

# Recurrent Neural Networks, Attention and Transformers

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# Spatial / Temporal Data

Feature vector as a function of space and/or time

- Channels in a 1D/2D/3D image
- Features across time
- Combination of both

# Spatial and/or Temporal Data

- Often apply the same computational operators across each of the feature vectors
- “Neighboring” feature vectors are also informative as to how we should interpret the current feature vector

# Parts of a Convolutional Neural Network

- **Convolutional operators:** search for specific patterns within the spatial or temporal neighborhood
- **Max pooling operators:** does there exist a feature \*somewhere\* within the pool?
- **Striding** (often coupled with pooling): decrease the spatial or temporal resolution

# The Plan (next few lectures)

- 1D data & Recurrent Neural Networks
  - Compact approach for integrating information across long sequences
- Example: Sentence-to-sentence translation
- Attention: tool for focusing on specific pieces of information across the sequences
- Transformers (attention<sup>2</sup>)
- Transformers with 2D data

# Recurrent Neural Networks

Processing feature vectors in time and/or: producing some output in time

- Sequential steps for a robot control signal
- Processing textual input
- Producing textual output

Each time step: use the same network to get to the next time step

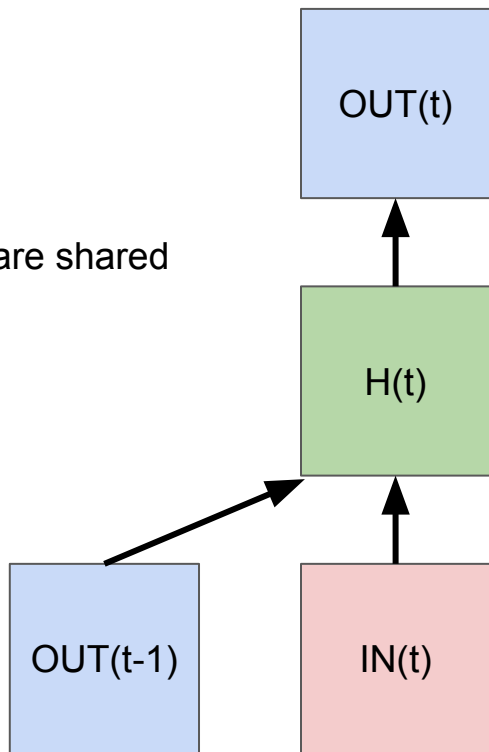
# Recurrent Neural Networks

- Jordan (1997): output at time  $t$  is an input to the network at time  $t+1$
- Elman (1990): hidden layer state at time  $t$  is an input to the network at time  $t+1$

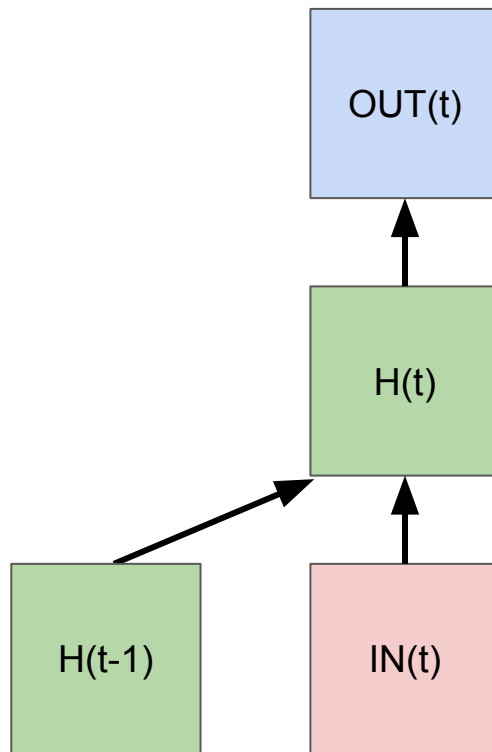
Either way: the extra input acts as a context for producing the next output

# Recurrent Neural Networks

Jordan



Elman



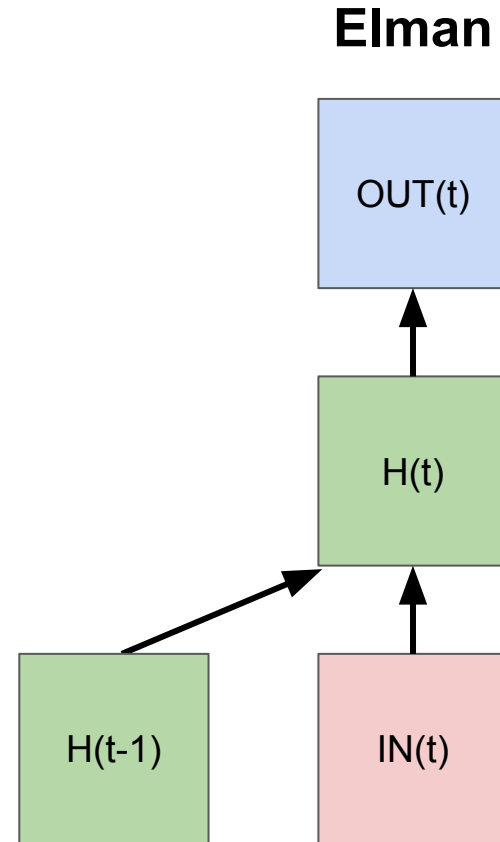
Parameters are shared  
across time



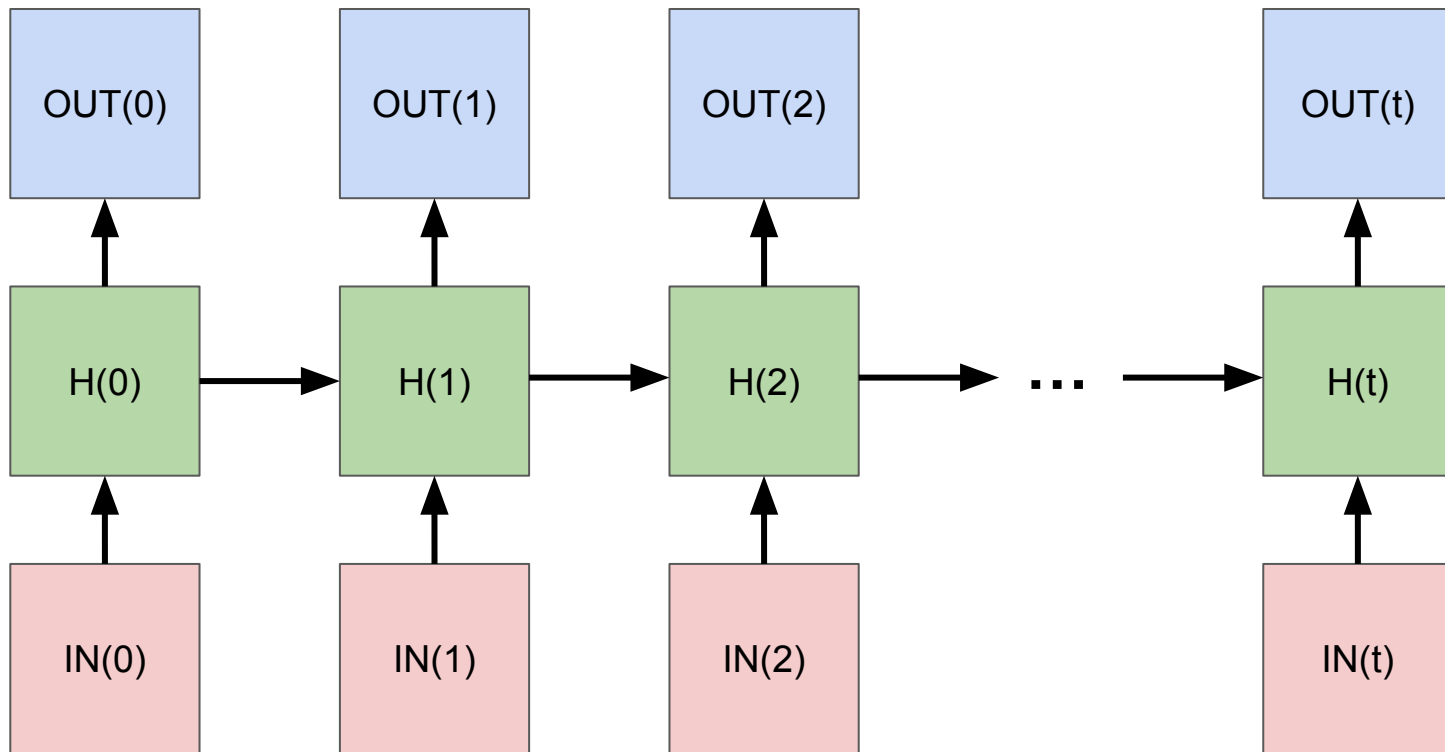
# Backpropagation Through Time

- Jordan and Elman: error gradient only flowed through the network for one time step
  - Still had to supply input/output pairs for each time step
  - Could only hope that the extra input provided sufficient information
- Werbos (1988): Backpropagation through time: error gradients flow across time

# Recurrent Neural Networks



# Unrolling the Recurrent Network



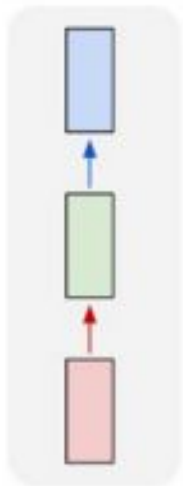
# Unrolling the Recurrent Network

- Parameters are shared at each time step
- Error gradients can pass across time
- Hidden state can carry key information across many time steps. Often referred to as **latent state**

Note: there are key similarities with 1D Convolution

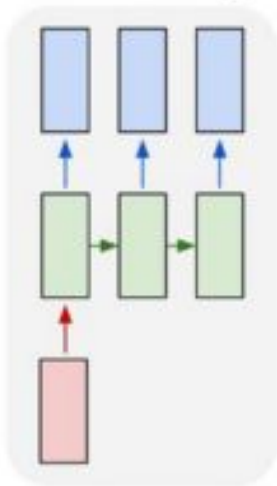
# Variety of RNN Architectures

one to one

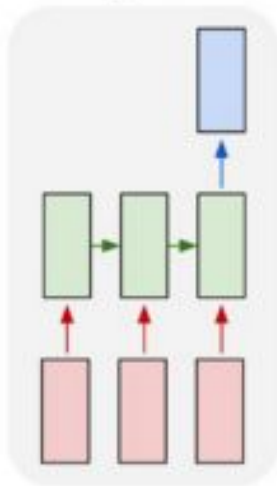


typical neural  
network

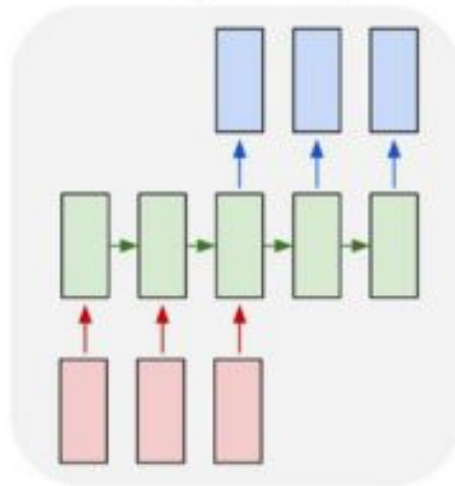
one to many



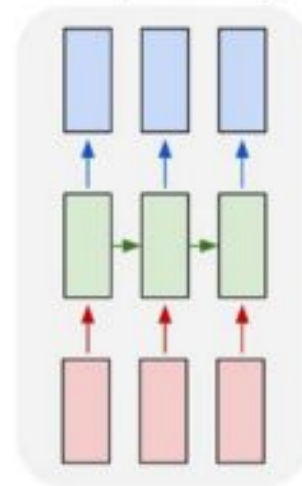
many to one



many to many



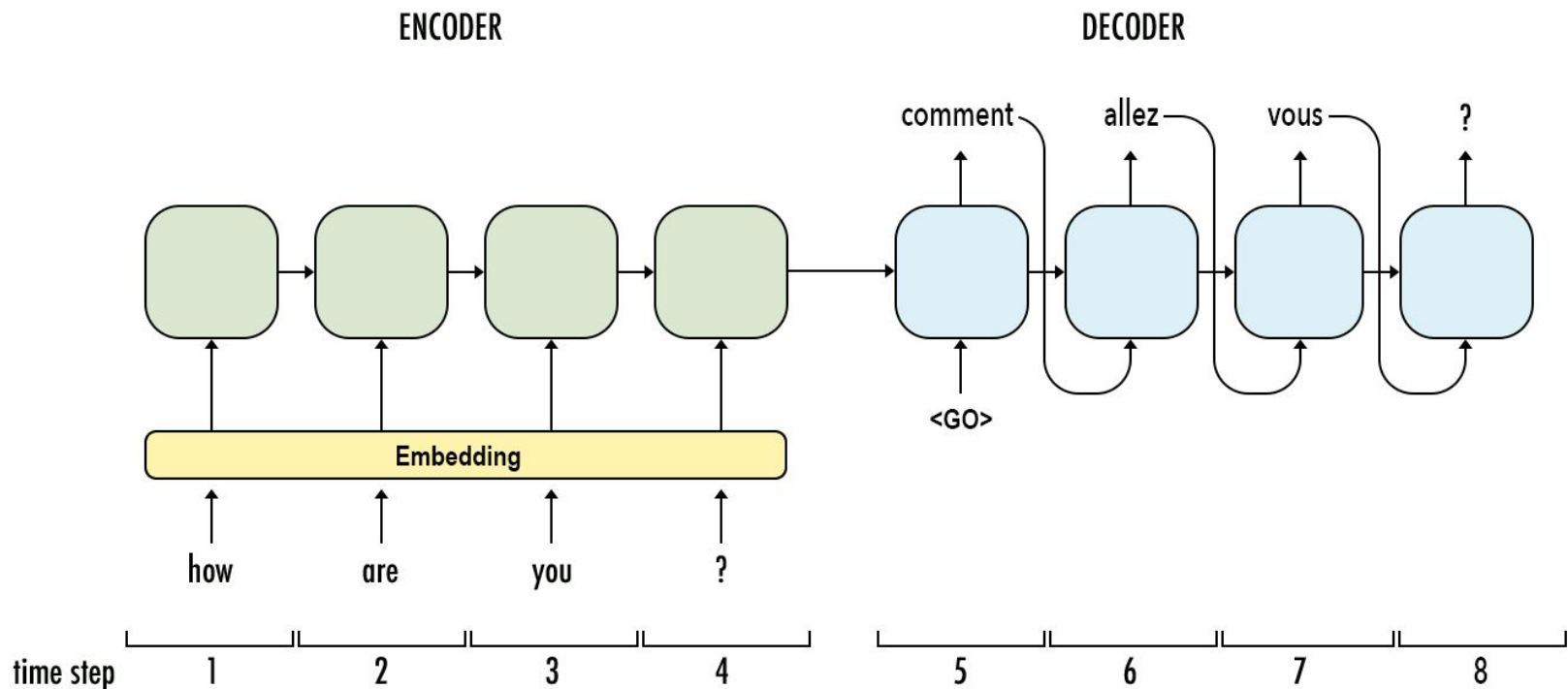
many to many



Recurrent Neural Networks

Image from: Andrej Karpathy

# Use in Machine Translation



# Use in Machine Translation

What is the output of the decoder?

# Use in Machine Translation

What is the output of the decoder?

- Translation is not a one-to-one mapping
- Need to capture the set of possible translations to French
- One possibility: probability distribution over all possible valid translations



# Use in Machine Translation

What is the output of the decoder?

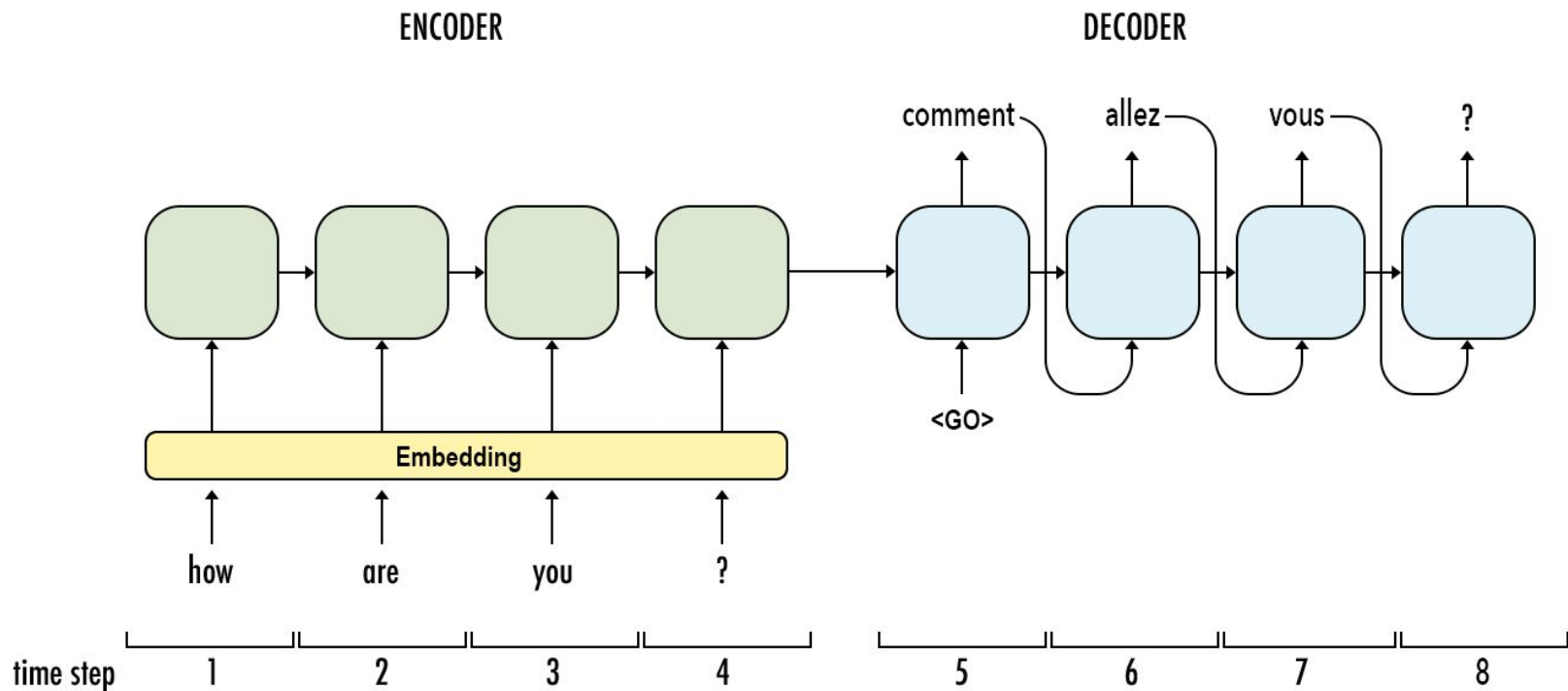
- One possibility: probability distribution over all possible valid translations
- Potentially a very complicated pdf
  - Can't really enumerate all possible word sequences
- Then, how do we capture it?

# Use in Machine Translation

What is the output of the decoder?

- Then, how do we capture it?
- Decode 1 word at a time!

# Use in Machine Translation



# Use in Machine Translation

Decoding:

- Given query, compute pdf over all possible next words
- Sample from this pdf
- Include the chosen word in the query
- Repeat until decoded word is a STOP marker

# Challenges

- Hidden state may need to carry critical information from the first token in the input to the final token in the output sequence
- Learning these representations requires propagating error information through all of these hidden state layers
- Can be many steps, especially when we are translating one paragraph at a time
- Vanishing error gradient can prevent a network from learning a mapping from input to output in feasible time

# Vanishing Gradient

Many solutions to the vanishing gradient problem:

- Ioffe & Szegedy (2015): Batch normalization
- Hochreiter & Schmidhuber (1997): Long/short-term memories (LSTM)
- Cho et al. (2014): Gated Recurrent Unit (GRU)

# Gated Recurrent Units (GRUs)

- Goal: structure our network so that \*some\* gradient can flow through each time step
- Approach:
  - Output from one step is a mix of the output from the last step and some new computation



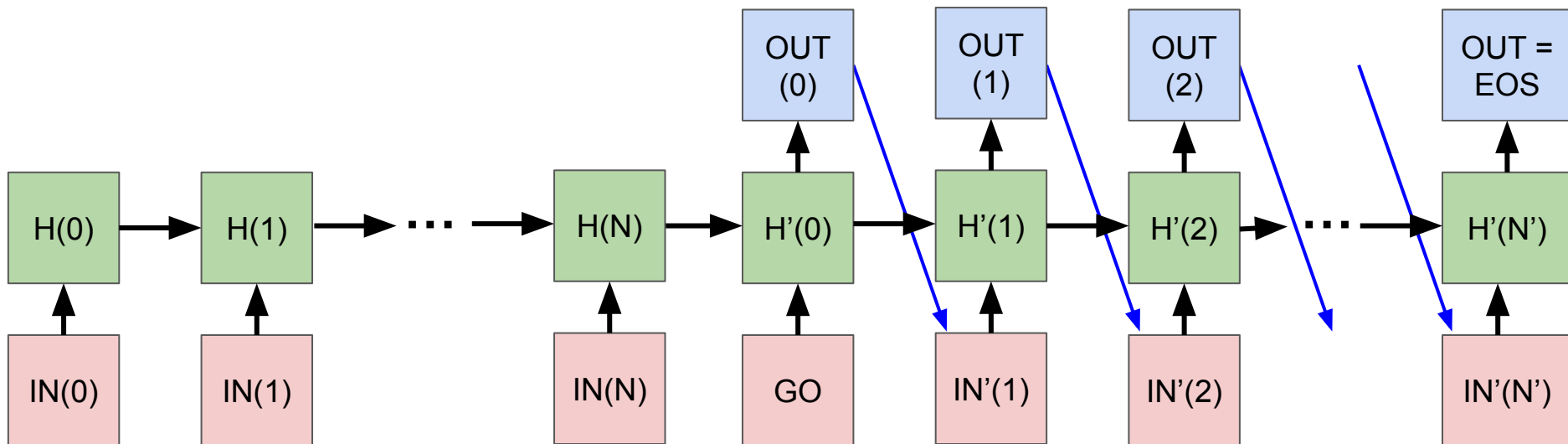


# An Alternative Approach

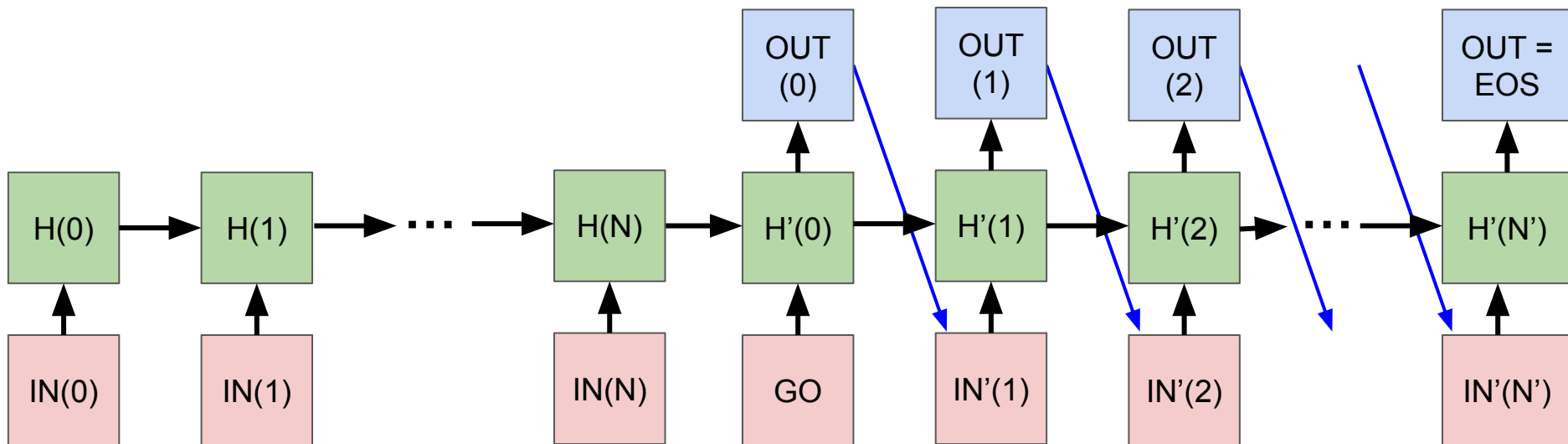
Key insight:

- To decide which token to generate at time  $t$ , we don't need the context of the entire input sentence (or paragraph)
- Really only need to know a handful of the input words & their spatial relationship to the current word
- **Attention**: blend the representations of only the tokens of interest & use the result to decide on the current output token

# RNN for Machine Translation



# RNN for Machine Translation



Insight: to compute  $Out(k)$ , may only need to pay attention to a small subset of the  $H$ 's

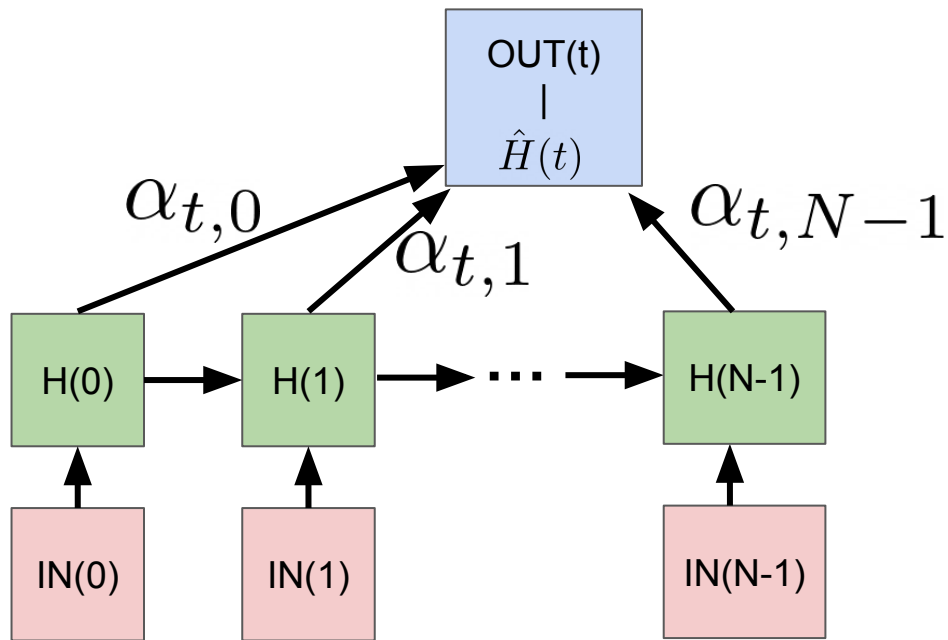
# Attention for Machine Translation

N time steps. Each time step t has:

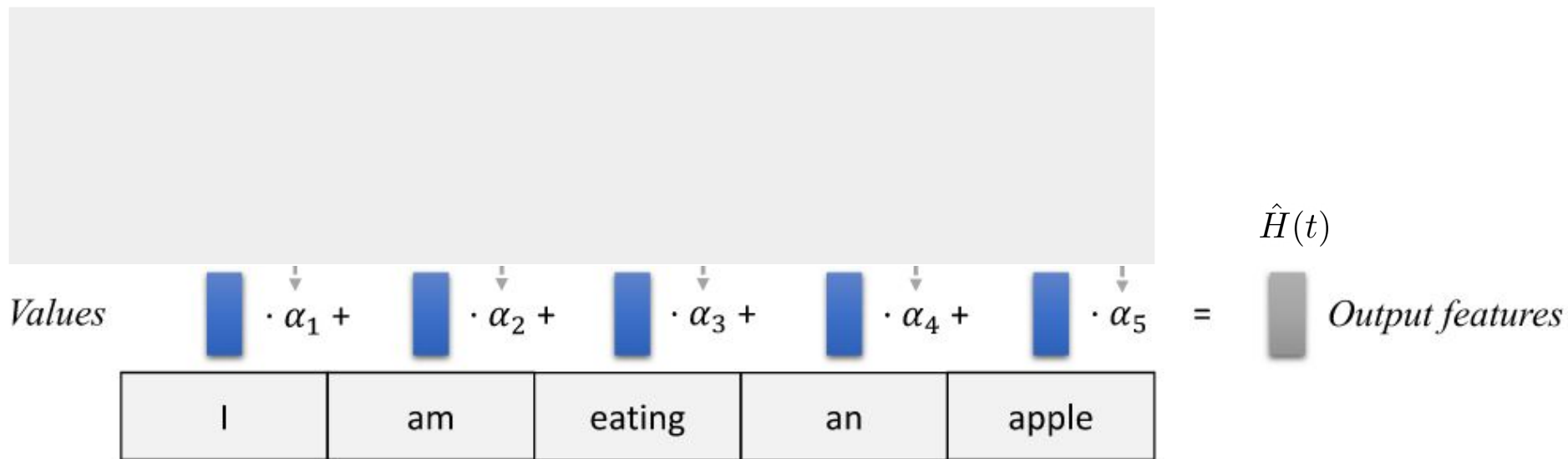
- Set of alphas that sum to 1
- A blended version of all N latent states

$$\sum_{i=0}^{N-1} \alpha_{t,i} = 1$$

$$\hat{H}(t) = \sum_{i=0}^{N-1} \alpha_{t,i} H(i)$$



# Attention for Machine Translation



# Attention for Machine Translation

$\alpha_{t,i}$  is the degree that  $H(i)$  plays in  $\hat{H}(t)$

- By selecting a small number of non-zero  $\alpha_{t,i}$ 's, the output generator can choose to focus on a small number of  $H(i)$ 's
- This means that many of the  $H(i)$ 's are ignored while generating the output for time  $t$ 
  - ... and these ignored  $H(i)$ 's do not propagate error gradients

The FBI is chasing a criminal on the run .

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# Content-Addressable Memories

- Memory is composed of a set of key/value pairs
  - $\mathbf{k}$  and  $\mathbf{v}$  are row vectors
- A query is compared to the set of keys
  - Hard version: the value for the one matching key is “returned”
  - Soft version: a blend of the best matching keys is “returned”



# Content-Addressable Memories

- Degree of match between a query (**q**) and a single key (**k**):

$$s = q \cdot k^T = \|q\| \|k\| \cos(\theta_{q \rightarrow k})$$


- Degree match between a query (**q**) and a set of keys (**K**)

$$S = q \cdot K^T$$


This gives us a row vector of scores


# Content-Addressable Memories

- Row vector of scores:  $S = q K^T$
- Use softmax to translate scores into alphas:

$$\alpha = \text{softmax}(q K^T)$$


$$\alpha_i = e^{s_i} / \sum_{j=0}^{N-1} e^{s_j}$$

- Blend in each value according to its corresponding alpha:

$$\hat{v} = \text{softmax}(q K^T) V = \sum_{i=0}^{N-1} \alpha_i V_i$$


# Content-Addressable Memories

- Blend in each value according to its corresponding alpha:

$$\hat{v} = \text{softmax}(q \ K^T) \ V = \sum_{i=0}^{N-1} \alpha_i \ V_i$$


- Can also parallelize for a set of queries:

$$\hat{V} = \text{softmax}(Q \ K^T) \ V$$

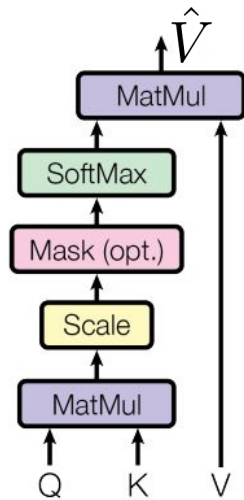

Note: comparing all N keys against all N queries

# Implementing Attention

## Scaled Dot-Product Attention: DL Implementation

- All inputs are matrices of the same size (N x #features)
  - Q: Queries
  - K: Keys
  - V: Values
- Output is also N x #features

Scaled Dot-Product Attention



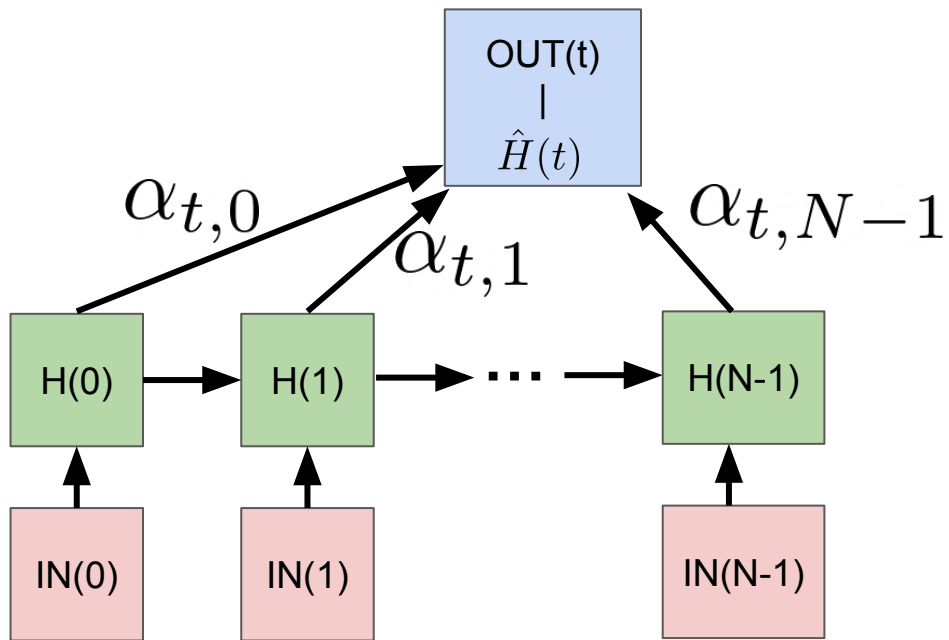
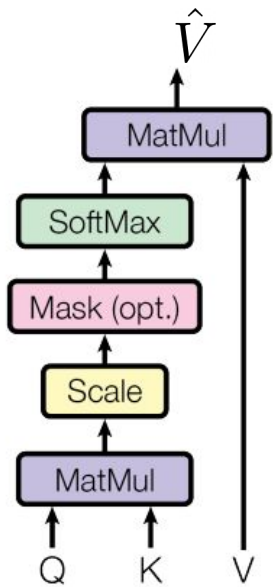
Vaswani et al. (2017)

$$\hat{V} = \text{Attention}(Q, K, V) = \text{softmax}\left(\frac{QK^T}{\sqrt{d_k}}\right)V$$

# Mapping Attention to our RNN

Many options, one possibility:

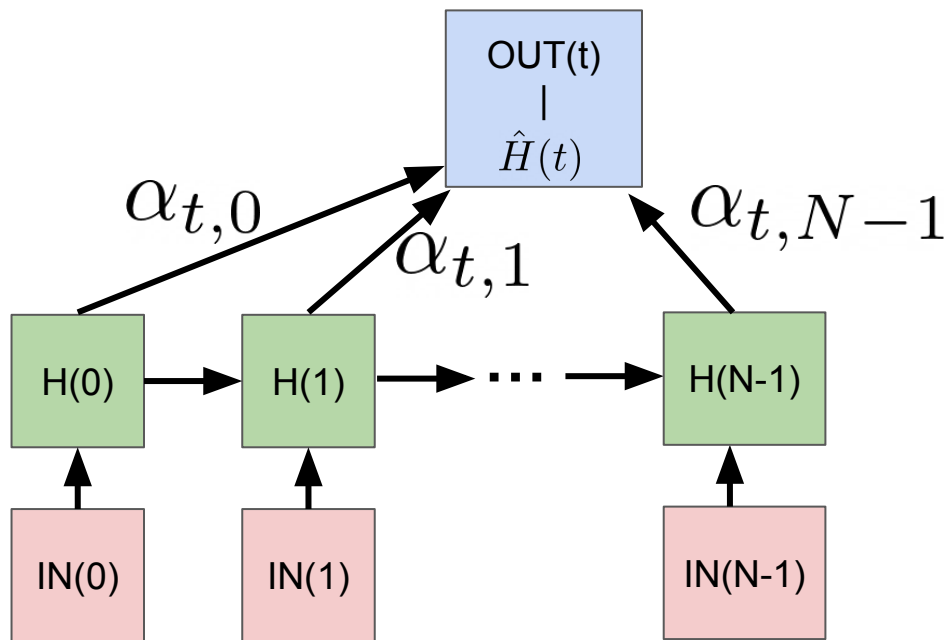
- Outputs:  $\hat{H} = \hat{V}$
- Inputs:
  - $K(t), V(t) = H(t)$
  - $Q(t) = \hat{H}(t - 1)$



# RNN Training

In this simple form:

- Attention is fixed
- Use backpropagation to simultaneously learn:
  - Encoder that produces  $H(t)$  from  $H(t-1)$  and  $IN(t)$
  - Decoder that produces  $OUT$  from  $\hat{H}(t)$



# RNN Training

- Through attention, every output token has the opportunity to examine every input token, so we are doing  $N^2$  comparisons
- We are still doing backpropagation through  $N$  latent layers (our  $H$ 's)

# Multi-Headed Attention

- Explicitly acknowledge that different categories of information need to be extracted and represented separately
- For example, may want to separately capture how the current word relates to other words in the sentence:
  - The action (verb)
  - Modifications to the action (adverbs)
  - The subject
  - ...



# Multi-Headed Attention

Approach: multiple single-headed Attention modules are used in parallel. For each head:

- Input: its own “perspective” on the MH Attention inputs (implemented as three linear projections)
- Output: its own  $\hat{H}_i(t)$

Grand output is a linear combination of the the individual heads: 
$$\hat{H}(t) = \sum_{i=0}^{K-1} w_i^O \hat{H}_i(t)$$

# Implementation Details

Single-Head Attention:

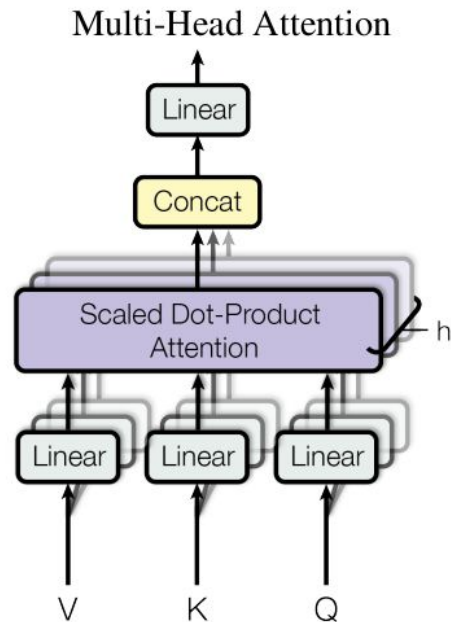
$$\text{Attention}(Q, K, V) = \text{softmax}(Q K^T) V$$

Multi-Head Attention:

$$Q_i = Q W_i^Q \quad K_i = K W_i^K \quad V_i = V W_i^V$$

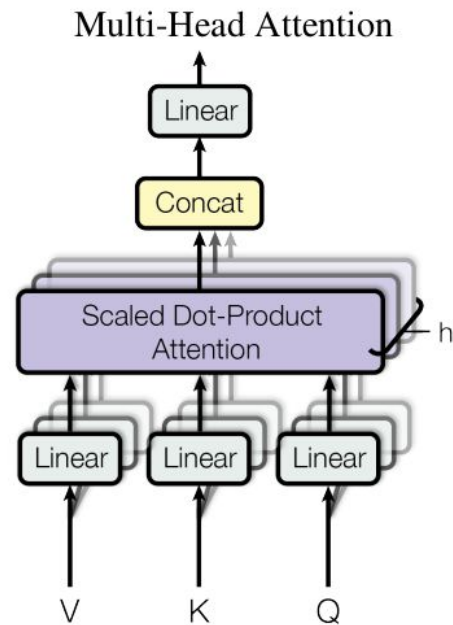
$$\hat{H}_i = \text{Attention}(Q_i, K_i, V_i)$$

$$\hat{H} = \sum_{i=0}^{K-1} w_i^O \hat{H}_i$$



# Implementation Details

- Each head has its own linear parameters
  - Linear parameters are shared across the input tokens
- These parameters are selected as part of the larger learning process
- This allows each head to specialize in what types of information it extracts



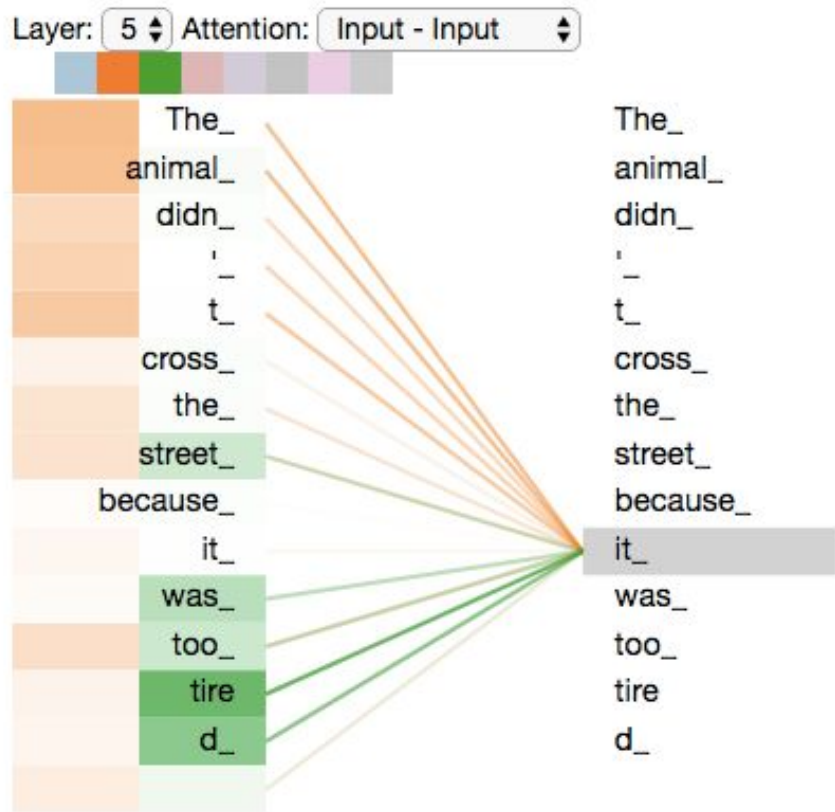
# Multi-Headed Attention

*The animal didn't cross the street because it was too tired*

Two Attention heads:

- What does ***it*** refer to?
- What is the description of ***it***?

<http://jalammar.github.io/illustrated-transformer/>



# RNN Training with Attention

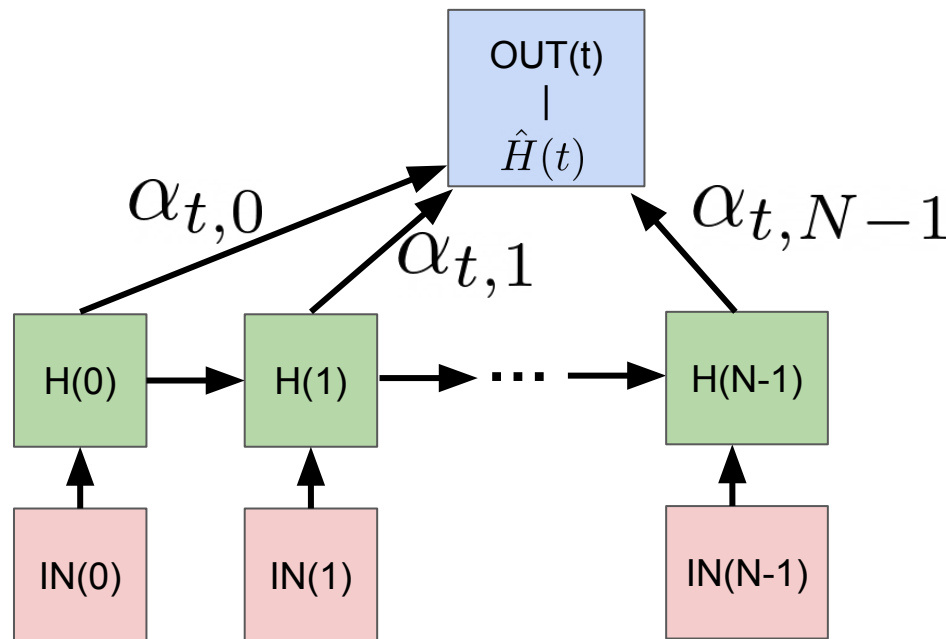
- Through attention, every output token has the opportunity to examine every input token, so we are doing  $N^2$  comparisons
- We are still doing backpropagation through  $N$  latent RNN layers (our  $H$ 's)

The deep backpropagation is still a big computational problem

# Re-Examining the RNN

- $H(t)$  is a function of all of the input tokens  $IN(0) \dots IN(t)$
- $H(t)$  must contain information that is useful for  $H(t+1) \dots$

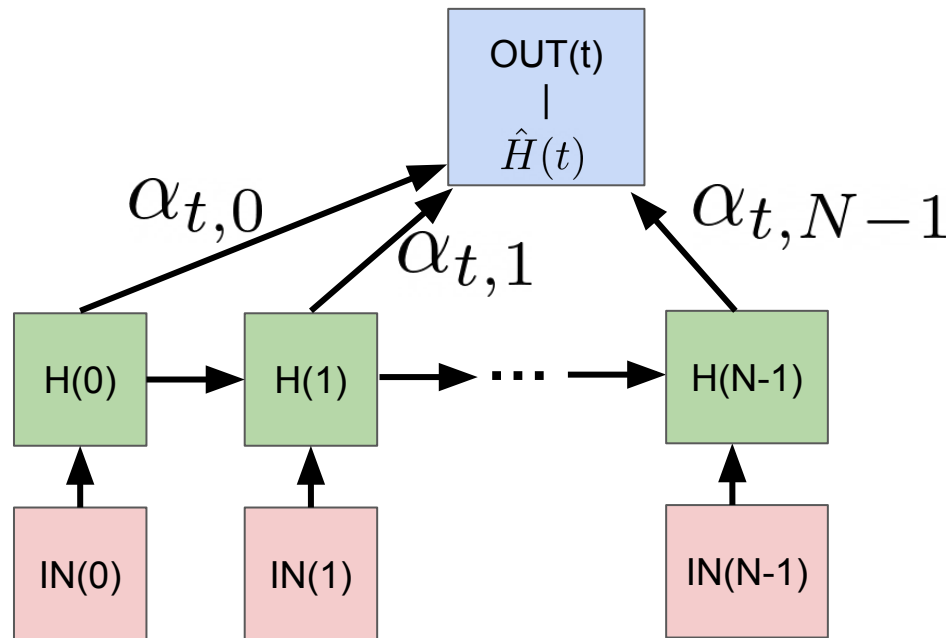
What if  $H(t)$  could just focus on the input tokens that are relevant specifically to the decisions that it needs to make?



# Re-Examining the RNN

What if  $H(t)$  could just focus on the input tokens that are relevant specifically to the decisions that it needs to make?

-> This sounds just like  
**Attention!**



# Attention is All You Need

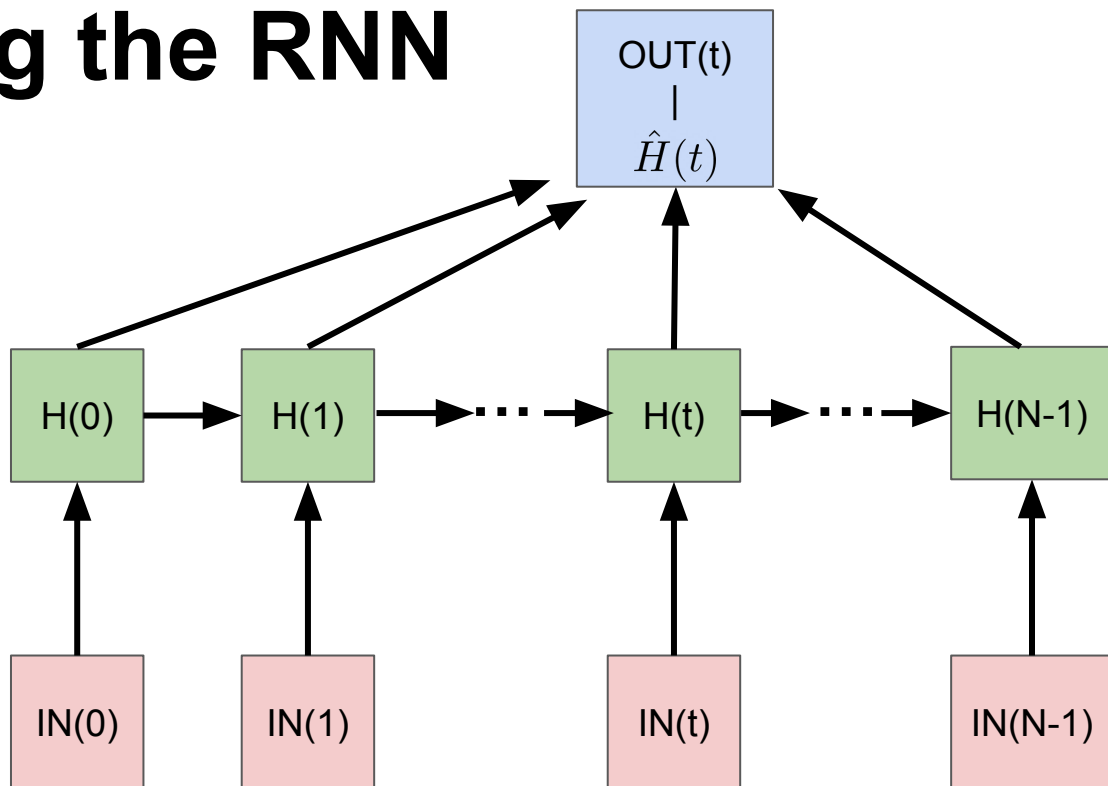
Vaswani et al. (2017):

- Attention to process the input tokens
- Attention to generate the output tokens



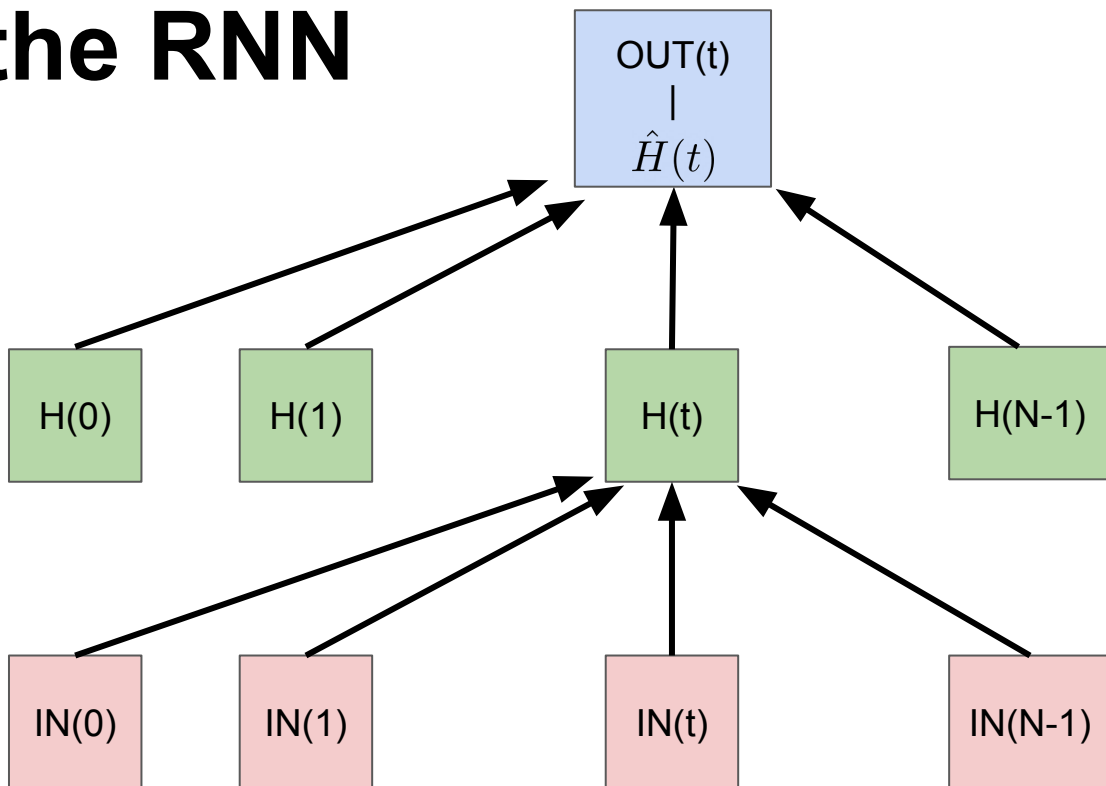
# Re-Examining the RNN

Primary challenge comes from the connection from  $H(t)$  to  $H(t+1)$



# Re-Examining the RNN

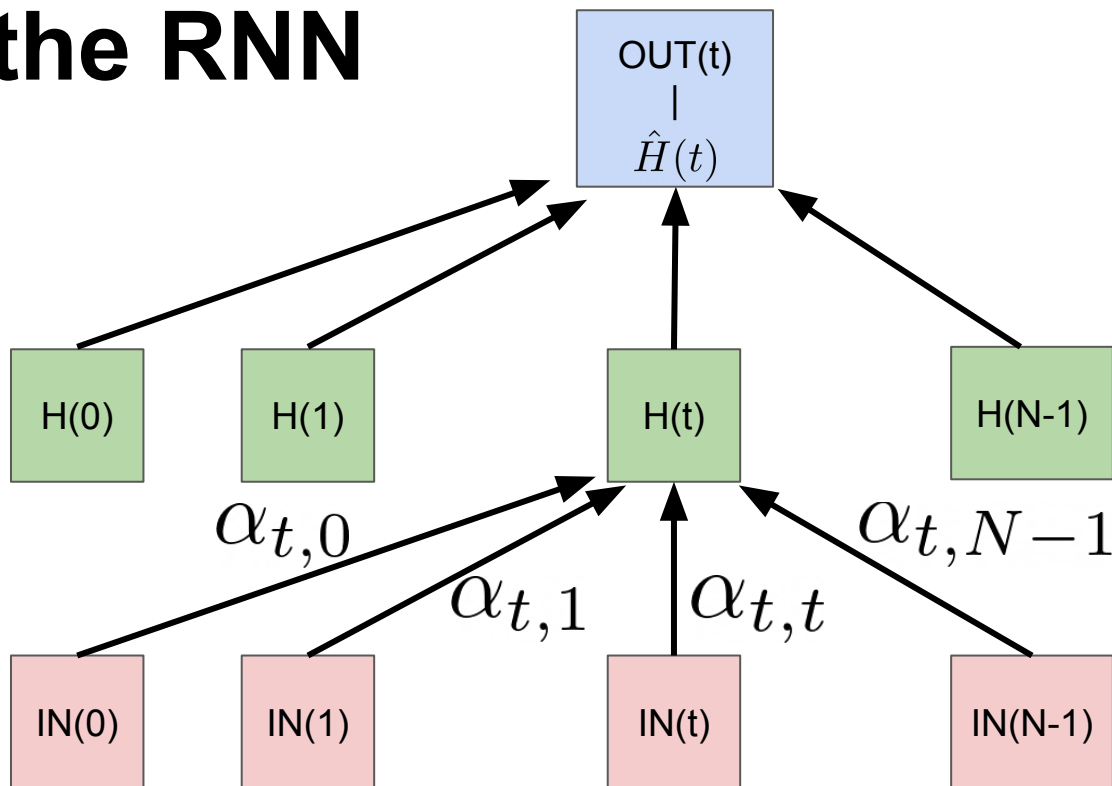
Each latent step has access to all inputs simultaneously



# Re-Examining the RNN

Each latent step has access to all inputs simultaneously

- Blend of all inputs
- Implemented using Multi-Headed Attention



# Implementation Details

Single-Head Attention:

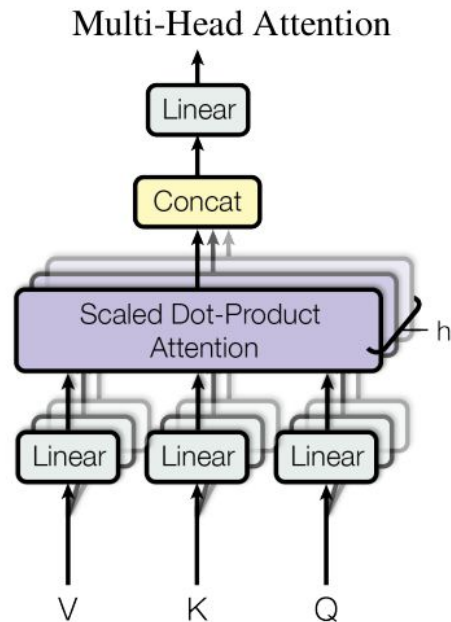
$$\text{Attention}(Q, K, V) = \text{softmax}(Q K^T) V$$

Multi-Head Attention:

$$Q_i = Q W_i^Q \quad K_i = K W_i^K \quad V_i = V W_i^V$$

$$\hat{H}_i = \text{Attention}(Q_i, K_i, V_i)$$

$$\hat{H} = \sum_{i=0}^{K-1} w_i^O \hat{H}_i$$



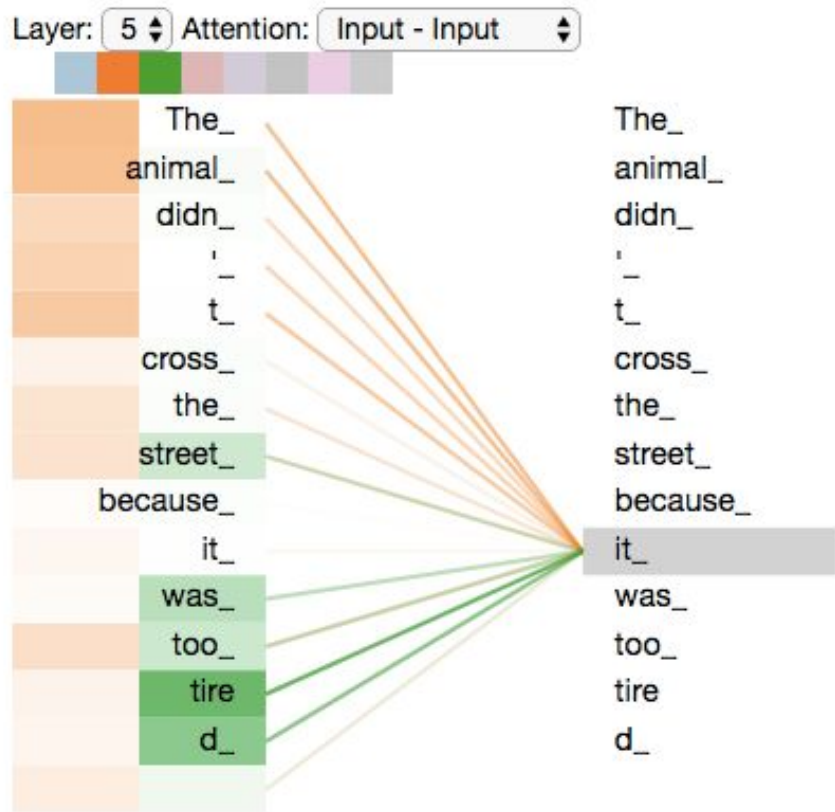
# Multi-Headed Attention

*The animal didn't cross the street because it was too tired*

Two Attention heads:

- What does ***it*** refer to?
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<http://jalammar.github.io/illustrated-transformer/>



# Tool: Position Encoding

- With our RNN encoder, the relative positions of the input token are captured in the latent representation
- Likewise, with our decoder, relative positions of the output words were captured in the blended latent representation & the output

By replacing our RNN encoder with MH Attention, we lose an encoding of position

# Position Encoding

Goals for a positional encoding:

- Want the network to be able to reason about absolute position in the sequence of an input token
- Also want the network to be able to reason about the relative position of two input tokens
- Should make use of finite values, even when the sequences are long

# Positional Embeddings

Approach: for each token, translate its integer position in the sequence ( $t$ ) into a vector

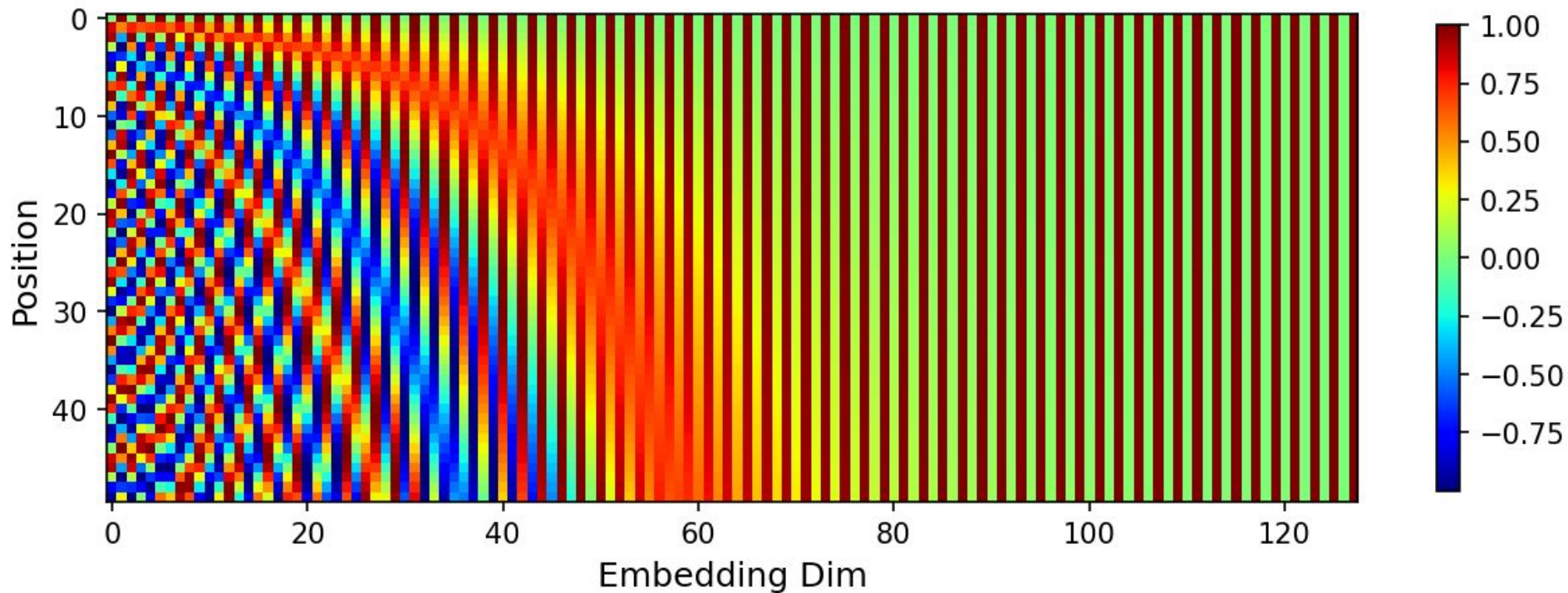
where:

$$w_k = \frac{1}{10000^{(2 \cdot k / d)}}$$

$$\vec{p}_t = \begin{bmatrix} \sin(\omega_1 \cdot t) \\ \cos(\omega_1 \cdot t) \\ \\ \sin(\omega_2 \cdot t) \\ \cos(\omega_2 \cdot t) \\ \\ \vdots \\ \\ \sin(\omega_{d/2} \cdot t) \\ \cos(\omega_{d/2} \cdot t) \end{bmatrix}_{d \times 1}$$



# Embedding Example



# Positional Embeddings

Details:

- $d$  is selected to match the token embedding size
- #positions is the maximum “sentence” length
- 10,000 is selected so that the different positional encodings are distinct
- Each element falls within +/- 1

$$\vec{p}_t = \begin{bmatrix} \sin(\omega_1 \cdot t) \\ \cos(\omega_1 \cdot t) \\ \\ \sin(\omega_2 \cdot t) \\ \cos(\omega_2 \cdot t) \\ \\ \vdots \\ \\ \sin(\omega_{d/2} \cdot t) \\ \cos(\omega_{d/2} \cdot t) \end{bmatrix}_{d \times 1}$$

# Positional Embeddings

Key property: easy to compute the relative difference between two positions

- Consider the encoding of two positions:  $p_t$  and  $p_{t+\Delta t}$
- For any  $t$  and  $\Delta t$ , they are related through a fixed linear transformation:  $p_{t+\Delta t} = D(\Delta t) p_t$
- Where:
  - $D(\Delta t)$  is a fixed tridiagonal matrix that is only a function of  $\Delta t$  !

# Positional Embeddings: Implications

Two tokens that are separated by a fixed distance ( $\Delta t$ ) share the same  $D(\Delta t)$

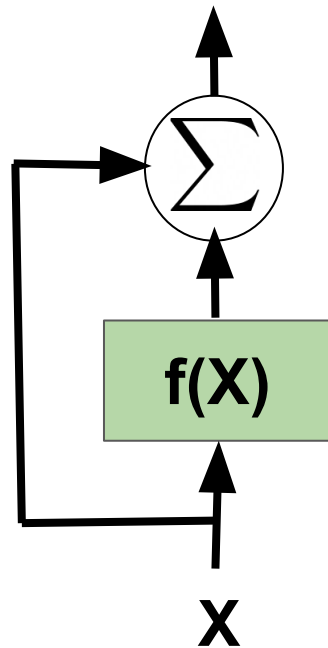
- Relative positions between tokens are really easy to compute by our network
- The phrase “they are” are the same positional difference, no matter their absolute location
- The phrase “are they” has a distinct difference in meaning
- Allows for generalization to sequence lengths that are different than what the network is trained with

# Next Tool: Skip Connections

- Shapes of  $X$  and  $f(X)$  are the same
- Error propagation through  $f()$ : it can be hard to find a gradient
- Error propagation through the skip is trivial

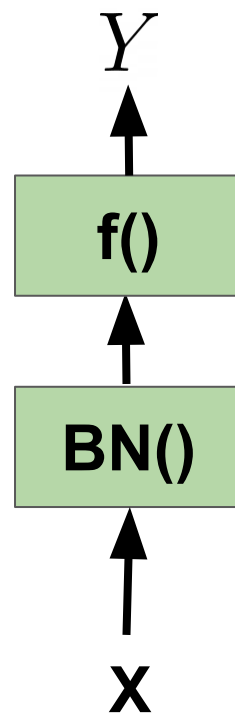
-> Even when there are many of these modules stacked on top of each other, there is an easy gradient to find

$$Y = X + f(X)$$



# Final Tool: Batch Normalization

- Statistics of  $X$  over a large batch *\*can\** be anything
  - Assume that we fall within a Normal dist
- $\text{BN}()$  scales and translates each element of  $X$  so that the inputs to  $f()$  fall according to  $N(0,1)$
- This means that the **net inputs** to  $f()$  are more likely to fall within the dynamic range of the non-linearity within  $f()$



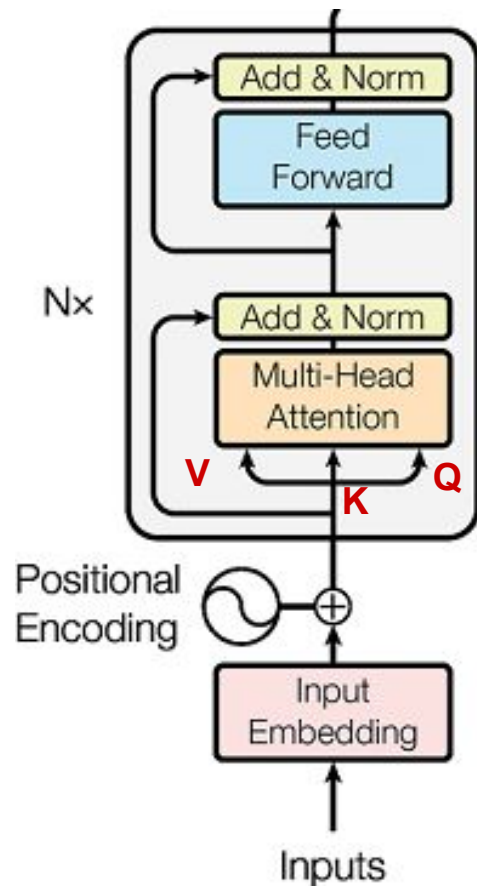
-> Much less likely to vanish the gradient

# Putting All the Pieces Together

- Input: encoded sequence of tokens ( $N \times d$ )
- Encoder: use Attention to create a sequence of “hyper-tokens” (also  $N \times d$ ), each of which captures some subset of the token sequence
  - Computed in parallel
- Decoder: use Attention to “read out” one token at a time
  - Combines the latent representation of the encoder with what has already been read out

# Transformer: Encoder

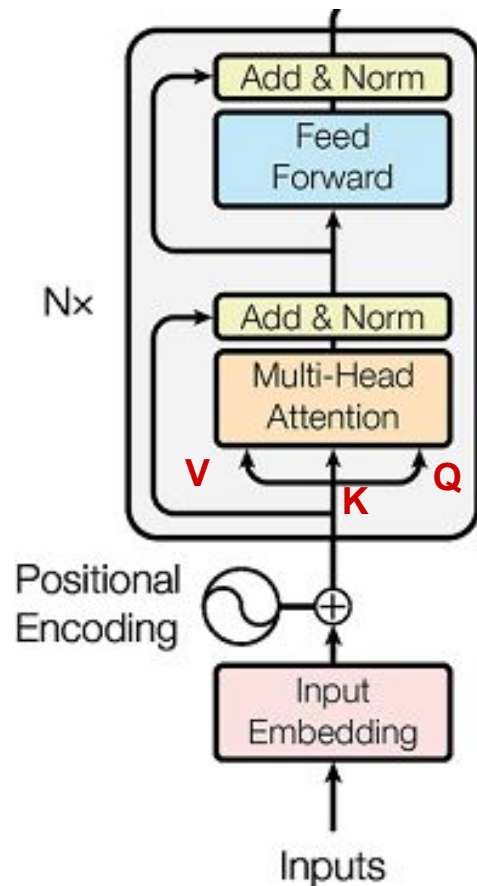
- Embedding of the inputs ( $N \times d$ ) is the same shape as the positional encoding for each position
- MH Attention creates multiple combinations of the input tokens
  - $V$ ,  $K$  and  $Q$  are all the same!
  - Called ***self-attention***
- Feed Forward is some learned function that is applied to each of the hyper-tokens





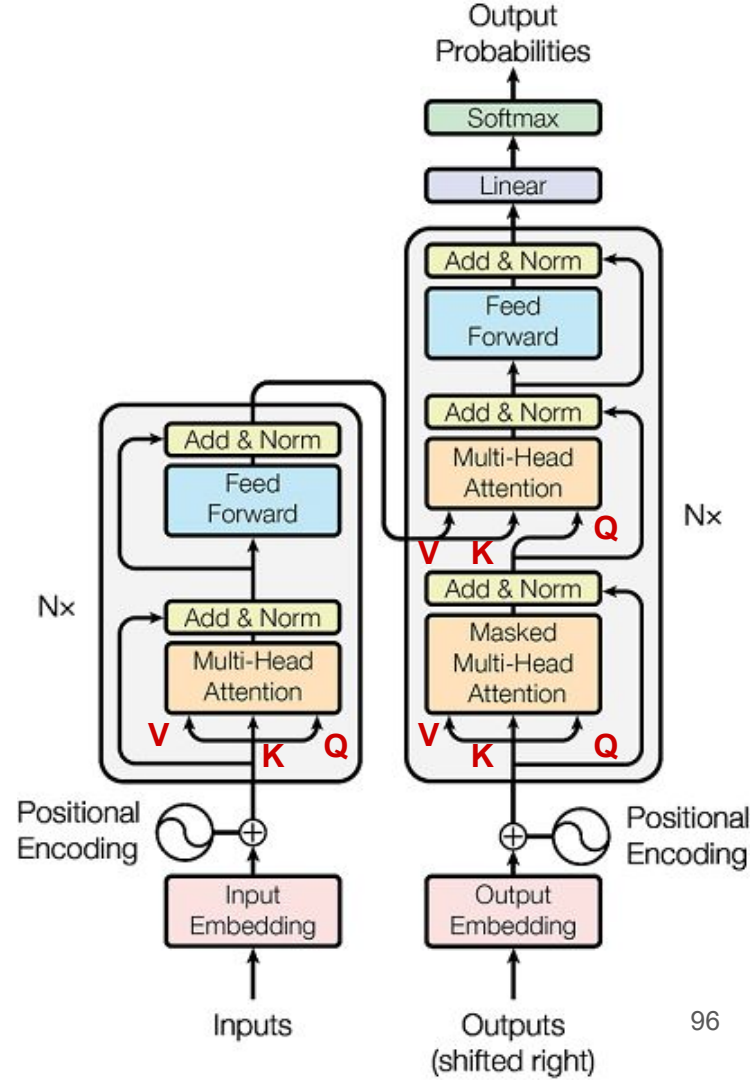
# Transformer: Encoder

- Skip connections + Normalization: avoid vanishing gradient
- Shape stays the same at each stage
- Stack multiple modules on top of each other (for Vaswani et al., they use  $N=6$ )



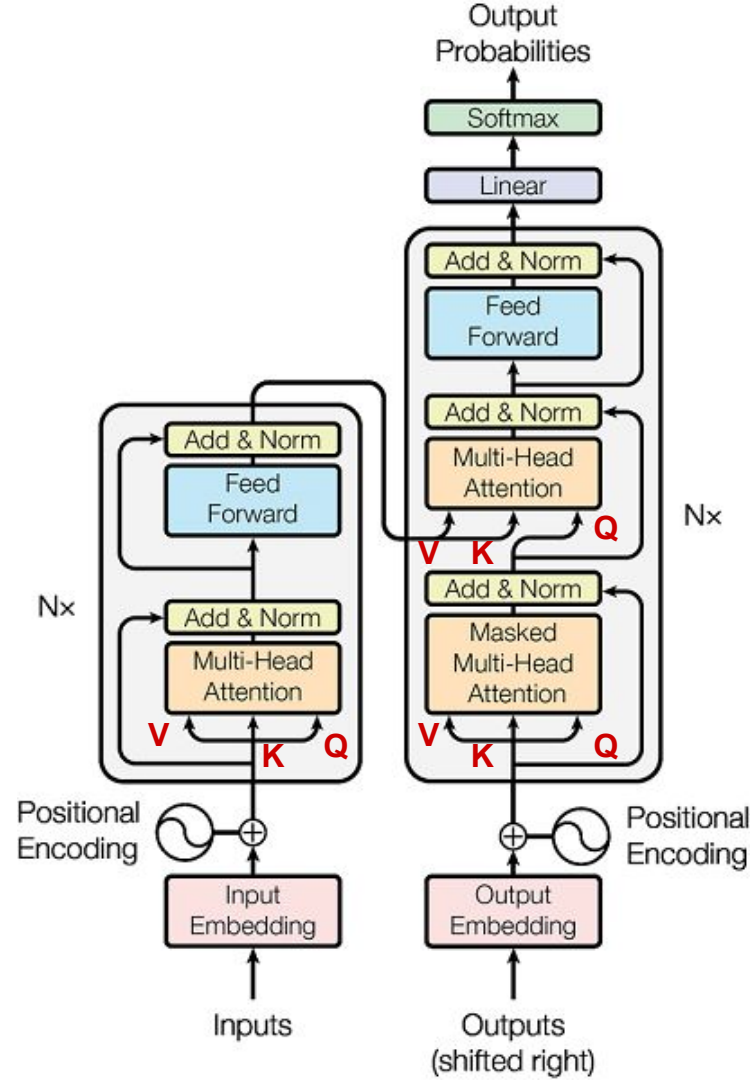
# Transformer: Decoder

- MH Attention 1: Hyper-token rep of output sentence
  - V, K and Q
  - Mask avoid “look ahead”
- MH Attention 2: Integrate input
  - V, K from Encoder
  - Q from Decoder



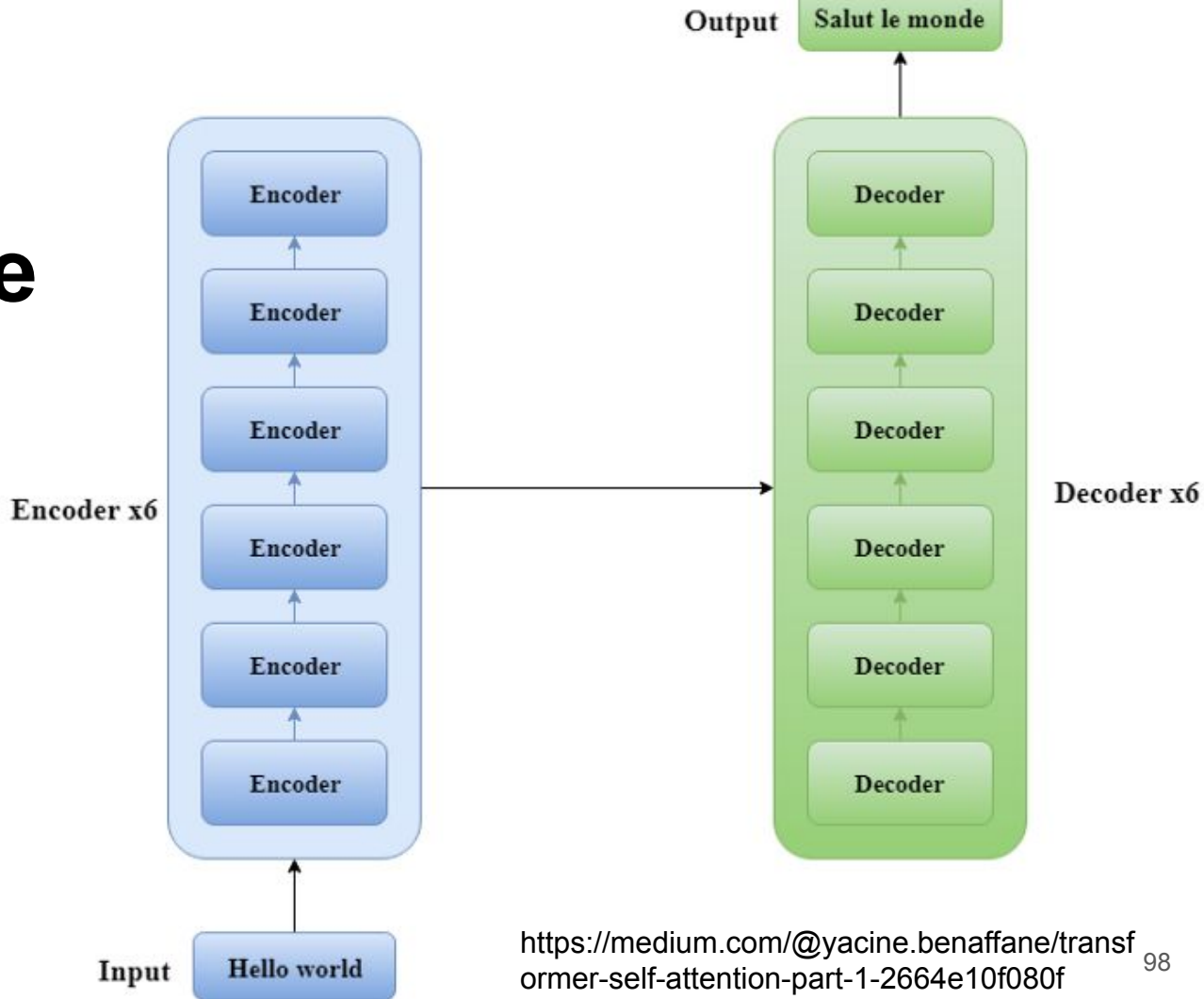
# Transformer: Decoder

- Stack multiple modules
- Final stages:
  - Linear transform computes scores for every possible output token
  - Softmax: probability of emitting a given token



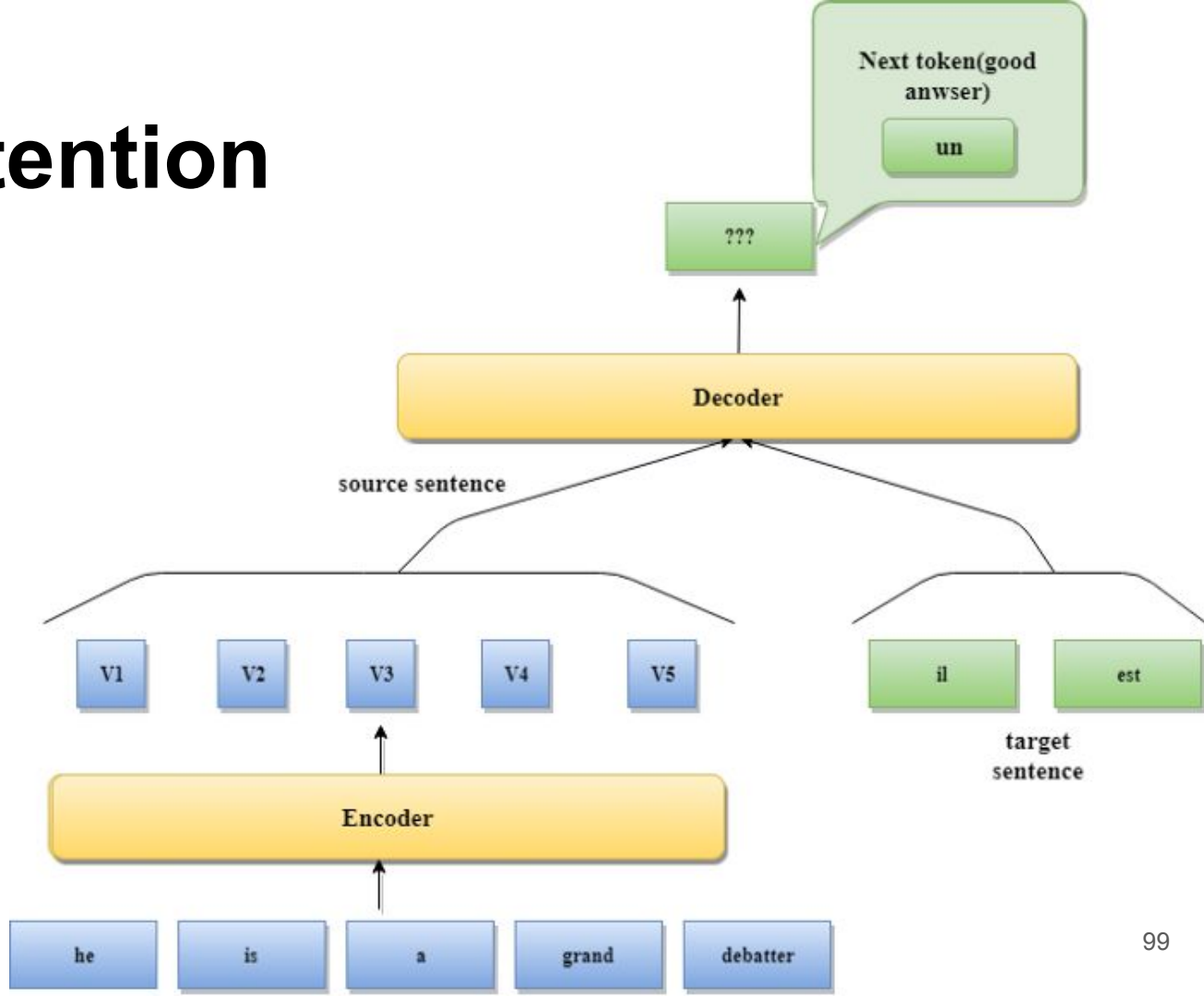
# Full Architecture

Note: output from the top of the encoder stack is the input to each of the decoder layers



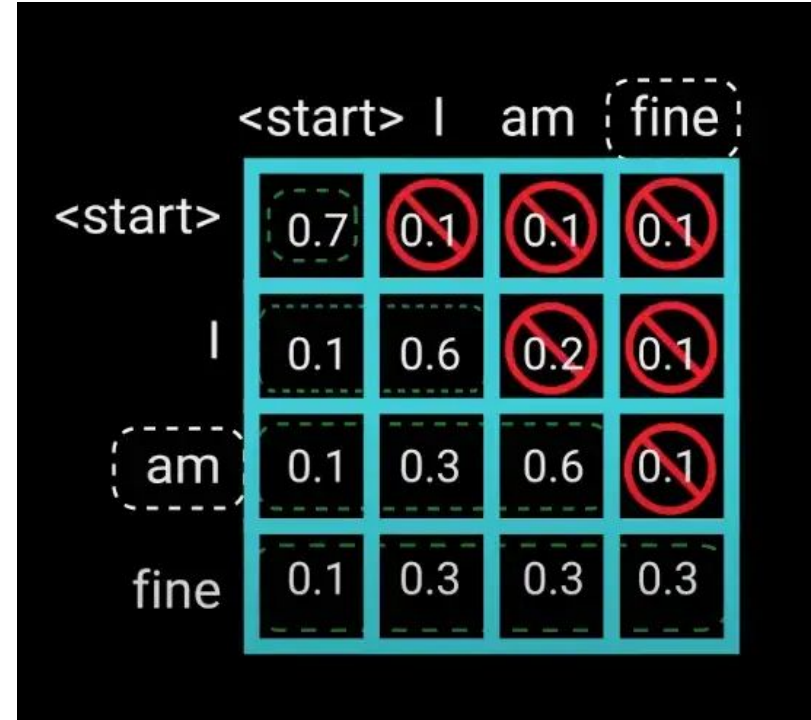
# Masked Attention

- Decoder only produces output one token at a time
- For a token at time  $t$ , we do not yet know output tokens  $t+1 \dots$



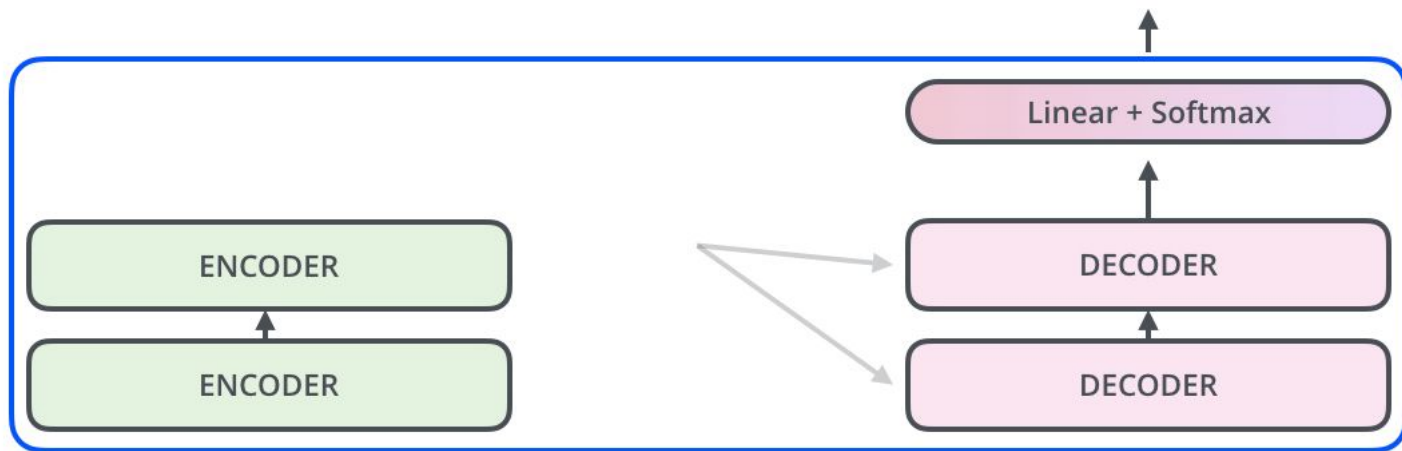
# Masked Attention

- Alphas for future tokens are set to zero
- Decoder input token “fine” cannot be used as context (the query) while selecting the output token “fine”

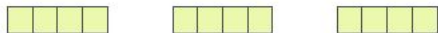


Decoding time step: 1 2 3 4 5 6

OUTPUT



EMBEDDING  
WITH TIME  
SIGNAL



EMBEDDINGS

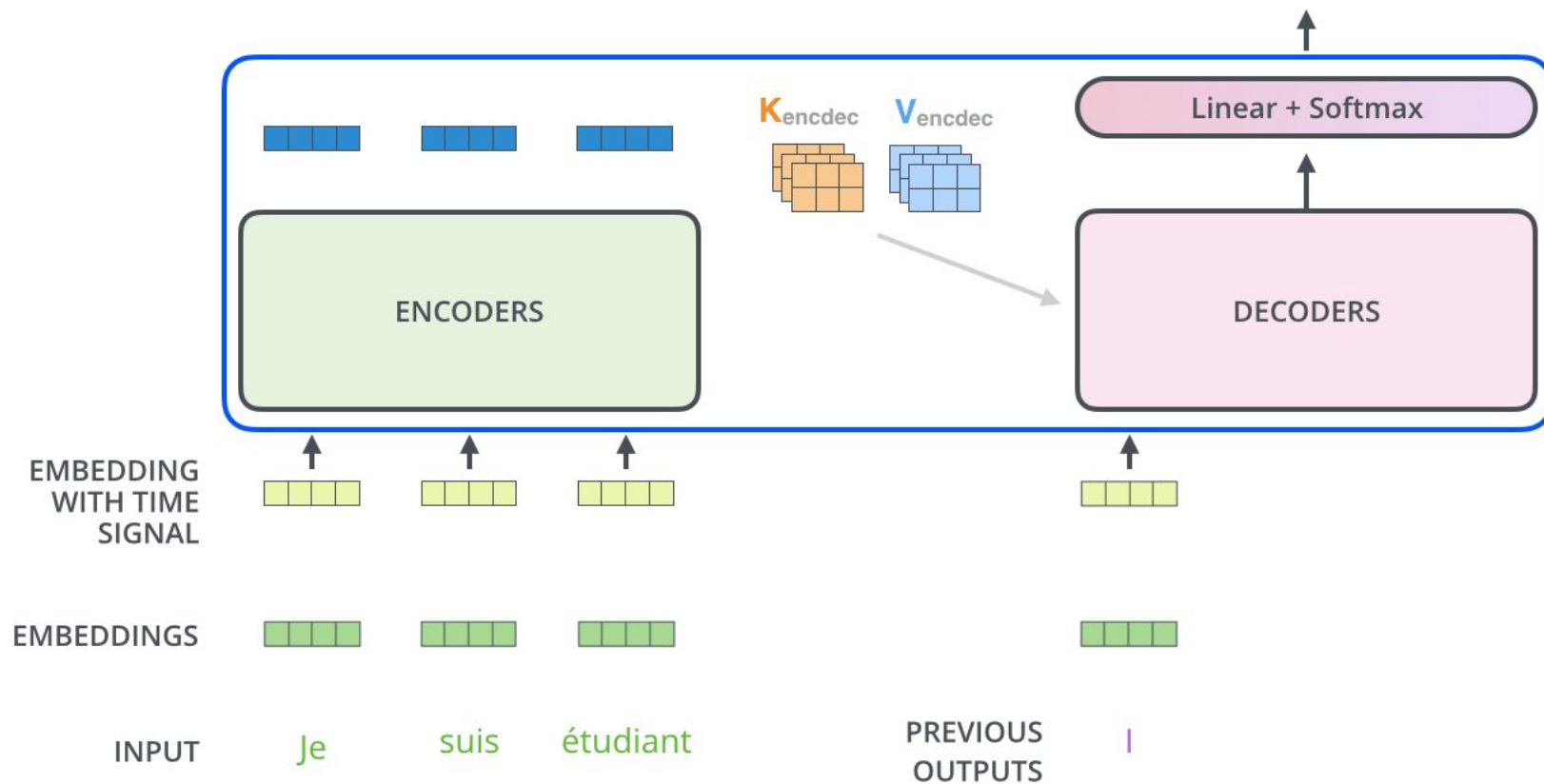


INPUT

Je suis étudiant

Decoding time step: 1 2 3 4 5 6

OUTPUT |





# Machine Translation Training Process

Simple case:

- Training is done with a large corpus of paired sentences/paragraphs/more across two languages
- Cost function: cross-entropy
- Although all of the true output tokens are known ahead of time, **Masked Attention** is still used so that the model does not learn to rely on future information

# Training Process

These models are data hungry. Many variations for addressing this with examples from a single language

- Self-supervised pre-training of the encoder model (BERT; Devlin et al., 2019)
- Judging similarity of sentences
- Predicting next sentence/paragraph/other

Also: multilingual training outperforms bilingual models

# Uses of Text-Based Transformers

- Language translation
- Generating text given small prompts
- Question answering systems
- Text summarization
- ...

# Transformers

- Transformers are one class of generative models
- Fundamentally, they are about sampling from a conditional distribution  $p(y|x)$ , where  $x$  and  $y$  are composed of smaller, similarly-structured objects
  - Objects have some spatial or temporal relationship
  - Often gridded

# Transformers: Extensions

x and y can come from different domains

- Text to image
- Text to movie
- Image to text
- Image to semantic segmentation
- Image to repaired image

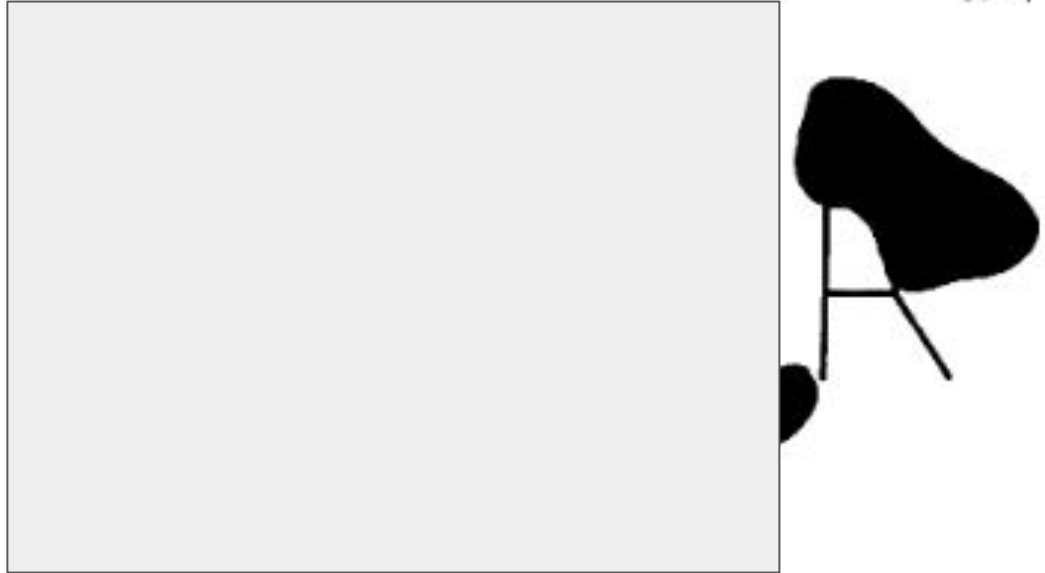
# Gentle? Introduction to Attention and Transformers III

Andrew H. Fagg  
Symbiotic Computing Laboratory  
University of Oklahoma



# A Challenge

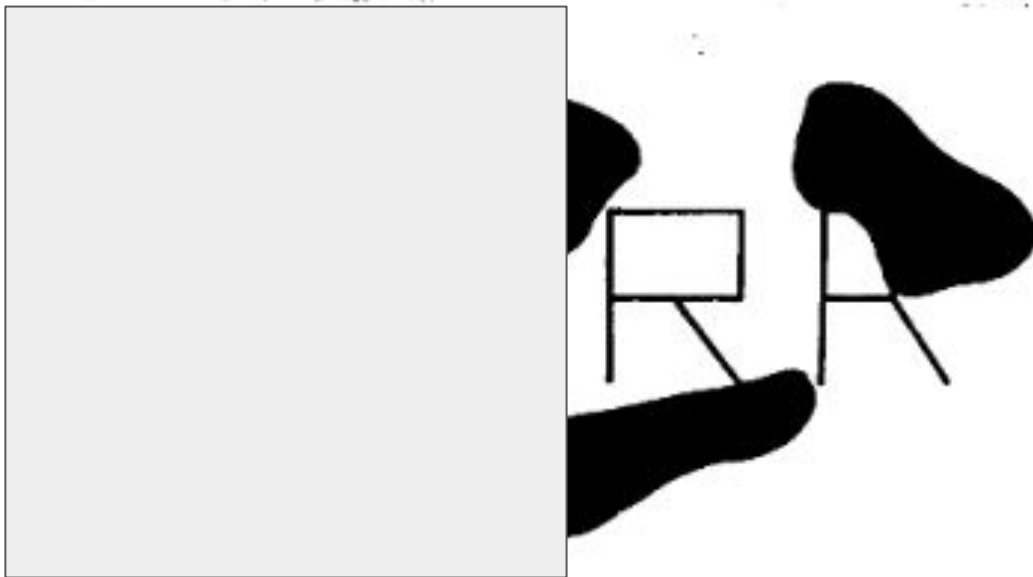
What is this letter?



McClelland & Rumelhart (1981)

# A Challenge

What is this letter?

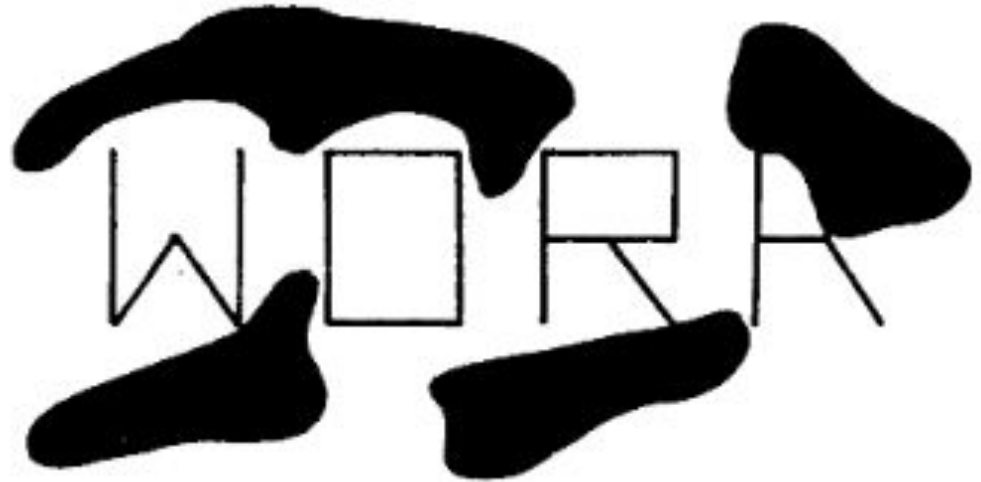


McClelland & Rumelhart (1981)



# A Challenge

What is this letter?

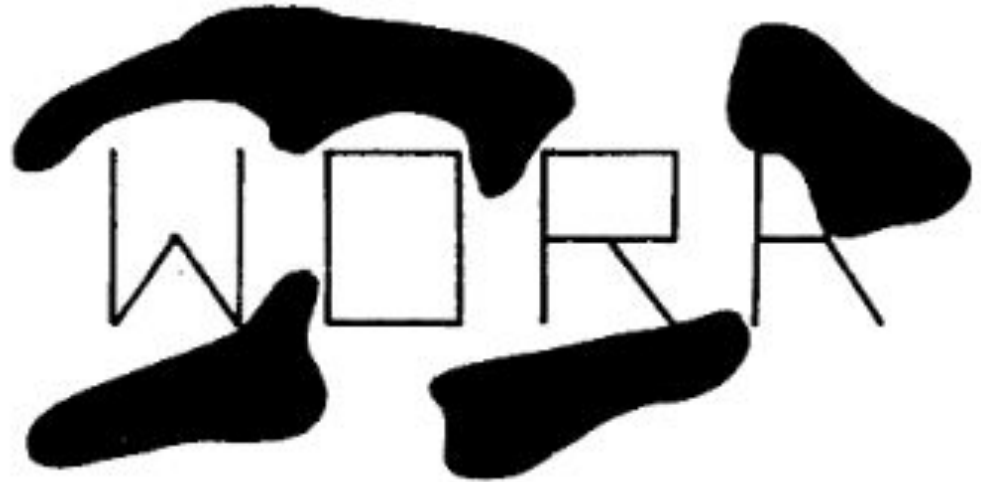


McClelland & Rumelhart (1981)

# A Challenge

What is this letter?

We need the context of the entire sequence of letters to properly interpret the last letter



McClelland & Rumelhart (1981)

# Review: Our Data Context

- Most general sense: we are working with some regular sampling of ‘objects,’ each of which is described by some feature vector
  - Sequences of words/tokens
  - Sequences of images or parts of images
- Our models must be able to reason (potentially) about all elements of the sequence as it is producing its predictions

I am going to continue to use the word ***token*** to mean the representation of a single object

# Attention

While the model is processing one token in this sequence, it often must use the context of the other tokens in the sequence to properly interpret it

- The word 'it' in the middle of a sentence is ambiguous
- An eye-like shape in an image can be interpreted in different ways
- An updraft has different meanings, depending on other, nearby, high-level features

# Attention

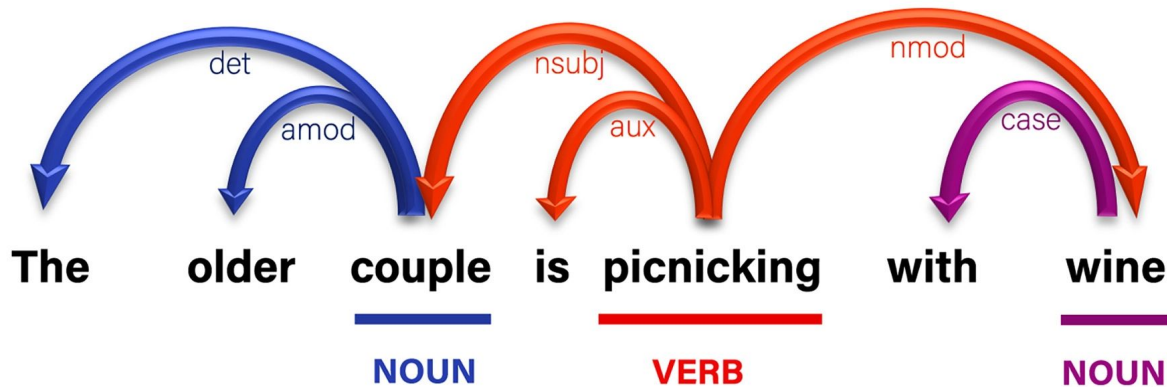
- Attention enables the model to bring in information from other parts of the sequence
- It is selective as to what information is used
- For sentences, can think of the model as ‘decorating’ a word with richer, context-specific information
- Multi-headed attention provides multiple types of decoration for a single input element

A

The older couple is picnicking with wine.



B



C

det + amod + NOUN      nsubj+ aux + VERB + nmod      case + NOUN

# Position Embedding

- Judging how one token should decorate another token depends on their relative positions
- Positional embedding re-encodes the index position to a vector. Key properties:
  - All elements of the embedding fall within  $\pm 1$
  - Difference of position between two tokens is a linear operation

# Transformers

Transformers are generative models: they produce samples from some conditional distribution  $p(y|x)$

- A sentence in German ( $y$ ) given a sentence in English ( $x$ )
- A sentence given a previous sentence
- The completion of an incomplete or corrupted image
- The generation of a sequence of images given a sequence of non-image objects



# Transformers

Key property: we have a sequence of input and output tokens. As we are sampling from  $p(y|x)$ :

- The tokens that are generated must be consistent with one another
- Hard to do all at once with long sentences or large images
- Transformers (and RNNs) solve this problem by generating one token at a time

# Transformers

Transformers solve this problem by generating one token at a time

- With this type of model, what has already been generated is important context for the next token to generate
- Transformers use a combination of the encoded input sequence and the encoded outputs up to time step  $t$  to decide what the next token(s) should be

# Plan for Today

Transformers for 2D data

- Image recognition (encoder only)
- Image generator (encoder + decoder)

# Image Recognition with Transformers

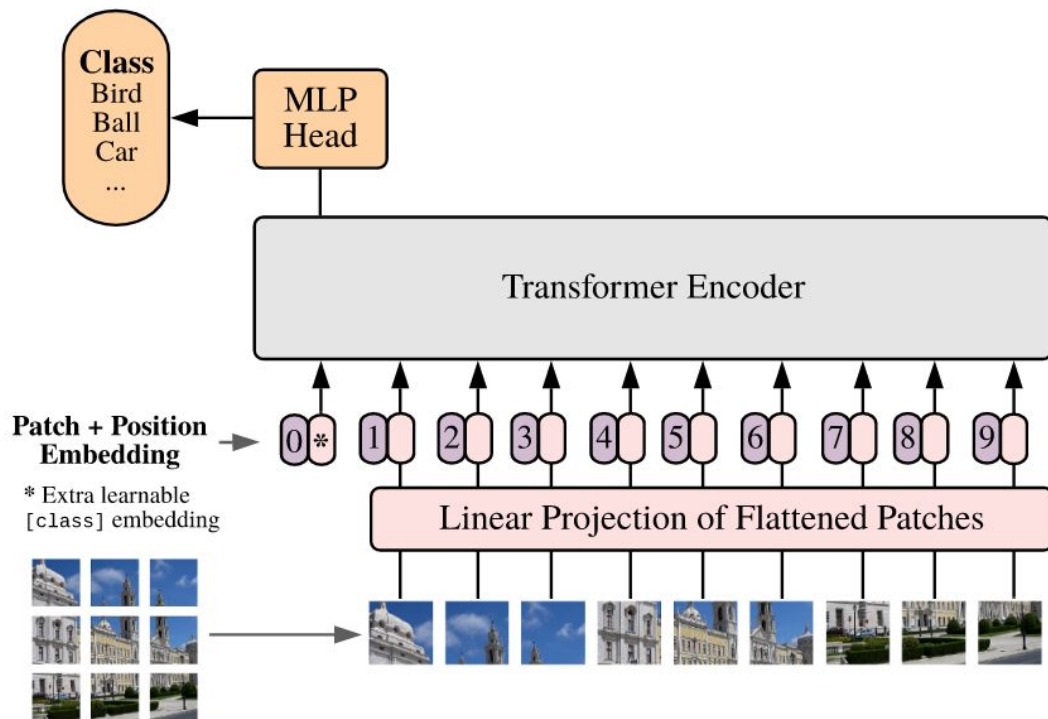
Ramachandran et al. (2019):

- Spatial convolutions can only integrate information from small neighborhoods
- But want to recognize spatial details that potentially cover the entire image
- Can Attention be used to replace convolutions?

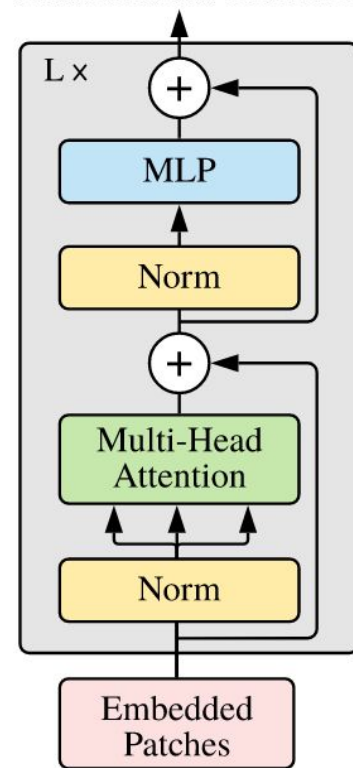
# Attention with Images

- Want to be able to integrate information from all corners of the image, but to do so in a computationally feasible way
- Proposal:
  - Cut the input image into a grid of image patches
  - The individual ‘tokens’ for attention are the image patches or are derived from them
  - Within a patch: processing is done with a fully-connected layer
  - Across patches: Attention layers

## Vision Transformer (ViT)



## Transformer Encoder



# Within a Patch

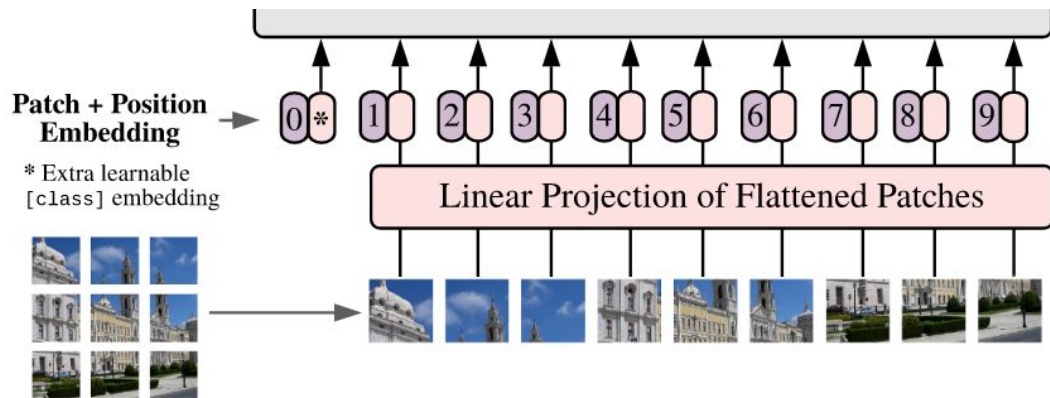
Extreme approach: pixels in a patch are flattened into an embedding vector

( $d = \text{\#pixels} \times \text{\#channels}$ ):



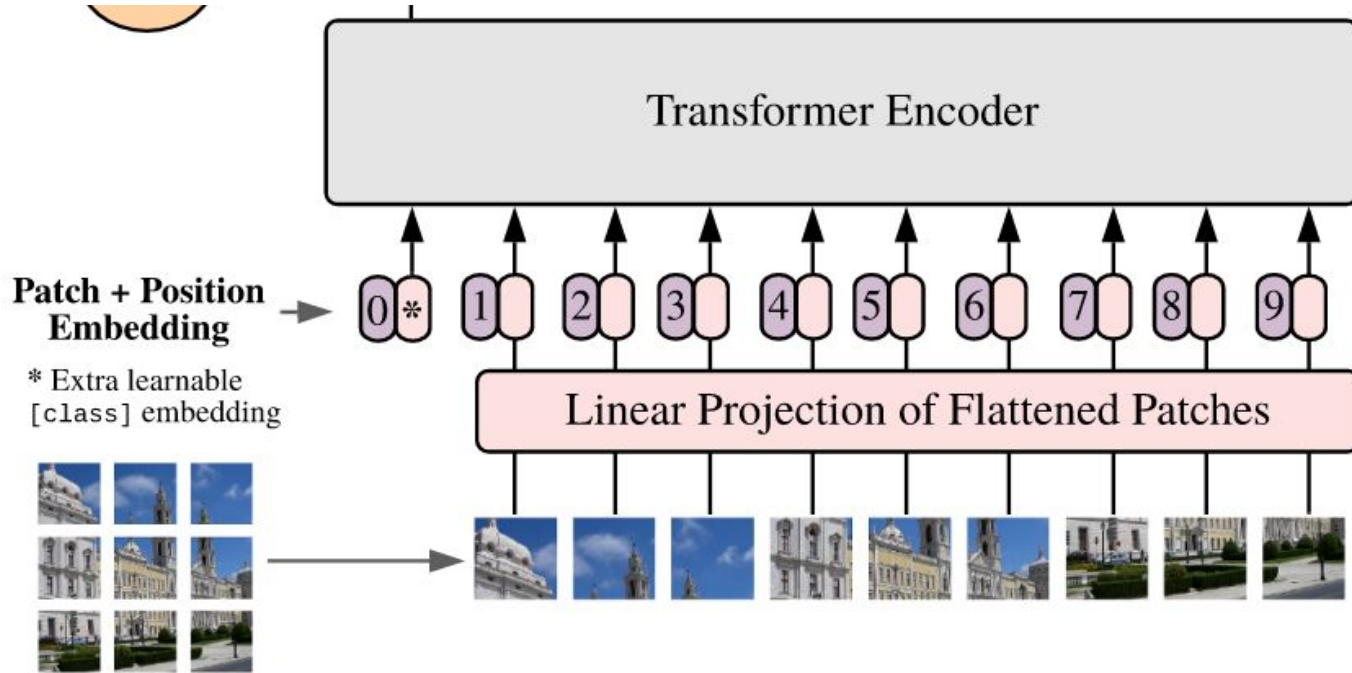
# Pre-Processing

- Patches can undergo some transformation beforehand
- Each patch is transformed in the same way
- Position embedding captures 2D position of each patch in the original image





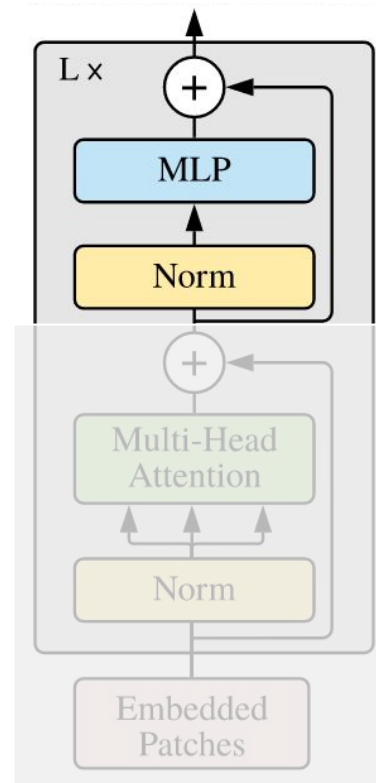
# Transformer Encoder



# Transformer Encoder Module

Latter stage:

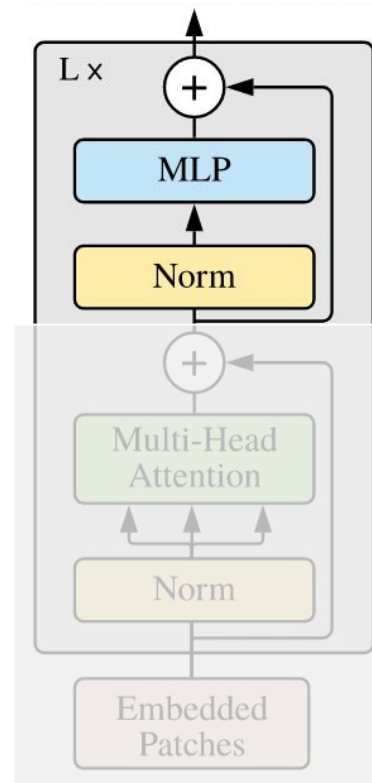
- Transforms a single patch into an output patch of the same dimensionality through a fully-connected layer (MLP)
- Each pixel in the patch influences every other pixel in the output patch



# Transformer Encoder Module

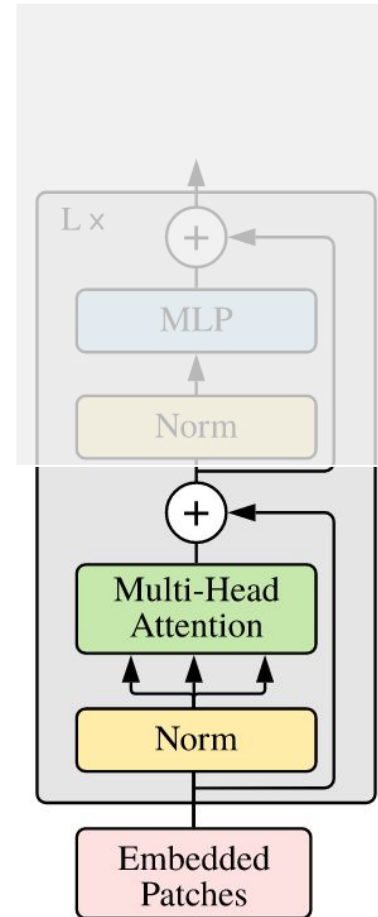
- A fully connected layer is far more expressive than a convolutional layer
- This comes at the cost of more parameters
- But, if the patches are small, then this is not a huge increase over convolution

Note: each of the patches are processed with same fully connected network



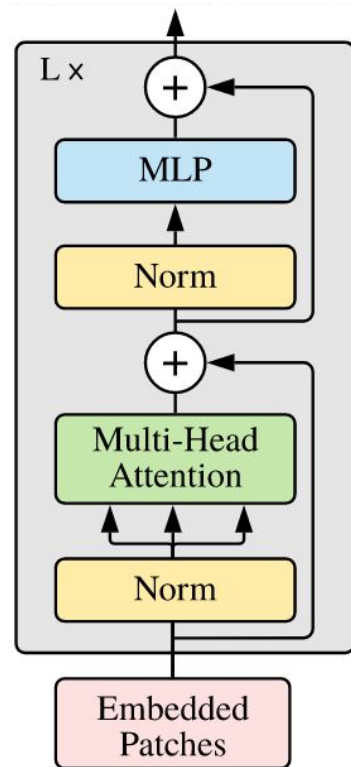
# Attention Across Patches

- Multi-Headed Self Attention: allows the interpretation of one image patch to be influenced by other patches
- This influence is implemented as a weighted blend of the patch with other patches (these are our attentional alphas, again!)
- Skip connection ensures that the current patch is maintained to some degree



# Transformer Encoder Modules

- Output shape is identical to the input shape
- Multi-Headed Attention: convolution-like operation, but with a reach across the entire image
- MLP: dense processing at a pixel scale within each patch separately



# Attention vs Convolution

- Convolution only allows a local neighborhood of pixels to influence the corresponding output pixel
  - This transformation is the same for all offsets
- Attention potentially allows all patches to influence all output patches
  - This influence varies depending on the match of the key/query match

Note: there is a scale difference here (pixels vs patches)

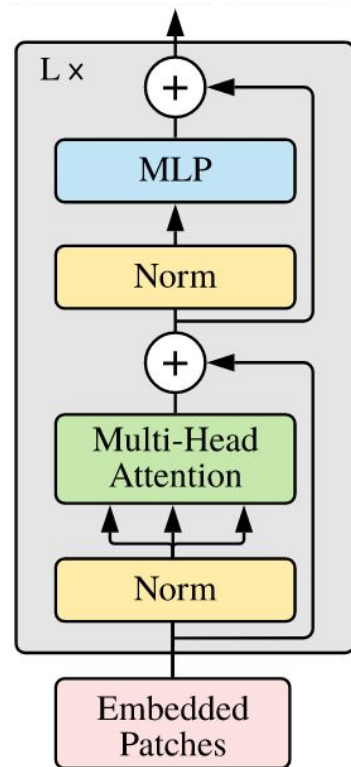
# Attention vs Convolution

- Pure Attention approach requires that all patches can attend to all other patches
  - This requires  $N^2$  comparisons & a lot of parameters
- Can reduce the complexity of the model by only allowing comparisons with a limited neighborhood of patches
- Think of this as a compromise between pure Attention and convolution

# Attention vs Convolution

Stacking multiple Attention modules on top of each other

- Allows for building more abstract representations the higher we go
- Can compensate for limited Attention
  - One patch may not be able to attend to another patch directly, but it can do so across multiple layers of modules





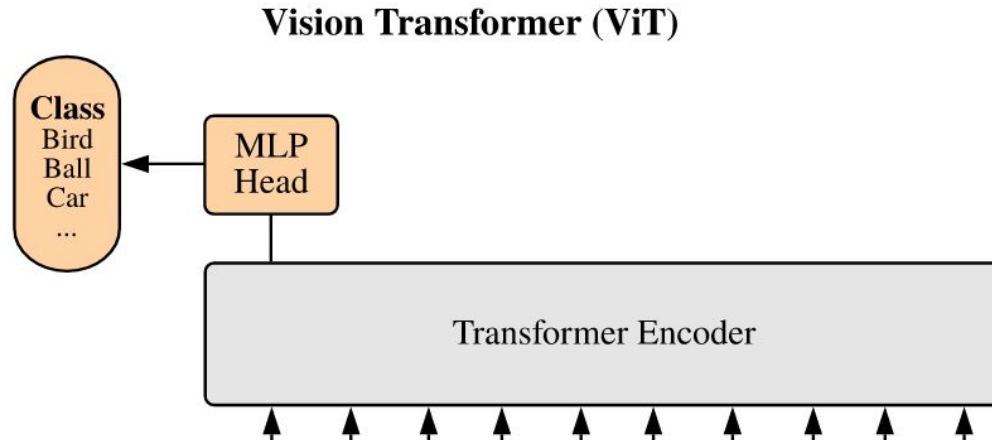
# Positional Embedding

Multiple options for implementation:

- None
- 1 D: absolute position of the patches
- 2 D: absolute row/col position of the patches (learned)
- 2 D-relative: relative row/col of two patches (learned)

Empirically: positional embedding is helpful over None

# Image Recognition



Final stage:

- Combine evidence across the patches
- Compute class probabilities (via softmax)

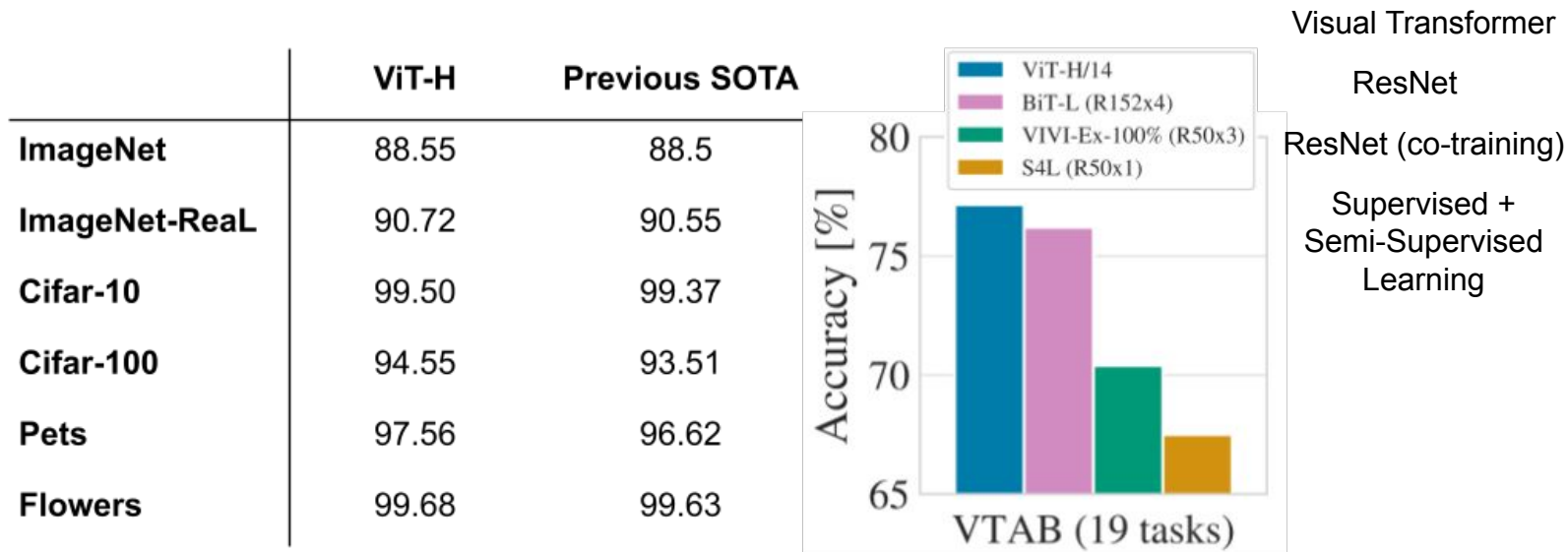


<https://ai.googleblog.com/2020/12/transformers-for-image-recognition-at.html>

# Training details

- Typical loss: cross-entropy
- These methods are very data hungry
  - ImageNet is really small by these standards
  - A lot of work has gone into using bigger data sets for training or for pre-training the models

# Results: Collection of Image Recog Tasks

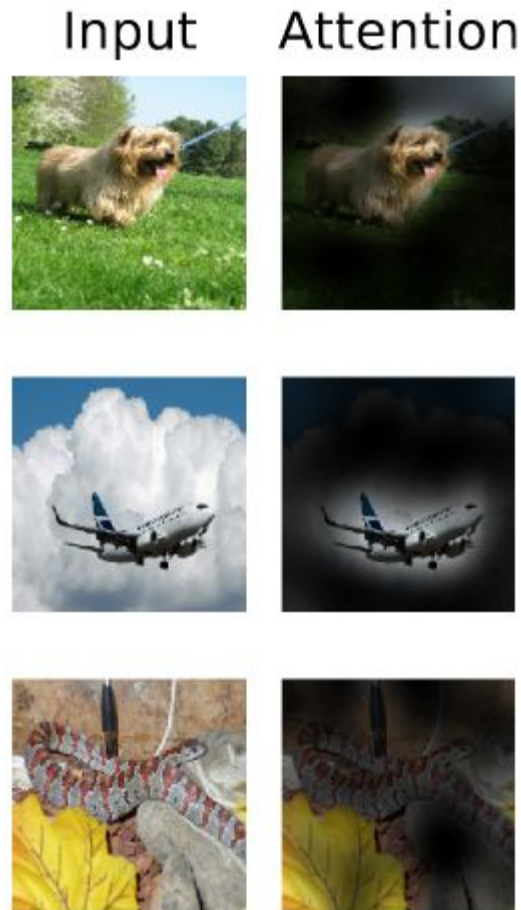


Requires fewer training compute cycles than SOTA CNNs

# Attention XAI

Aggregate Attention across multiple layers

- Approach feels a lot like Grad-CAM

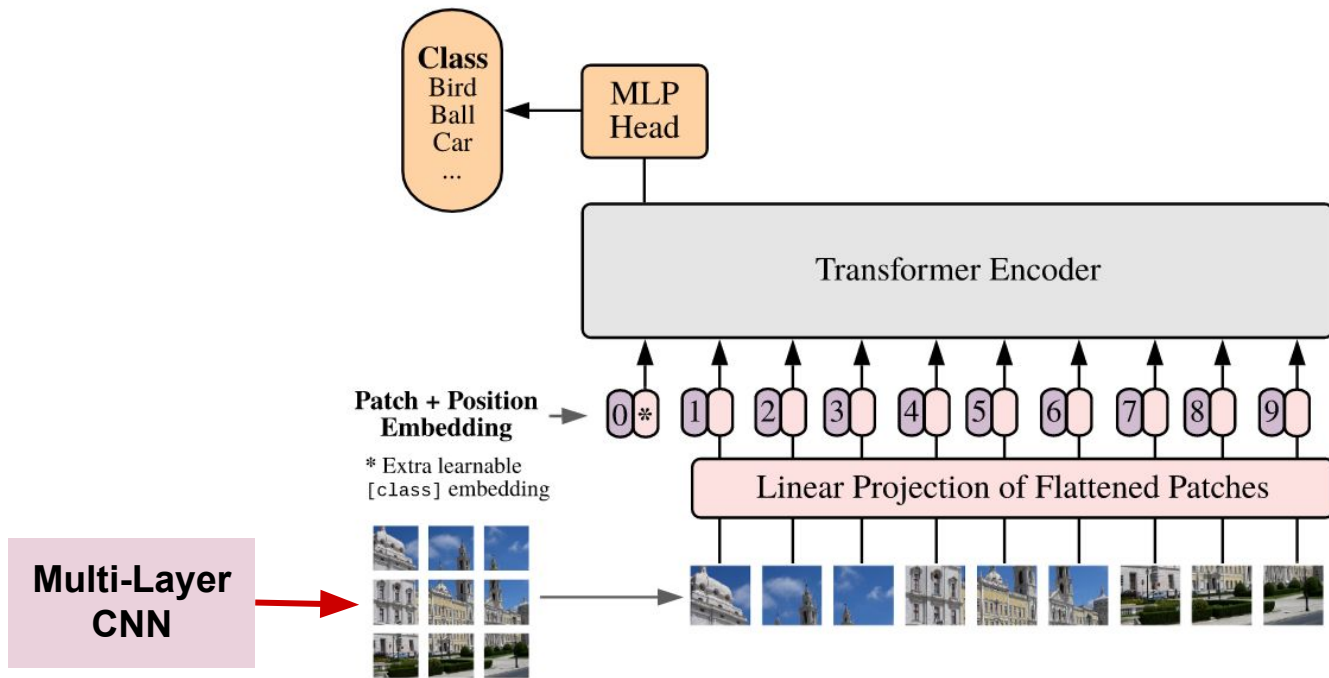


# Hybrid CNN / Attention Approaches

- Early layers are just about learning primitive feature detectors
- Convolution can do this with fewer parameters than Attention
- Ramachandran et al. (2019): Use a CNN as a pre-processing step to the Attention layers

# Hybrid CNN / Attention Approaches

## Vision Transformer (ViT)



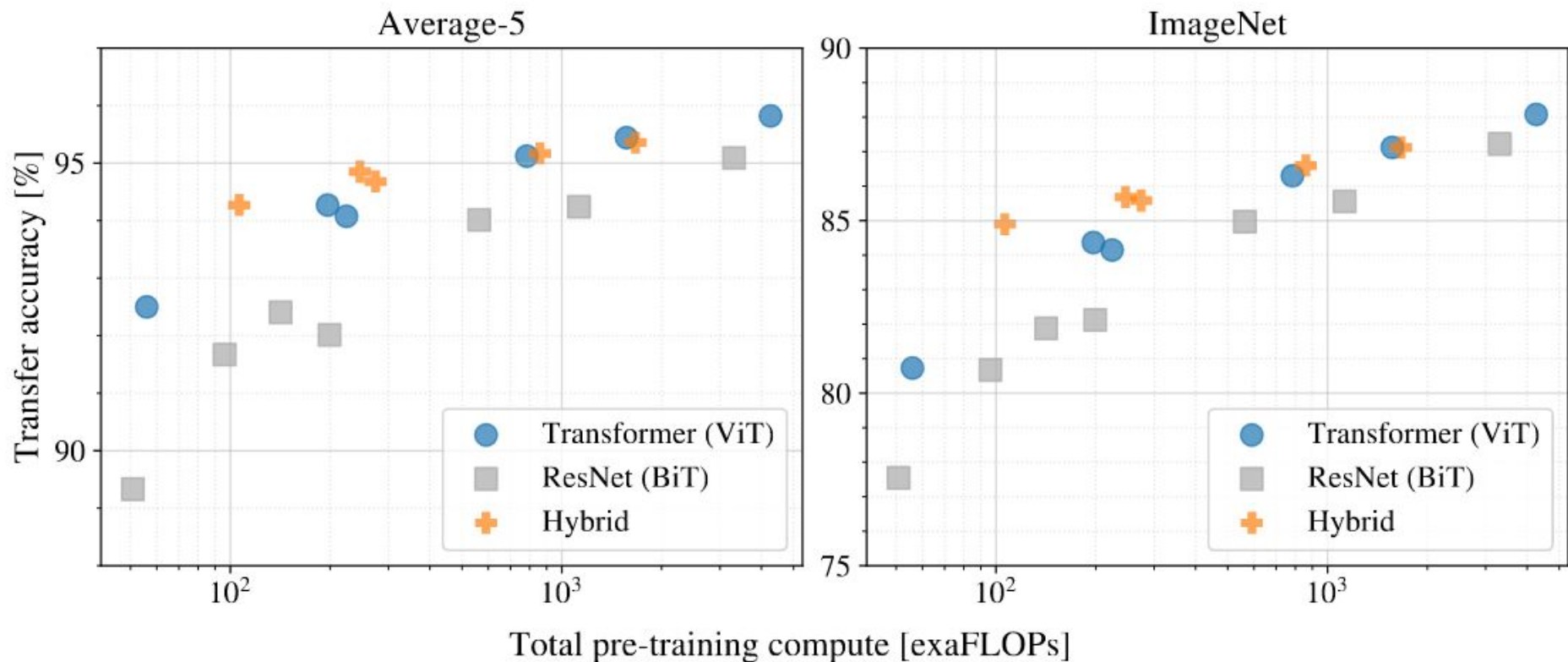


# Hybrid CNN / Attention Approaches

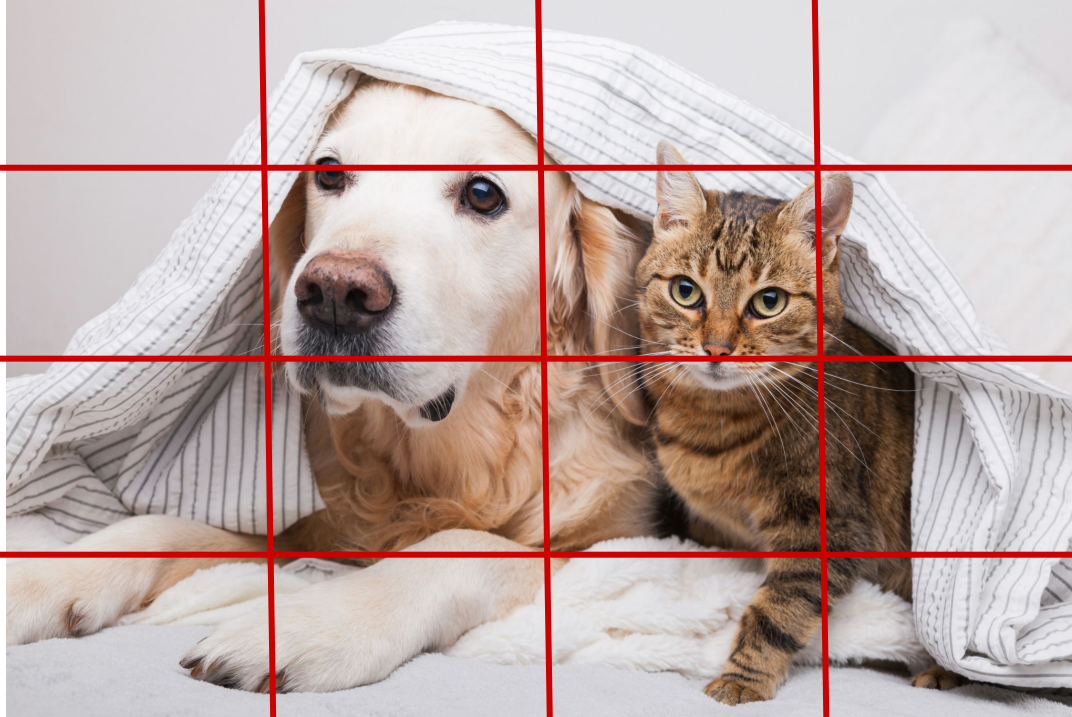
Conv Groups	Attention Groups	FLOPS (B)	Params (M)	Top-1 Acc. (%)
-	1, 2, 3, 4	7.0	18.0	80.2
1	2, 3, 4	7.3	18.1	<b>80.7</b>
1, 2	3, 4	7.5	18.5	<b>80.7</b>
1, 2, 3	4	8.0	20.8	80.2
1, 2, 3, 4	-	8.2	25.6	79.5
2, 3, 4	1	7.9	25.5	79.7
3, 4	1, 2	7.8	25.0	79.6
4	1, 2, 3	7.2	22.7	79.9

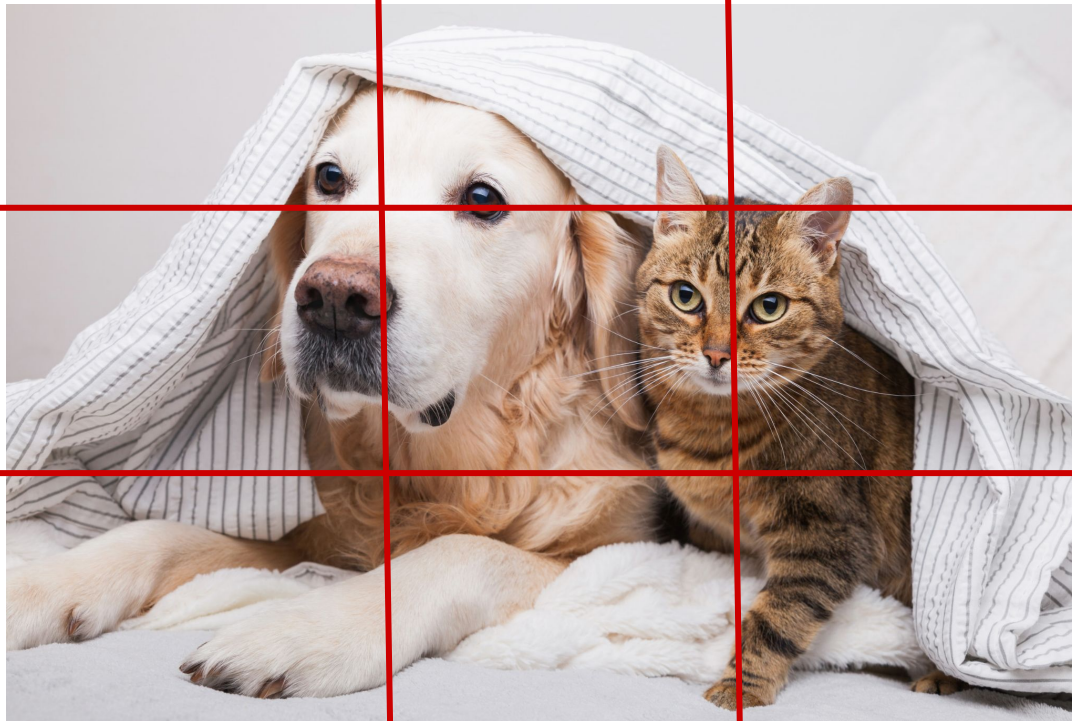
Ramachandran et al. (2019)

# Transfer Learning Advantages

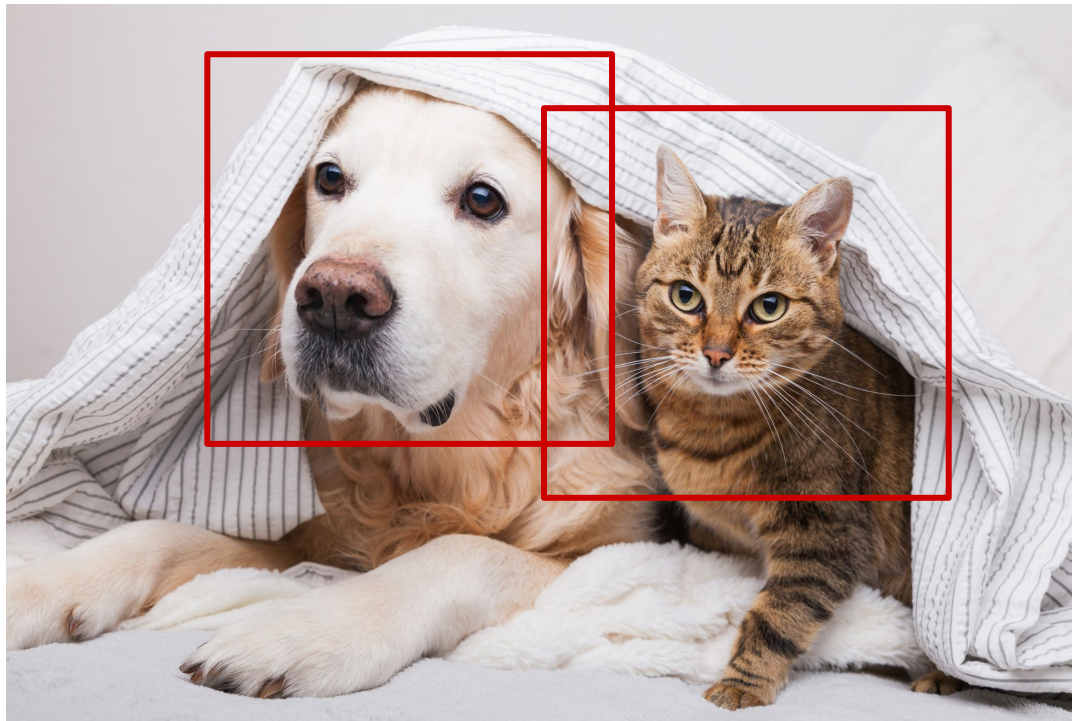


# **Is a Regular Gridding Appropriate?**





# Region of Interest Preprocessing



# Region of Interest Preprocessing

- Identify Rols
  - These become our image patches
- CNN to extract high-level representation of each patch
  - Class label?
  - Embedding vector?
- Attention to construct higher-level representations of the patches

E.g.: “A dog sitting next to a cat”





# Generative Models

Goal: produce images

- Conditioned on some input
  - Could be another image
- Generated image should be self-consistent

# Generative Models

Can be used for:

- Image clean-up
- Inpainting / Outpainting
- Upsampling
- Production of (fake) in-distribution samples for training other models
- Text to image
- Prediction of future video frames
- ...

# Transformer Image Decoder

- Producing a full, self-consistent image in one shot is challenging (pdf is high-dimensional and complex)
- Transformer approach:
  - Produce one piece of the image at a time
  - Can then condition the next piece on the pieces that have already been generated
  - Easier to produce self-consistent images

# Transformer Image Decoder

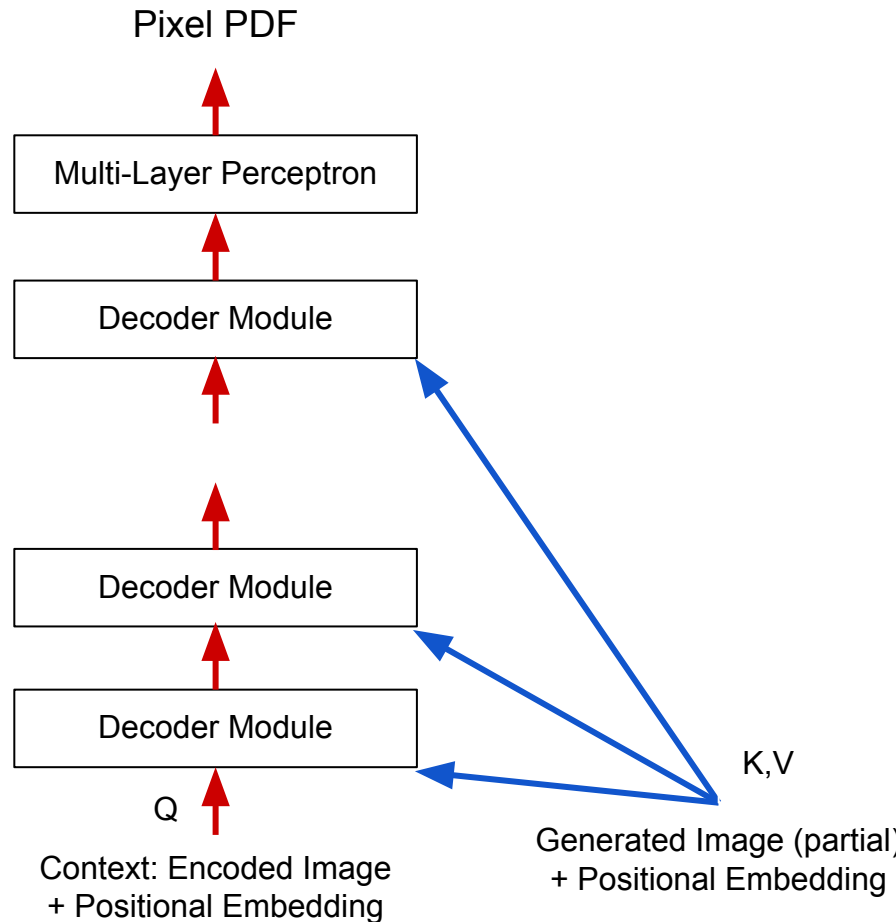
Parmar et al. (2018):

- Following PixelRNN architecture (van den Oord, 2016):  
produce pixels one at a time
- Pixels are sampled from a distribution that is conditioned on some external context + the pixels generated so far
- External context: from an **image encoder**, text encoder or other source

# Full Decoder

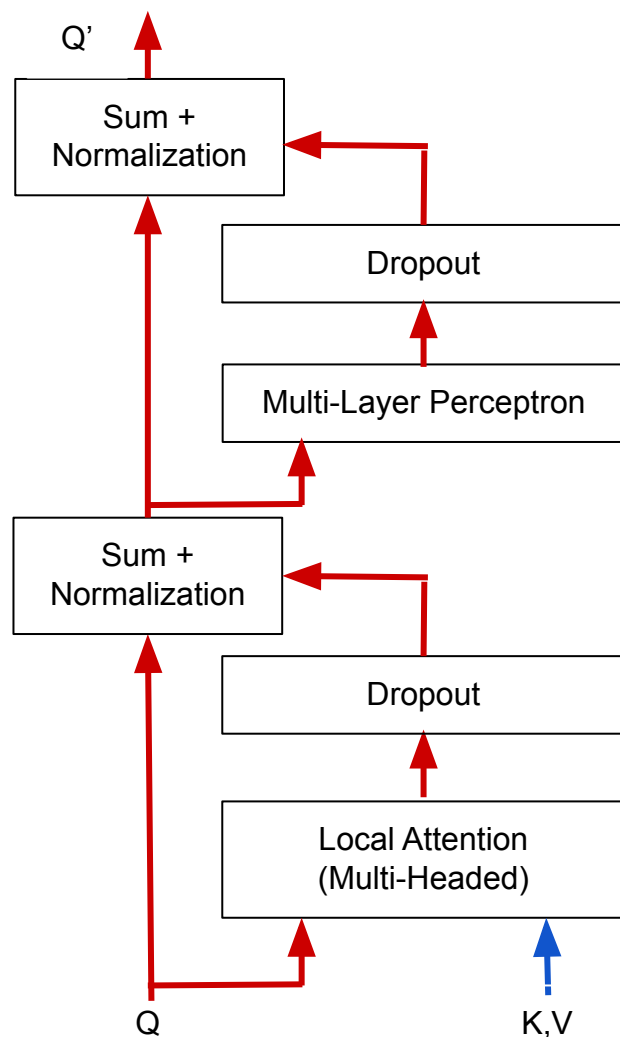
Similar in structure to our text decoders. But:

- Q: Encoder pixel
- K, V: Partially generated image



# Decoder Modules

- Similar in structure to our text decoders. But:
  - Q: Encoder pixel
  - K, V: Partially generated image
- Local Attention: only attend to a subset of pixels
- Skip connections

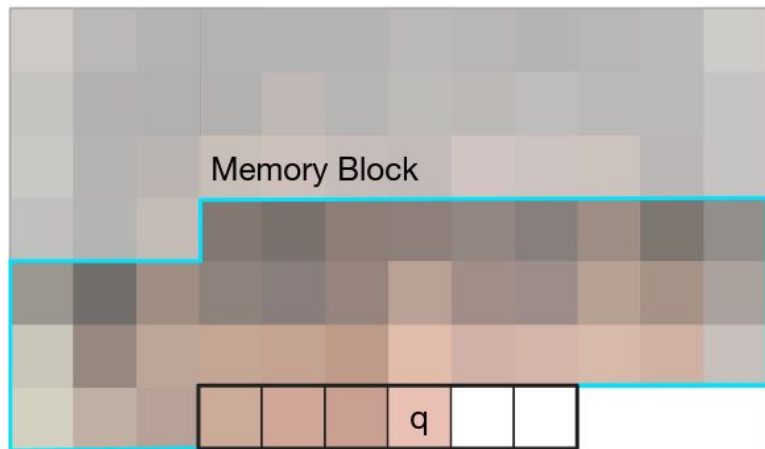


# Local Attention

- **Masked Attention:** attend only to pixels that have already been generated so far
- However, it is not feasible to allow a pixel to be able to attend to all other generated pixels
- **Local Attention:** further restrict attention to some local neighborhood
- Two varieties: 1D and 2D Attention

# Local Attention

Local 1D Attention



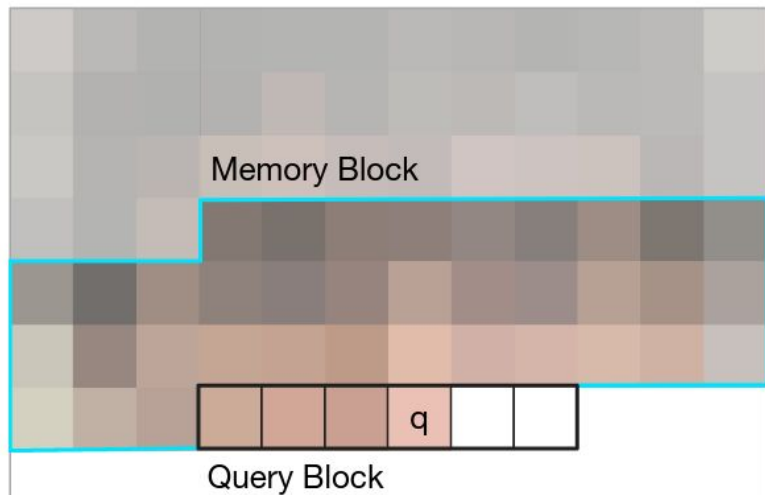
Query Block

Parmar et al. (2018)

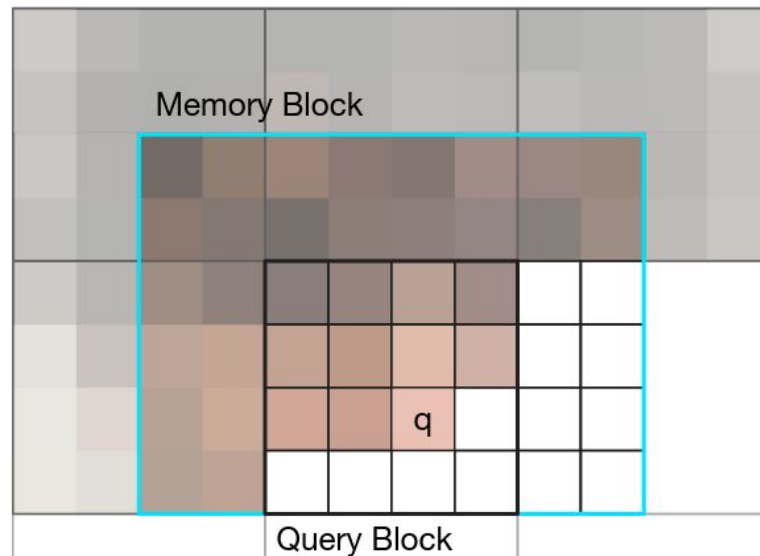


# Local Attention

Local 1D Attention



Local 2D Attention



# Decoder Output

- As a function of the contextual input and what pixel values have already been produced, network outputs a representation of the likelihood over possible pixel values
- Model samples from this distribution & adds the new pixel to what has been generated
- Process is repeated until the full image emerges

# Decoder Output

Two possibilities for representing the output pdf:

- Categorical probability distribution (van den Oord, 2016):  
represent probability for each pixel value combination  
( $3 \times 256$  parameters/pixel)
- Discretized mixture of logistics (Salimans et al., 2017):  
Gaussian-style mixture distribution (100 parameters/pixel)

# Training

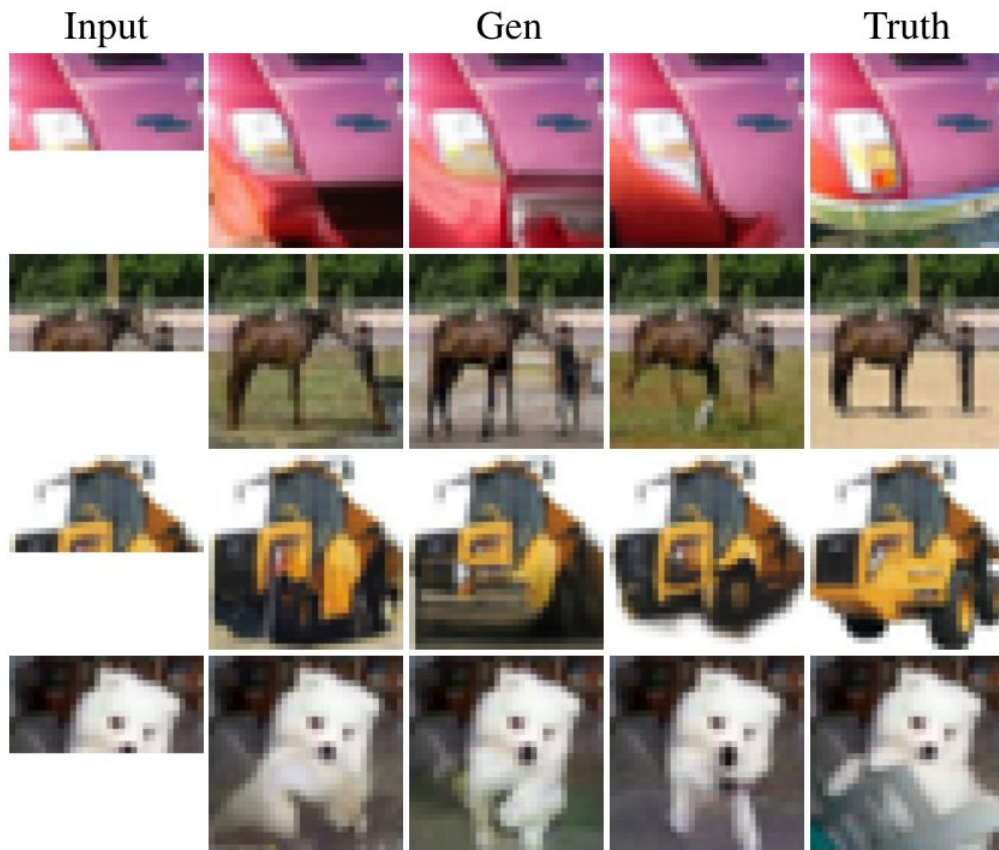
- For the results today:
  - Inputs: a modified/corrupted version of an image + (optionally) a class label
  - Outputs: the original image
- Maximize likelihood of each pixel variable:

$$LL = \sum_{i=0}^{3 \times r \times c - 1} \log p(x_i | x_0 \dots x_{i-1})$$

# Image Completion

Input: partial image

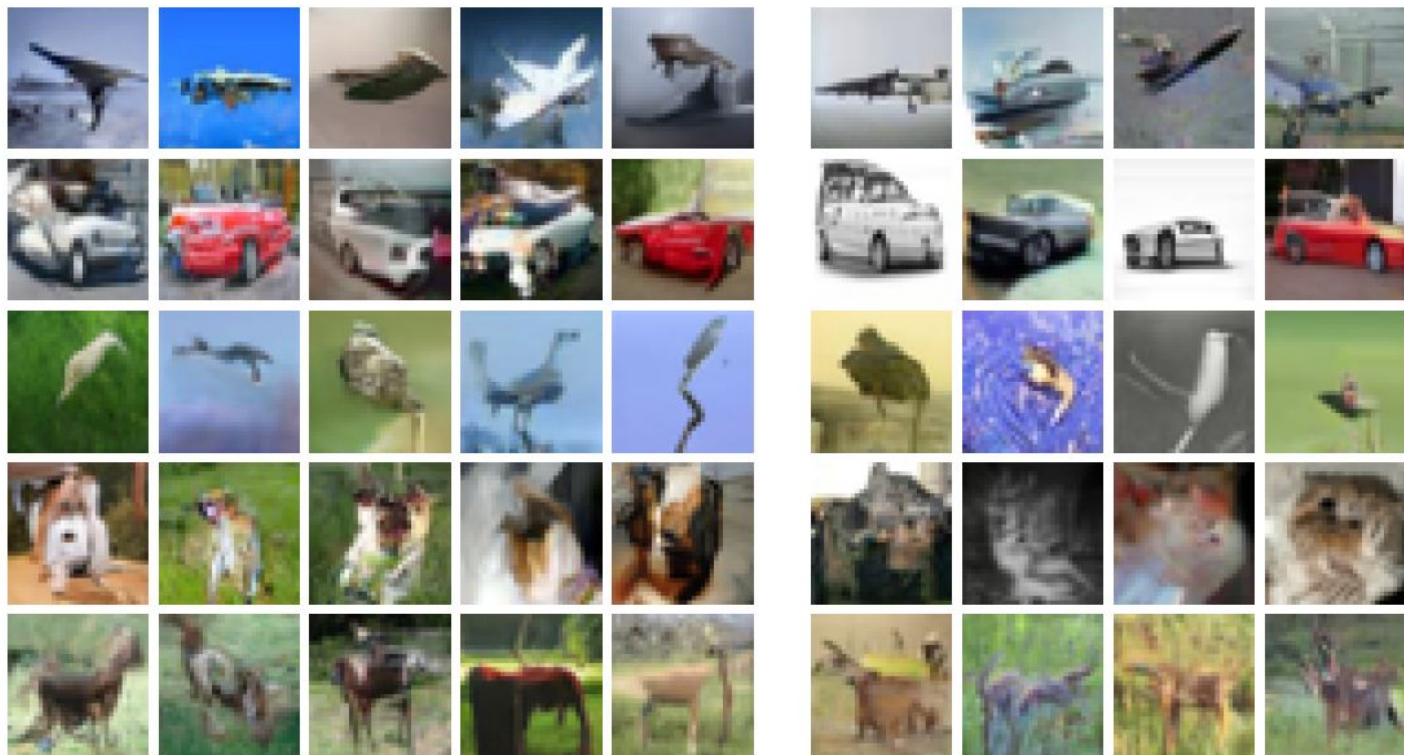
Output: generated image



# Image Generation

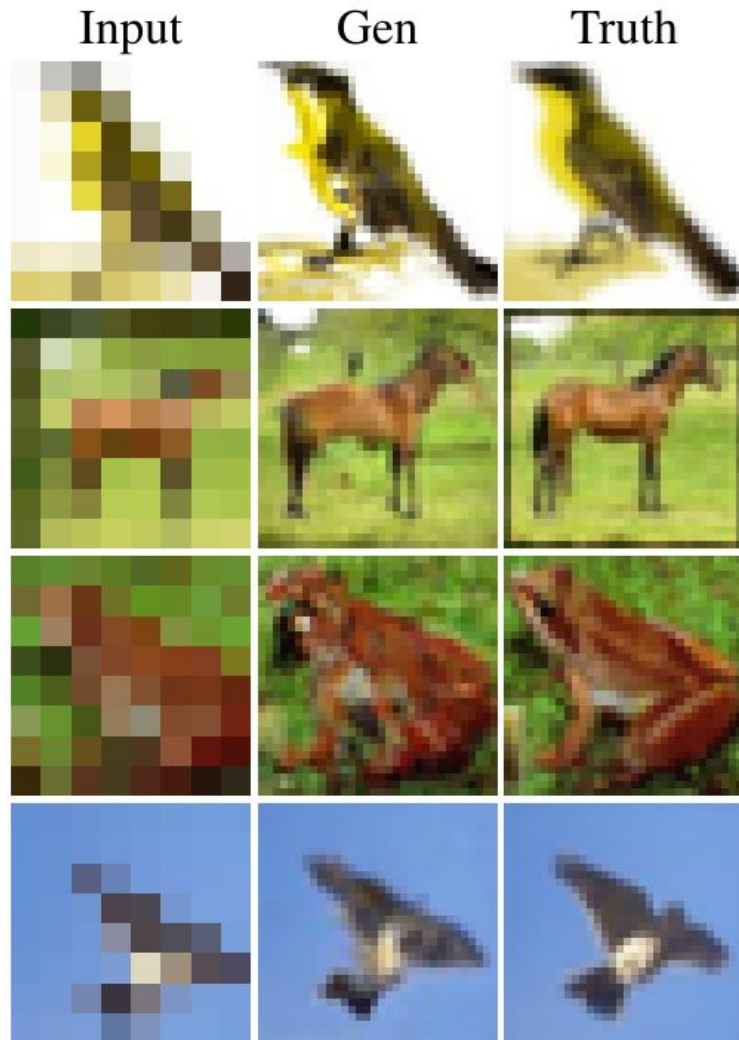
Input: image  
class

Output: 32x32  
image



# Image Upsampling

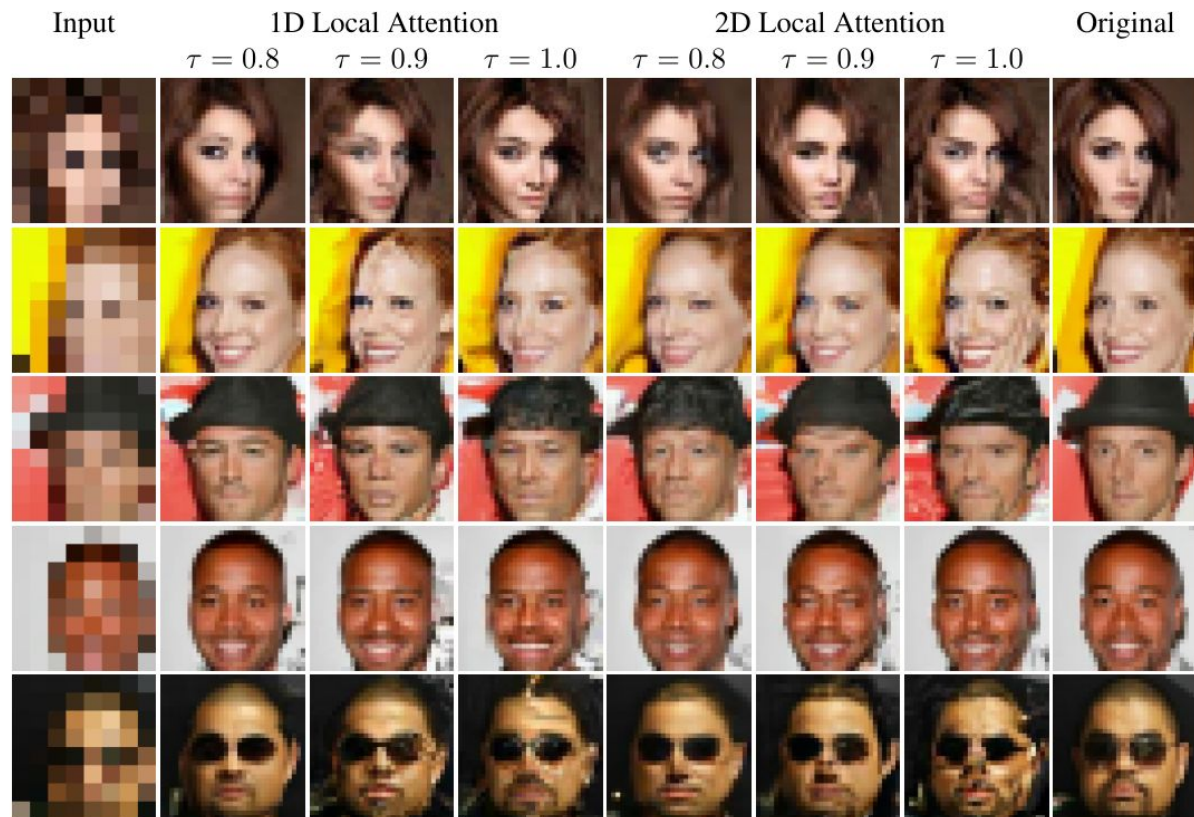
- Input: 8x8 image
- Output: 32x32 image





# Super-Resolution

Tau controls the entropy in the output pixel selection step





# Visual Self-Attention

Self-Attention can supplant convolutional modules

- Even with local Attention, receptive fields are larger
- Can also implement more complex transformations
- The cost is an increased number of parameters and the need for larger training data sets

# Decoder

Explicitly represent the pdf of the next pixel color:

- Conditioned on a contextual input and the output pixels that have already been selected
- Makes it easy to take many samples from the distribution
- Cost is that images are generated one pixel (or one channel) at a time

# References

- Vaswani et al. (2017) Attention is All You Need:  
<https://arxiv.org/abs/1706.03762>
- Alammam Blog Post:  
<http://jalammar.github.io/illustrated-transformer/>
- Kazemnejad Blog Post:  
[https://kazemnejad.com/blog/transformer\\_architecture\\_positional\\_encoding/](https://kazemnejad.com/blog/transformer_architecture_positional_encoding/)

# References

- Visual Transformers for classification:  
<https://arxiv.org/abs/2010.11929>
- Image Transformers (generators):  
<https://arxiv.org/abs/1802.05751>





