FSMs to Control?

- States are our memory of recent inputs
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- Outputs are the control actions

# A Robot Control Example

Consider the following task:

- The robot is to move toward the first beacon that it “sees”
- The robot searches for a beacon in the following order: right, left, front

What is the FSM representation?

# Robot Control Example II

Consider the following task:

- The robot must lift off to some altitude
- Translate to some location
- Take pictures
- Return to base
- Land
- At any time: a detected failure should cause the craft to land

What is the FSM representation?

# FSMs As Controllers

- Need code that translates sensory inputs into FSM events
- An FSM output can require an arbitrary amount of time
  - We will often implement this control action as a separate function call
- Control actions will not necessarily be fixed (but could be a function of sensory input)

# FSMs As Controllers (cont)

- We might choose to leave some events out of the implementation
  - Only some events may be relevant to certain states
- When in a state, the FSM may also issue control actions (even when a new event has not arrived)
  - Again, this may be implemented as a function call



# FSMs in C

```
int state = 0;    // Initial state
while(1) {
    <do some processing of the sensory inputs>
    switch(state) {
        case 0:
            <handle state 0>
            break;
        case 1:
            <handle state 1>
            break;
        case 2: ...
    }
}
```

# FSMs in C

```
int state = 0; // Initial state
while(1) {
    <do some processing of the sensory inputs>
    switch(state) {
        case 0:
            <handle state 0>
            break;
        case 1:
            <handle state 1>
            break;
        case 2: ...
    }
}
```

**Variable  
declaration and  
initialization**

# FSMs in C

```
int state = 0;    // Initial state
while(1) {
    <do some processing of the sensory inputs>
    switch(state) {
        case 0:
            <handle state 0>
            break;
        case 1:
            <handle state 1>
            break;
        case 2: ...
    }
}
```

**Loop forever**

# FSMs in C

```
int state = 0;    // Initial state
while(1) {
  <do some processing of the sensory inputs>
  switch(state) {
    case 0:
      <handle state 0>
      break;
    case 1:
      <handle state 1>
      break;
    case 2: ...
  }
}
```

“pseudo code”:  
not really code,  
but indicates what  
is to be done

# FSMs in C

```
int state = 0;    // Initial state
while(1) {
  <do some processing of the sensory inputs>
  switch(state) {
    case 0:
      <handle state 0>
      break;
    case 1:
      <handle state 1>
      break;
    case 2: ...
  }
}
```

In this case: we will translate the current sensory inputs into a representation of an event (if one has happened)

# FSMs in C

```
int state = 0;    // Initial state
while(1) {
    <do some processing of the sensory inputs>
    switch(state) {
        case 0:
            <handle state 0>
            break;
        case 1:
            <handle state 1>
            break;
        case 2: ...
    }
}
```

Switch/case syntax allows us to cleanly perform many “if(x==y)” operations

# FSMs in C

```
int state = 0;    // Initial state
while(1) {
    <do some processing of the sensory inputs>
    switch(state) {
        case 0:
            <handle state 0>
            break;
        case 1:
            <handle state 1>
            break;
        case 2: ...
    }
}
```

If state==0, then execute the following code

# FSMs in C

```
int state = 0;    // Initial state
while(1) {
    <do some processing of the sensory inputs>
    switch(state) {
        case 0:
            <handle state 0>
            break;
        case 1:
            <handle state 1>
            break;
        case 2: ...
    }
}
```

This code can be as complex as necessary



# FSMs in C

```
int state = 0;    // Initial state
while(1) {
    <do some processing of the sensory inputs>
    switch(state) {
        case 0:
            <handle state 0>
            break;
        case 1:
            <handle state 1>
            break;
        case 2: ...
    }
}
```

**break** says to exit the switch (don't forget it or strange things can happen!)

# FSMs in C

```
int state = 0;    // Initial state
while(1) {
    <do some processing of the sensory inputs>
    switch(state) {
        case 0:
            <handle state 0>
            break;
        case 1:
            <handle state 1>
            break;
        case 2: ...
    }
}
```

If state==1, then ...

# FSMs in C

```
int state = 0;    // Initial state
while(1) {
    <do some processing of the sensory inputs>
    switch(state) {
        case 0:
            <handle state 0>
            break;
        case 1:
            <handle state 1>
            break;
        case 2: ...
    }
}
```

End of the **switch**  
block



# FSMs in C (some other possibilities)

```
int state = 0;    // Initial state
while(1) {
    <do some processing of the sensory inputs>
    switch(state) {
        case 0:
            <handle state 0>
            break;
        :
    default:
        <handle default case>
        break;
    }
    <do some low-level control>
}
```

# FSMs in C (some other possibilities)

```
int state = 0;    // Initial state
while(1) {
    <do some processing of the sensory inputs>
    switch(state) {
        case 0:
            <handle state 0>
            break;
        :
        default:
            <handle default case>
            break;
    }
    <do some low-level control>
}
```

Matches any state  
(if we reach this  
point)

# FSMs in C (some other possibilities)

```
int state = 0;    // Initial state
while(1) {
    <do some processing of the sensory inputs>
    switch(state) {
        case 0:
            <handle state 0>
            break;
        :
        default:
            <handle default case>
            break;
    }
    <do some low-level control>
}
```

(possibly) alter  
some control  
outputs (e.g.,  
steering direction)

# Handling Each State

- You will need to provide code that handles the event processing for each state
- Specifically:
  - You need to handle each event that can occur
  - For each event, you must specify:
    - What action is to be taken
    - What the next state is

# Handling Each State

In our vending machine example:

- Events are easy to describe (only a few things can happen)
- It is convenient in this case to also “switch” on the event



# FSMs in C: Processing for Individual States

```
case STATE_10cents:
    // $.10 has already been deposited
    switch(event) {
        case EVENT_NICKEL:    // Nickel
            state = STATE_15cents; // Transition to $.15
            break;
        case EVENT_DIME:      // Dime
            state = STATE_20cents; // Transition to $.2
            break;
        case EVENT_JOLT:     // Select Jolt
        case EVENT_BUZZ:     // Select Buzzwater
            display_NOT_ENOUGH();
            break;

        case EVENT_NONE:    // No event
            break;          // Do nothing

    };
break;
```

# FSMs in C: Processing for Individual States

```
case STATE_10cents:
    // $.10 has already been deposited
    switch(event) {
        case EVENT_NICKEL:    // Nickel
            state = STATE_15cents; // Transition to $.15
            break;
        case EVENT_DIME:     // Dime
            state = STATE_20cents; // Transition to $.2
            break;
        case EVENT_JOLT:    // Select Jolt
        case EVENT_BUZZ:    // Select Buzzwater
            display_NOT_ENOUGH();
            break;

        case EVENT_NONE:    // No event
            break;          // Do nothing
    };
break;
```

Another integer

# FSMs in C: Processing for Individual States

```
case STATE_10cents:
    // $.10 has already been deposited
    switch(event) {
        case EVENT_NICKEL:    // Nickel
            state = STATE_15cents; // Transition to $.15
            break;
        case EVENT_DIME:     // Dime
            state = STATE_20cents; // Transition to $.2
            break;
        case EVENT_JOLT:    // Select Jolt
        case EVENT_BUZZ:    // Select Buzzwater
            display_NOT_ENOUGH();
            break;

        case EVENT_NONE:    // No event
            break;          // Do nothing

    };
break;
```

A nickel has  
been received

# FSMs in C: Processing for Individual States

```
case STATE_10cents:
    // $.10 has already been deposited
    switch(event) {
        case EVENT_NICKEL:    // Nickel
            state = STATE_15cents; // Transition to $.15
            break;
        case EVENT_DIME:     // Dime
            state = STATE_20cents; // Transition to $.2
            break;
        case EVENT_JOLT:    // Select Jolt
        case EVENT_BUZZ:    // Select Buzzwater
            display_NOT_ENOUGH();
            break;
        case EVENT_NONE:    // No event
            break;          // Do nothing
    };
break;
```

Change state for next iteration of the while() loop

# FSMs in C: Processing for Individual States

```
case STATE_10cents:
    // $.10 has already been deposited
    switch(event) {
        case EVENT_NICKEL:    // Nickel
            state = STATE_15cents; // Transition to $.15
            break;
        case EVENT_DIME:      // Dime
            state = STATE_20cents; // Transition to $.2
            break;
        case EVENT_JOLT:      // Select Jolt
        case EVENT_BUZZ:      // Select Buzzwater
            display_NOT_ENOUGH();
            break;
        case EVENT_NONE:     // No event
            break;           // Do nothing
    };
break;
```

If any of these match, then execute the following code (which does nothing in this example)

# Handling Each State

Some events do not fall neatly into one of several categories

- This precludes the use of the “switch” construct
- For example: an event that occurs when our heli reaches a goal orientation or a goal height
- For these continuous situations, we typically use an “if” construct:

```
if(heading_error < 20 && heading_error > -20){...}
```

# A Note on “Style” in C

- The numbers that we assigned to the different states are arbitrary (and at first glance, hard to interpret)
- Instead, we can define constant strings that have some meaning
- Replace: 0, 1, 2, 3, 4, 5
- With: STATE\_00, STATE\_05, STATE\_10, STATE\_15, STATE\_20

# A Note on “Style” in C

In C, this is done by adding some definitions to the beginning of your program (either in the .c file or the .h file):

```
#define STATE_00cents    0
#define STATE_05cents    1
#define STATE_10cents    2
#define STATE_15cents    3
#define STATE_20cents    4
```



# Shared Data Problem

Necessary conditions (in our context):

- Both the main program and an ISR share global variables
- The variable(s) is larger than one byte

The problem:

- The main program starts to access a variable & is then interrupted by the ISR
- The ISR changes the variable
- The main program “sees” a corrupted value

# Shared Data Problem

The solution (in the main program):

- Disable the interrupts
  - E.g., `timer0_disable()`
- Access the shared variables
- Enable the interrupts
  - E.g., `timer0_enable()`

Note: do not leave interrupts disabled for very long (no loops or waits!)

# Tasks for Today

- FSM for sonar control and processing
  - FSM modifications for the “mission”
- (note that these are two different FSMs!)

# Project Group Exercise

Design a FSM for control of the sonar

- What are the states?
- What are the events?
- What are the actions?

# Project 4

## Sonar FSM hints:

- Remember that the overflow ISR is called at regular intervals
- Each call to your ISR:
  - Depending on the current FSM state, you will:
    - Check the time on a clock
    - Check the input from the sonar
    - Generate an output to the sonar
- No need for the `while(1){}` loop!