## **Ensemble Methods**

#### **Back to Decision Trees ...**

- Simple learning algorithm(s)
- Both classification and regression forms
- Classification models easily handle multiple classes
- Models can be intuitive for human experts
  - Naturally give us a sense of the most important features

## **Decision Tree Challenges**

- Splits are most often based on individual features
- Crisp region boundaries
  - Most common regression architecture: end up with a piece-wise constant function (so, it is discontinuous)
- Deep trees are necessary to capture complex models
- Deeper models:
  - > Fewer samples in the leaf nodes
  - > Brittle when it comes to generalization

## Sir Francis Galton (1822-1911)

- Meteorology: first weather maps
- Statistics: regression
- Psychology
- Heredity

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## Weighing a Cow

### Weighing a Cow

- Individually, non-experts are generally not good at guessing the weight of a cow
- However, the distribution is ~Normal, with a mean very close to the true weight

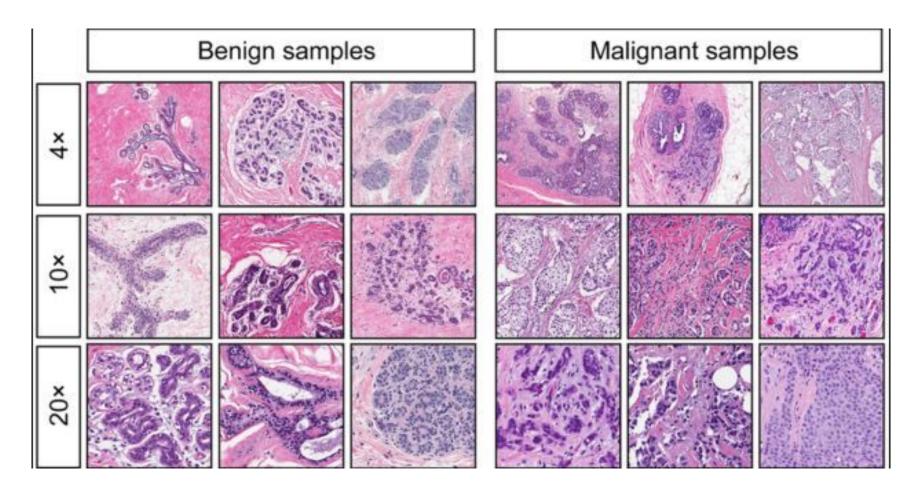
Message: Measures from a large set of *independent*, poor-quality predictors can give us a high-quality prediction

## Mixing Many Imperfect "Experts"

#### Ensemble-based methods:

- Create many models
- Combine the predictions of these models
  - Classifiers: voting
  - Regression: some mechanism for blending the predictions (e.g., computing a mean)

### **Example: Breast Cancer Classification**



Levenson et al. (2015), PLOS One

#### **Breast Cancer Classification**

#### Levenson et al:

- Trained individuals to label images of tumors as either malignant or benign
- After 2 weeks, these individuals could classify the images with an accuracy of 85%
- Hard voting classifier: the votes across the individuals were tallied
- Accuracy increased to 99%!

#### **Breast Cancer Classification**

### Hard voting classifier:

- This improvement in performance requires independence of the individuals
- The law of large numbers: combining a large number of independent random variable samples gives us the correct answer with high probability

#### **Breast Cancer Classification**

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And, the individuals in this case were pigeons...

#### **Ensemble Predictions**

- Set of trained classifiers
- Can be different types of classifiers: decision tree, logistic regression, support vector machine...
  - Different model types often capture different trends in the training set
- Combine the labels from the classifiers:
  - Hard voting: crisp answers are counted across the ensemble
  - Soft voting: average class probabilities & select the highest one

# **Example: Voting Classifier**

#### **Ensemble Predictions**

sklearn.ensemble: VotingClassifier

- Constructor:
  - List of classifiers
    - We have generally already chosen hyperparameters
  - Hard or soft voting
    - Soft voting requires predict\_proba() to be available
- fit() will fit each model in sequence
- predict() will query all models and combine the results

# **Bagging and Pasting**

#### **Ensemble Methods**

- Success of ensemble methods relies on independence of the individual models
- Can we achieve this if the models are all of the same type?

- Train each model instance with a subsample of the training set:
  - Pasting: sample without replacement
  - Bagging (bootstrap aggregation): sample with replacement
- Models can be trained in parallel

- Pasting: sample without replacement
  - All ensemble members have different training data
  - Effective training sets may not be large enough
- Bagging (bootstrap aggregation): sample with replacement
  - A single training sample may be used by multiple ensemble members -> less independence
  - But, allows us to have larger training sets

After training, a new query is addressed by asking each model to provide an answer

- Classifier: voting
- Regression: average the predictions of the individual models

## **Example: Bagging Classifier**

## Random Subspaces

- So far:
  - Bagging & pasting take random subsets of the training data
  - These are Random Patches of the data
- Sampling features:
  - Random Subspaces: only use a subset of the available features for a given model
  - Support for this also in BaggingClassifier

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### **Random Forests**

#### **Random Forests**

#### **Ensemble of Decision Trees**

- Can continue to use the Bagging Classifier
- RandomForestClassifier class does the same thing, but is optimized for classifying with decision trees
  - Hyper-parameters for this class include Decision Tree hyper-parameters and the ensemble hyper-parameters
- RandomForestRegressor also optimized for ensemble of regression trees

Adding noise to tree construction. For each possible split:

- Random forest: consider only a small subset of the available features
  - This is the Random Subspaces idea!
  - Particularly useful when there are many features possible or many possible questions
- Extra trees: consider only a subset of possible thresholds (or question parameters)
  - ExtraTreesClassifier class
  - Reduces search during each leaf node split

#### **Ensemble Methods**

- Allow us to combine many weak learners
  - Each does not have to perform very well
  - The ensemble model often performs better than the weak learners
- Bigger implications:
  - We can specifically choose simpler models (e.g., trees that are heavily regularized)
  - Cheaper to compute and leaf node predictions are based on a larger number of samples (compared to deeper trees)

- Feature Importance:
  - Which of our input features are useful in constructing our models?

- Getting this right can:
  - Help domain scientists focus their models
  - Allow us to more efficiently construct models in the future
  - Refine our data collection / storage processes

### Common approaches:

- Measure the reduction of impurity for questions involving specific features
  - Support built into the RandomForestClassifier
- How often does a feature occur in a tree?
- Where does a feature occur in a tree?
- *Importance sampling*: how does the model perform when an individual feature is corrupted?

For now, our focus is on the impurity reduction measure ...

## **Boosting**

#### **Forests**

So far: training of one tree is handled independently of other trees

- Natural parallelization
- Independence to varying degrees
  - True independence: can easily combine the output of the different models
  - In general:
    - We don't necessarily achieve true independence
    - If a part of the sample space is not well represented in the training set,
      then it will often be ignored by all of the constituent models

### **Boosting**

#### Alternative approach:

- Grow ensemble incrementally
- The model currently being learned attempts to repair prediction errors of the prior models
  - Want each new model to solve a new piece of the problem
  - With the set of models, we attempt to cover all of the training set (even the sparsely represented regions of the sample space)

#### **AdaBoost**

- Prior algorithms: all training samples have been treated with equal weight in computing the cost function
- In boosting, we adjust these weights depending on how well the current ensemble performs

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## **Example: AdaBoost**

### **Boosting**

 Advantage: at each step, we learn a new model that tries to repair problems with the prior model

The cost: we lose parallelization

## **Gradient Boosting**

### **Gradient Boosting**

- Focus: regression
- Learn a sequence of regression models
  - Each model in the sequence: try to predict the errors from the previous model
  - Then, this model's output is added to the rest of the model outputs

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# **Example: Gradient Boosting**

#### **Example: Gradient Boosting**

#### GradientBoostingRegressor class

- learning\_rate: total contribution by each tree (shrinkage)
- n\_estimators: maximum number of trees
- subsample: fraction of the number of training samples to use for a given tree
- validation\_fraction: fraction of samples to hold out to detect overfitting
- Can overfit the training data
  - Cut-off training at some number of trees based on performance
  - We can do this after the fact or dynamically

So far: we have combined the outputs of the individual models through some fixed method

- Voting, averaging ...
- Ignores the fact that some models are better than others

Exception: Boosting

We can ask another model to do this combination

- Split the training set
- First training set:
  - Train the individual models
- Second training set:
  - Each model makes predictions for the samples in the 2<sup>nd</sup> training set
  - New learner (the blender or meta-learner):
    - Inputs: predictions made by the individual models
    - Outputs: outputs from the 2<sup>nd</sup> training set

### **Ensemble Methods**

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